# **100 Excel VBA** Simulations

Using Excel to Model Risk, Investments, Genetics, Growth, Gambling and Monte Carlo Analysis

By: Dr. Gerard M. Verschuuren



**MARTIN MARTIN** 





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### Dr. Gerard M. Verschuuren

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### **Using Excel VBA to Model Risk, Investments, Genetics, Growth, Gambling, and Monte Carlo Analysis**

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### **II. INSTRUCTIONS**

All simulations in this book are supported by files that you can download from the following website: <http://www.genesispc.com/download/100VBAsimulations.zip>.

I assume that you are already familiar with many Excel features, including graphs or charts. In this book, I will only explain in more detail those features that are very helpful when you do what-if-analysis with simulations. For more basic features of Excel, I would refer you to some learning tools that you can find on [www.mrexcel.com/microsoft-office](http://www.mrexcel.com/microsoft-office-visual-learning.html)visual-learning.html.

If you want to create simulations exclusively with Excel functions and formulas, without using VBA, I recommend another book: [http://genesispc.com/tocsimulations100.htm.](http://genesispc.com/tocsimulations100.htm)

This book is not about the basics of Visual Basic (VBA) either. It only uses VBA to make simulations faster, better, and more user-friendly. If you want to learn VBA from the bottom up, I would recommend my interactive CD-ROM: <http://genesispc.com/tocvba2013CD.htm>. Yet, here are a few basic rules for using VBA:

• To start a new command line in VBA, use ENTER.

• Never use ENTER inside a command line. (In this book lines may wrap to the next line, but in VBA that is not allowed.)

• A colon (:) can separate amd combine several commands on the same line

Use an apostrophe ( $\dot{\ }$ ) for a comment after, or at the end of, a command line.

• To create shortcuts in Excel for a macro (or *Sub* in VBA), you need the *Developers* tab (if that tab is missing, go to File Options | Macros | Options | Shift + a character.

Files with macros open with the message "Enable" Content." If you find that annoying place such files in a socalled *Trusted Location*: Files | Options | Trust Center | Trust Center Setting | Trusted Locations.

- To open VBA, you can use this shortcut: ALT F11.
- On the VBA screen, choose: Insert | Module.

• I always use *Option Explicit* in VBA: Tools | Options | Require Variable Declaration.

This means you always have to declare variables with a *Dim* statement.

There are value type variables such as integer, double, string (see Appendix) and object type variables (Range, Sheet). The latter require the *Set* keyword.

• Type a *dot* (.) after an object such as Range or Chart in order to get access to its properties and methods.

It is wise to use consistent indentation to make your code more readable and checkable.

• A *With* statement allows us to refer to it later with just a simple dot (.), followed by a property or method.

• Formulas are always strings in VBA, so they should be inside double quotes ("..."). If there are double quotes inside those double quotes, they should be ""..."".

• To split a long string into several lines, you use endquotes-space-ampersand-space-underscore-enteropenquotes.

• To interrupt running code, use *Ctrl* + *Break*.

If your VBA code ever runs into trouble (and it will!), make sure you stop the Debugger before you can run the code again. You do so by clicking the *Reset* button:



### <span id="page-11-0"></span>**I. GAMBLING**

### <span id="page-11-1"></span>**Chapter 1: The Die Is Cast**

#### **What the simulation does**



We start with a very simple case of simulation—casting a die. The code generates a random number. According to that outcome, the colored die shows the appropriate number of eyes at their proper locations. Each time the random number changes, the die adjusts accordingly. The code stops when you hit the number 6.

#### **What you need to know**

Excel has a volatile function called RAND. On each recalculation, this function generates a new random number between 0 and 1. The equivalent of RAND in VBA is *Rnd*. In addition to these two operators, later versions of Excel also let you use RANDBETWEEN, which returns a random integer between two integers. Instead of using RANDBETWEEN, you can always use a more complicated formula. If you want numbers

between 1 and 6, for instance, you multiply by 6, round the number down by using the INT function, and then add 1 to the end result. More in general:  $=INT((high-low+1)*RAND() + low)$ . In VBA, you must replace RAND with *Rnd*.

Finally, we need to regulate which eyes should pop up for each new random number. This is done by using the *IIf* function in VBA. This function is a "decision maker," which determines whether a specific eye should be on or off.

*GoTo* allows the code to jump to a specific label—in this case called *Again*, followed by a colon. *GoTo* lets you jump forward or backward in code.

A *MsgBox* can just have an OK button, or a combination of OK, Cancel, Yes, and No. In case there is more than one option, an IF statement has to check what the users decided to click on.

#### **What you need to do**

**Sub Dice()**

**Dim i As Integer**

**Again: 'this is called a label that we use at the end to go back to**

 $i = Int(Rnd * 6) + 1$ **Range("B3") = IIf(i > 1, "O" , "") Range("D3") = IIf(i > 3, "O" , "") Range("B5") = IIf(i = 6, "O" , "") Range("C5") = IIf(i = 1 Or i = 3 Or i = 5, "O" , "") Range("D5") = IIf(i = 6, "O" , "") Range("B7") = IIf(i > 3, "O" , "") Range("D7") = IIf(i > 1, "O" , "") If**  $i = 6$  **Then Exit Sub If MsgBox("Number " & i & vbCr & "Again?" ,**

### **vbOKCancel) = vbOK Then GoTo Again End Sub**



### <span id="page-14-0"></span>**Chapter 2: Casting Six Dice What the simulation does**



This time we have six different dice. Each die "listens" to a random number in VBA. The settings for each die are similar to what we did in simulation 1.

There is not much new on this sheet. The main difference is that we need 6 different cells with a RAND function in order to control the six die displays. This is done with a *For*-loop in VBA, running from 0 to 5 (or 1 to 6).

When there are at least 3 dice in a row with six eyes, all dice get marked at the same time.

#### **What you need to know**

A variable of the *Variant* type can hold an array of items. We fill the array here by using the *Array* function in VBA. This array starts at 0 (that's why the *For*-loop runs from 0 to 5 instead of from 1 to 6). Notice that cell rows and columns always start at 1 (not 0).

VBA can use almost all Excel functions by calling them with *WorksheetFunction*. In this case we use Excel's COUNTBLANK function.

The use of *Range* and *Cells* in VBA can be very powerful, but can also be rather confusing at first sight (see Appendix). *Range("A1")* is equivalent to *Cells(1,1)*, but the latter one is more flexible in loops because

we can use a loop variable for the row and/or the column position. Sometimes, they are combined: *Range(Cells(1,1),Cells(10,2))* would refer to A1:B10.

Another important tool in VBA is *Offset*, with which you can specify the row offset and the column offset. For instance, *Range*("Al"). Offset(2,2) would evaluate to cell C3.

Don't confuse *End Sub* with *Exit Sub*. Each *Sub* must close with *End Sub*. But if you want to prematurely end the *Sub* routine, you must use *Exit Sub*.

**What you need to do**

```
Sub Dice()
  Dim vArr As Variant, i As Integer, r As Integer, n
As Integer, iSix As Integer, oRange As Range
  Sheet1.Cells.Interior.ColorIndex = 0
  vArr = Array("B3"
,
"F3"
,
"J3"
,
"N3"
,
"R3"
,
"V3")
Again:
  Sheet1.Cells = ""
  iSix = 0
  For r = 0 To 5
     Set oRange = Range(Range(vArr(r)),
Range(Range(vArr(r)).Offset(4, 2).Address))
     With oRange
          i = Int(Rnd * 6) + 1.Cells(1, 1) = IIf(i > 1,
"O"
,
"")
          .Cells(1, 3) = IIf(i > 3,
"O"
,
"")
          .Cells(3, 1) = IIf(i = 6,
"O"
,
"")
          .Cells(3, 2) = IIf(i = 1 Or i = 3 Or i = 5,
"O"
,
"")
          .Cells(3, 3) = IIf(i = 6,
"O"
,
"")
          .Cells(5, 1) = IIf(i > 3,
"O"
,
"")
          .Cells(5, 3) = IIf(i > 1,
"O"
,
"")
          If WorksheetFunction.CountBlank(.Cells)
= 9 Then iSix = iSix +1
```

```
End With
Next r
n = n + 1If iSix >= 3 Then
  Cells.Interior.Color = vbYellow
  MsgBox "3x6 or more! After " & n & " runs."
  Exit Sub
End If
If MsgBox(n & " runs. Again?"
, vbOKCancel) =
```
**vbOK Then GoTo Again End Sub**



## <span id="page-18-0"></span>**Chapter 3: Roulette Machine**

**What the simulation does**



Most people believe that if they keep consistently betting "odd," the ball will most certainly land on an odd number sometime soon. This is called "the law of averages" which says, the longer you wait for a certain random event, the more likely it becomes.

Do not believe it! Try it out in this "real life" simulation and find out how the casino makes money on people who think that way. You may initially gain but eventually lose.

The code clears previous results in the columns A:C when you start the code. Column A simulates a roulette with 1,000 random numbers between 1 and 36. In column B, the code types 1 if you confirm an odd number through the *MsgBox*, expecting the next number to be odd otherwise 2 for even.

Column C keeps track of the score: it adds 1, when your prediction was correct—otherwise it subtracts 1.

Once you hit *Cancel*, a *MsgBox* tells you whether you won or lost, and with which score.

#### **What you need to know**

*CurrentRegion* represents the entire range bounded by any combination of blank rows and blank columns. So in the above case, that would be A1:C5, and in the case below A1:C11.

Excel has a MOD function that returns the remainder after a number is divided by a divisor. For instance,  $=MOD(3, 2)$  returns the remainder of the division 3/2, which is 1. VBA, however, uses the *Mod* operator, which does basically the same. So the syntax would be*: 3 Mod 2*, which also returns 1.

**What you need to do**

```
Sub Guess()
  Dim r As Long, iGuess As Integer, vGuess As
Variant, oRange As Range
  Range("A1").CurrentRegion.Offset(1, 0).Delete
  Do
    r = Range("A1").CurrentRegion.Rows.Count + 1
    vGuess = MsgBox("Odd (Yes), Even (No), Stop
(Cancel)"
, vbYesNoCancel)
     Select Case vGuess
       Case 6: Cells(r, 2) = 1
       Case 7: Cells(r, 2) = 2
       Case 2: GoTo Report
    End Select
     Cells(r, 1) = Int(Rnd * 50) + 1
     Cells(r, 3) = IIf(Cells(r, 1) \text{ Mod } 2 = Cells(r, 2)Mod 2, Cells(r - 1, 3) + 1, Cells(r - 1, 3) - 1)
  Loop
Report:
  Set oRange =
Cells(Range("A1").CurrentRegion.Rows.Count, 3)
  MsgBox "You " & IIf(oRange < 1,
"lost"
,
"won")
& " with a score of " & oRange
End Sub
```


### <span id="page-22-0"></span>**Chapter 4: An X-O Game**

#### **What the simulation does**



This is a game with two players who "choose" X or O randomly. They win when a row or column has the same entries. As soon as a row or column has different entries, the word "lost" gets displayed. As soon as all 5 entries in a row or column are the same, the game is won. A *MsgBox* displays the endresult and keeps track of previous results during the game.

#### **What you need to know**

*Option Explicit* at the beginning of the code requires that all variables are explicitly declared as of a certain type with a *Dim* statement. This is a safe way to prevent you from misspelling a variable farther down in your code.

*Do*-loops run an unspecified number of times *until* a certain condition kicks in or *while* that condition persists.

To keep track of previous results, we need a *global* variable. Local variables are declared inside a *Sub*, but global variables need to be declared at the top of the *Module*. They retain information until the file is closed.

We also use the *Timer* of VBA. The *Timer* counts the number of seconds since midnight on your machine. This way we can pause a process for a short time. *DoEvents* prevents that the system is blocked during that time period.



**What you need to do**

**Option Explicit**

**Dim iO As Integer, iX As Integer, iTotal As Integer**

```
Sub IntelligentGame()
  Dim oBoard As Range, bPlayer As Boolean, i As
Integer, oCell As Range
  Dim iRow As Integer, iCol As Integer, iTime As
Long
  Set oBoard = Range(Cells(1, 1), Cells(5, 5))
  With oBoard
    .Cells(1.1).CurrentRegion.Clear
    .BorderAround , xlThick :
.Cells.HorizontalAlignment = xlCenter
    Do
       bPlayer = Not bPlayer
       Do
         iRow =
WorksheetFunction.RandBetween(1, 5)
         iCol = WorksheetFunction.RandBetween(1,
5)
         If .Cells(iRow, iCol) = "" Then
            .Cells(iRow, iCol) = IIf(bPlayer,
"X"
,
"O"): Exit Do
         End If
       Loop
```

```
i Time = Timer + 1
       Do Until Timer > iTime
         DoEvents
       Loop
       For i = 1, To 5If
WorksheetFunction.CountIf(.Rows(i).Cells,
"X") >=
1 And WorksheetFunction.CountIf(.Rows(i).Cells,
"O") >= 1 Then .Cells(i, 6) = "Lost"
         If
WorksheetFunction.CountIf(.Columns(i).Cells,
"X")
>= 1 And
WorksheetFunction.CountIf(.Columns(i).Cells,
"O")
>= 1 Then .Cells(6, i) = "Lost"
       Next i
       If WorksheetFunction.CountIf(.Cells(1,
1).CurrentRegion.Cells,
"Lost") = 10 Then MsgBox
"No winner": Exit Do
       For i = 1 To 5
         If
WorksheetFunction.CountIf(.Rows(i).Cells,
"X") = 5
Then MsgBox "X is the winner.": iX = iX + 1: Exit
Do
         If
WorksheetFunction.CountIf(.Rows(i).Cells,
"O") = 5
Then MsgBox "O is the winner.": iO = iO + 1: Exit
```
**Do**

**If**

**WorksheetFunction.CountIf(.Columns(i).Cells, "X")**  $=$  **5** Then MsgBox "X is the winner.":  $iX = iX + 1$ : **Exit Do**

**If**

**WorksheetFunction.CountIf(.Columns(i).Cells, "O")**  $=$  **5** Then MsgBox "O is the winner.":  $iO = iO + 1$ : **Exit Do**

**Next i**

**If WorksheetFunction.CountBlank(oBoard) = 0 Then MsgBox "No winner": Exit Do**

**Loop**

**End With**

**iTotal = iTotal + 1**

**MsgBox "X won " & iX & vbCr & "O won " & iO & vbCr & "in " & iTotal & " games." End Sub**

### <span id="page-27-0"></span>**Chapter 5: A Slot Machine What the simulation does**



This spreadsheet makes 20 runs for each game (columns F:H). Each run creates 3 random numbers between  $-2$  and  $+2$ , and then calculates the cumulative total in column J. After 20 runs, a new game starts.

The results for each game are recorded in columns N and O. After 20 games, the average score features in cell R3. At any moment, the user can cancel further runs and a *MsgBox* reports what the average score was in X games of 20 runs. Then the process can start all over with run 1 for game 1.

#### **What you need to know**

To make all of this possible, we need a *Do*-loop for the runs inside a *Do*-loop for the games. Besides we added a *Timer* loop so the results come in gradually

To make the code more understandable, we used *Range Names* here that were assigned in Excel. The range name "games," for instance, refers to the range \$N\$2:\$N\$21.

The VBA function *FormatNumber* lets you determine the number of

decimals by specifying the second argument.

Instead of using RANDBETWEEN(-2,2), we can use also: *-2 + Int(Rnd \* 5).*

**What you need to do**

#### **Option Explicit**

```
Sub Run()
  Dim iRun As Integer, iGame As Integer, pTime As
Long
  Range(Cells(2, 1), Cells(21, 18)).ClearContents
  Do
    iRun = iRun + 1
    Do
       iGame = iGame + 1With Range("Runs")
         .Cells(iGame, 1) = iGame
         .Cells(iGame, 2) = -2 + Int(Rnd * 5)
         .Cells(iGame, 3) = -2 + Int(Rnd * 5)
         .Cells(iGame, 4) = -2 + Int(Rnd * 5)
         Range("cumsums").Cells(iGame,
1).FormulaR1C1 = "=SUM(RC[-4]:RC[-2])"
       End With
       pTime = Timer + 0.5
       Do While Timer < pTime
         DoEvents
       Loop
    Loop Until iGame = 20
    Range("run") = iGame
```

```
iGame = 0Range("game") = iRun
    Range("games").Cells(iRun, 1) = "Game " &
iRun
```

```
Range("gamescores").Cells(iRun, 1) =
Range("cumsums").Cells(20, 1)
```

```
Range("avgscore").Formula =
```

```
"=average(gamescores)"
```
**If iRun = 20 Then Exit Do**

**Loop Until MsgBox("New run?" , vbOKCancel) = vbCancel**

**MsgBox "Average of " &**

**FormatNumber(Range("avgscore"), 1) & " in " & iRun & " games of 20 runs" End Sub**



### <span id="page-31-0"></span>**Chapter 6: Gamblers' Ruin What the simulation does**



This sheet simulates what may happen to people who are addicted to gambling. When we run the code, we are asked how many chances we want in column A to go for odd or even. We simulate a 50% probability for either choice. If the choice was correct, the count in column A goes up by 1, otherwise it goes down by 1. All this is done on a new sheet.

Next we simulate that this addicted player repeats the game for some twenty more times. This is done with a *Data Table* in D:H (see Appendix). In its top row, we calculate average, minimum, maximum, standard deviation, and the final score (in column H). At the end, we calculate how often the player had a positive final score, and how often a negative one. Most of the work goes into the conditional formatting bars.

#### **What you need to know**

Usually a *Data Table* has *have* a formula in the first cell—which would be cell C1 in our case. Based on that formula, a *Data Table* typically uses a row input of variables and a column input of variables to recalculate the formula placed at its origin. It does so by filling the table cells with a formula that has the following syntax:  $\{=\text{TABLE}(\text{row-input}, \text{col-input})\}$ .

In this case we use a *Data Table* merely to trick Excel into simulating 20 (or many more) iterations of column A. We do so by not placing a formula at the origin, but by leaving the row-input argument empty, and having the col-input argument refer to an empty cell somewhere outside the table. Yes, that does the trick!

By using *Worksheet.Add* we create a new worksheet either before (1st argument) or after (2<sup>nd</sup> argument after the comma) the *Activesheet*, which is the sheet we are currently on.

An *InputBox* provides users to provide their own input for variables or questions.

**What you need to do**

**Sub Gambling() Dim oWS As Worksheet, iRow As Long iRow = InputBox("How many rows?" , , 100) Set oWS = Worksheets.Add( , ActiveSheet)**  $Range("A1") = 0$ **Range(Cells(2, 1), Cells(iRow, 1)).Formula = "=IF(RAND()>0.5,A1+1,A1-1)" Range("D1") = "Average": Range("D2").Formula = "=AVERAGE(A:A)" Range("E1") = "Min": Range("E2").Formula = "=MIN(A:A)" Range("F1") = "Max": Range("F2").Formula = "=MAX(A:A)" Range("G1") = "SD": Range("G2").Formula = "=STDEV(A:A)" Range("H1") = "Final": Range("H2").Formula = "=" & Cells(iRow, 1).Address(False, False) Range(Range("C2"), Range("H22")).Table , Range("B2") Dim oRange As Range, oFormat As**

**FormatCondition**

**Set oRange = Range(Range("D2"), Range("D22")) Set oFormat =**

**oRange.FormatConditions.Add(xlCellValue, xlLess, "=0")**

**oFormat.Interior.Color = 13551615**

**'Conditional Formatting with Bars (only in later versions of Excel) Dim oBar As Databar Set oRange = Range(Range("H2"), Range("H22")) oRange.ColumnWidth = 15 Range("H24").Formula = "=AVERAGE(" & oRange.Address & ")" Set oBar = oRange.FormatConditions.AddDatabar oBar.MinPoint.Modify newtype:=xlConditionValueAutomaticMin oBar.MaxPoint.Modify newtype:=xlConditionValueAutomaticMax oBar.BarFillType = xlDataBarFillGradient oBar.Direction = xlContext oBar.NegativeBarFormat.ColorType = xlDataBarColor oBar.BarBorder.Type = xlDataBarBorderSolid oBar.NegativeBarFormat.BorderColorType = xlDataBarColor oBar.AxisPosition = xlDataBarAxisAutomatic oBar.BarColor.Color = 13012579 oBar.NegativeBarFormat.Color.Color = 5920255 ActiveWindow.Zoom = 130**

**Dim sMsg As String**

**sMsg = WorksheetFunction.CountIf(Columns(4),**

**">0") & " runs with average above 0"**

**sMsg = sMsg & vbCr & "Average of final scores: " & FormatNumber(Range("H24"), 2)**

**MsgBox sMsg**

**End Sub**
### **Chapter 7: Lottery Numbers What the simulation does**



Each time we run this macro, the code creates a 4-digit random number in cell F1. Then it tries to match that number by creating new 4-digit random numbers until the two numbers match.

After each match, it plots in column A how many times—how many "tickets"—it took to find a match. The simulation keeps doing this until we hit the No-button in the *MsgBox*.

#### **What you need to know**

Each random digit is generated by *Int(Rnd \* 10)*. The *Int* function always rounds down to the nearest integer  $(0 - 9)$ . But because this digit has to be incorporated in the 4-digit lottery number, we need also the *CStr* function which converts the number into a *String*.

To "string" things together, we always need [space][ampersand] [space] between the individual strings that need to be "stringed" together.

*Do*-loops are perfect when we don't know ahead of time how many loops we need. The loop can be stopped by adding a *While* or *Until* condition on the *Do*-line or the *Loop*-line. Another possibility is—which we did here—using an *IF*-statement. If the condition of the *If*-statement kicks in, we perform an *Exit Do* (not to be confused with an *Exit Sub*), which takes us to the line after the *Loop*-statement.

#### **Option Explicit**

```
Sub Lottery()
  Dim sNumber As String, sGuess As String, i As
Integer, j As Long, n As Long
  Range("A1").EntireColumn.Clear
  If MsgBox("New winning number?"
, vbYesNo) =
vbYes Then
    sNumber = ""For i = 1 To 4
       sNumber = sNumber & CStr(Int(Rnd * 10))
    Next i
    Range("F1") = "'" & sNumber
  Else
    sNumber = Range("F1")
  End If
  Do
    For i = 1 To 4
       sGuess = sGuess & CStr(Int(Rnd * 10))
    Next i
    n = n + 1If CStr(sNumber) = CStr(sGuess) Then
      j = j + 1Cells(j, 1) = "After " & n & " tickets."
```
#### $n = 0$ **If MsgBox("Another run?" , vbYesNo, sGuess) = vbNo Then Exit Do End If sGuess = "" Loop End Sub**



# **Chapter 8: Win or Lose?**

**What the simulation does**



After each trial, the macro plots the current time in Column A, then a random win or lose amount of money in column B, and a cumulative total of what has been won or lost so far in column C.

When we decide to quit, a *MsgBox* reports to us how much we have won or lost in total after an X number of trials.

#### **What you need to know**

The *Now* function returns the serial number of the current date and time. If the cell format was *General* before the function was entered, Excel changes the cell format so that it matches the date and time format of your regional settings.

*AutoFit* widens the *EntireColumn* to its widest entry. It does so for the entire sheet if you use *Cells*, or for a specific range on the sheet that you specify—for instance, *Cells(1,1).*

*FormulaR1C1* uses a row and column notation—for instance, R1C1 instead of the more common notation of A1. To use this notation also in Excel itself, you can go here: File | Options | Formulas | R1C1 reference style.

*FormulaR1C1* can have relative or absolute references. Here are some examples: *RC* refers to the same row and column number as where the cell itself is located; *R1C1* refers to a cell in row 1 and column 1 (which is A1); *R[-1]C[1]* refers to 1 row up and 1 column to the right of where the reference is located (see Appendix).

*FormatCurrency* does something similar to what *FormatNumber* does. It lets you specify the number of decimals in the 2<sup>nd</sup> argument, but it also adds a currency symbol (which is a non-numeric entity).

**Sub WinOrLose() Dim i As Long, sMsg As String Columns("A:C").ClearContents Range("A1") = "Time": Range("B1") = "WinOrLose": Range("C1") = "Total"**  $For i = 2$  To  $1000$ **Cells(i, 1) = Now Cells(i, 2) = FormatCurrency(1 - 2 \* Rnd, 2) Cells(i, 3).FormulaR1C1 = "=SUM(R2C2:RC2)" Cells.EntireColumn.AutoFit If MsgBox("Another trial?" , vbYesNo) = vbNo Then Exit For Next i With Cells(i, 3)** If  $\mathbf{.Value} \geq 0$  Then  $\mathbf{sMsg} = \mathbf{''you}$  WON:  $\mathbf{''}$  Else **sMsg = "you LOST: " MsgBox "After " & i - 1 & " trials " & sMsg & FormatCurrency(Cells(i, 3), 2) End With End Sub**



# **Chapter 9: A Letter Game**

**What the simulation does**



The macro asks you first whether you want to use the  $1<sup>st</sup>$  or the  $2<sup>nd</sup>$ sheet. The  $2<sup>nd</sup>$  sheet uses "weighting"; the weight of each character is assigned in column O. Then the macro asks which word should be found; don't make this more than 2 characters long, for that could be a very timeconsuming search.

In a *Do*-loop with two nested *For*-loops, the code scans all numbers in B1:K10 until it finds the word you are looking for. Obviously, that goes faster with "weighted" characters.

#### **What you need to know**



All capitals have an ASCI number between 65 and 90. The Excel function CHAR returns the corresponding letter. Column M totals the scores in column O cumulatively. So cell M2 has this formula: =SUM(O1:\$O\$1). Now VLOOKUP can find a random number between 0 and 70 in column M, and then return the corresponding letter from column N. VLOOKUP always searches *vertically*, from top to bottom, in the *first* column of a table and then finds a corresponding value in a column to the right, specified by a *number*. So we need a lookup column of cumulative values before column N. Besides, VLOOKUP looks for the previous value in an *ascending* order.

#### **Option Explicit**

```
Sub Letters()
  Dim sWord As String, oRange As Range, c As
Integer, r As Integer, n As Integer, sFormula As String
  Application.Calculation = xlCalculationManual
  If MsgBox("Equal chars (Y) or weighted chars
(N)?"
, vbYesNo) = vbYes Then
    Sheet1.Activate
    sFormula =
"=CHAR(RANDBETWEEN(65,90))" '65-90 are the
capitals
  Else
    Sheet2.Activate
    sFormula =
"=VLOOKUP(RANDBETWEEN(0,70),$M$1:$N$26,2)"
  End If
  Set oRange = Range("B1:K10")
  oRange.ClearContents:
oRange.Interior.ColorIndex = 0
  sWord = InputBox("Which 2-letter word?"
, ,
"NO")
  sWord = UCase(Left(sWord, 2))
  oRange.Cells.Formula = sFormula
```
**With oRange Do Sheet1.Calculate**  $n = n + 1$  $For r = 1 To . Rows. Count$  $For c = 1 To . Columns. Count$ **If .Cells(r, c) = Left(sWord, 1) Then If c < .Columns.Count Then** If  $.Cells(r, c + 1) = Right(sWord,$ **1) Then Exit Do 'so this loop stops when it finds one (the 1st) case End If End If Next c Next r Loop Until MsgBox("Trial " & n & ": not found! Try again?" , vbYesNo) = vbNo .Range(.Cells(r, c - 1), .Cells(r, c)).Interior.Color = vbYellow MsgBox "Found " & sWord & " after " & n & " trials" & vbCr & \_ "in cells " & .Cells(r, c).Address & "+" & .Cells(r, c + 1).Address End With End Sub**

# **Chapter 10: A Three-Way Circuit What the simulation does**



This sheet has a simulation of a three-way circuit. It is, for example, used when a light is regulated by two switches. Either switch can turn the light on or off, but the connections have to be in a certain way, as explained in the diagrams to the right.

The position of the switches in column C and F is regulated randomly by either showing the switch with a black font or hiding it with a white font.

#### **What you need to know**

This time we declare *Boolean* variables, which can only be either True(1) or False  $(0)$ .

In an *IF*-statement we use a combination of *And* and *Or* operators.

Like *FormatCurrency*, the *FormatPercent* function has a 2<sup>nd</sup> argument for the number of decimals, and it adds the %-sign as a non-numeric entity.

This is ON:



This is OFF:



#### **Option Explicit**

```
Sub Hits()
  Dim b1 As Boolean, b2 As Boolean, b3 As Boolean,
b4 As Boolean
  Dim iHit As Integer, n As Integer, sMsg As String
  Do
    If Rnd > 0.5 Then
      Range("C4").Font.Color = vbBlack:
Range("C5").Font.Color = vbWhite

    Else
      Range("C4").Font.Color = vbWhite:
Range("C5").Font.Color = vbBlack
      b1 = False: b2 = True
    End If
    If Rnd > 0.5 Then
      Range("F4").Font.Color = vbBlack:
Range("F5").Font.Color = vbWhite
      b3 = True: b4 = FalseElse
      Range("F4").Font.Color = vbWhite:
Range("F5").Font.Color = vbBlack
      b3 = False: b4 = True
```

```
End If
    n = n + 1If (b1 And b3) Or (b2 And b4) Then iHit = iHit +
1
    sMsg = sMsg & "Runs: " & n & vbTab & "Hits:
```
**" & iHit & vbTab & FormatPercent(iHit / n, 0) & vbCr**

**MsgBox sMsg**

**Loop Until MsgBox("Again?" , vbYesNo) = vbNo End Sub**

# **Chapter 11: Flocking Behavior**

#### **What the simulation does**



Flocking behaviorr is the behavior exhibited when a group of birds, called a flock, are foraging or in flight. There are clear parallels with the shoaling behavior of fish, the swarming behavior of insects, and herd behavior of land animals. It is considered the emergence of collective behavior arising from simple rules that are followed by individuals and does not involve any central coordination

Scientists have demonstrated a similar behavior in humans. In their studies, people exhibited the behavioral pattern of a "flock": If a certain percentage of the flock changes direction, the others follow suit. In experiments, when one person was designated as a "predator" and everyone else was supposed to avoid him or her, the human flock behaved very much like a school of fish.

#### **What you need to know**



We assume that all animals (100) start randomly in one of four different directions (M2:N5). Once animals with a certain direction happen to gain a certain percentage (say, 35%), all the other animals follow suit.

In the range B2:K11 we place a VLOOKUP function that finds in M2:M5 a random number between 0 and 1, and then returns the corresponding direction arrow. Once column O registers a count over 35, all cells in B2:K11 display that arrow, and the count becomes 100. In other words, the flock has "decided" in which direction to fly or to swim.

**Option Explicit**

```
Sub FlockBehavior()
  Dim oRange As Range, i As Integer, bWon As
Boolean, pTime As Double
  Set oRange = Range("B2:K11")
  oRange.ClearContents
  Do
    oRange.Formula =
"=VLOOKUP(RAND(),$M$2:$N$5,2)"
    oRange.Formula = oRange.Value
    pTime = Timer + 0.5 'Timer: secs since
midnight; pause by .5 seconds
    Do While Timer < pTime
       DoEvents
    Loop
    For i = 1 To 4
      If \text{Range}("O1"). Offset(i, 0) >= 35 Then bWon
= True: Exit For
    Next i
  Loop Until bWon = True
  If bWon Then oRange =
WorksheetFunction.VLookup("+"
,
Range("$P$2:$Q$5"), 2, 0)
```
#### **MsgBox "One direction" End Sub**



# **II. STATISTICS Chapter 12: Samples What the simulation does**



The simulation first asks how many rows we want to plot on a new sheet. Each cell in that range—in the above case range B2:K18—holds a random number between 0 and 10. Columns O and P hold two frequency tables. The top one calculates frequencies for row 2, which are the values for a sample of 10 cases. The bottom one calculates frequencies for row 20, which holds the averages of each column based on a sample of  $17x10=170$ cases.

It is to be expected that the frequency curve for the large sample resembles more of a normal distribution than the curve for the small sample of 10 cases. Below is the result of 25 rows.

#### **What you need to know**



The FREQUENCY function is a so-called array function. That means in Excel, you have to select multiple cells at once and accept the formula with  $Ctrl + Shift + Enter$  (on a Mac: Command + Return). In VBA you do this by using the *FormulArray* property of a range of cells.

We also added two *ChartObjects* to the code and the sheet. They are numbered in the order they were created: 1 and 2. Notice that *SetSourceData* is followed by a space—yes, every minute detail counts in VBA!

**Option Explicit**

```
Sub Samples()
  Dim oWS As Worksheet, iRow As Long, oRange As
Range, oChart As Chart
  iRow = InputBox("How many rows on a new
sheet?"
, , 25) + 2
  Set oWS = Worksheets.Add(, ActiveSheet)
  Range(Cells(2, 2), Cells(2, 11)).Formula =
"=INT(RAND()*11)"
  Range(Cells(2, 2), Cells(2, 11)).Interior.Color =
vbYellow
  Cells(2, 13).Formula = "=STDEV(B2:K2)"
  Range(Range("A2"), Cells(iRow, 11)).Table ,
Range("A1")
  Set oRange = Range(Cells(iRow + 2, 2), Cells(iRow
+ 2, 11))
  oRange.FormulaR1C1 = "=AVERAGE(R[-2]C:R[-
" & iRow & "]C)"
  oRange.Interior.Color = vbYellow
  Cells(iRow + 2, 13).FormulaR1C1 =
"=STDEV(RC[-11]:RC[-2])"
  Range("O2:O11").Formula = "=ROW(A1)"
  Range("P2:P11").FormulaArray =
```

```
"=FREQUENCY(B2:K2,O2:O11)"
 Range("O14:O23") = "=ROW(A1)"
 Range("P14:P23").FormulaArray =
"=FREQUENCY(" & oRange.Address &
"
,O14:O23)"
```

```
Range("O2:P11").Select
  oWS.Shapes.AddChart2(240,
xlXYScatterLines).Select
  ActiveChart.SetSourceData oWS.Range("O2:P11")
  ActiveChart.HasTitle = False
  oWS.ChartObjects(1).Top = Range("R2").Top
  oWS.ChartObjects(1).Left = Range("R2").Left
  oWS.ChartObjects(1).Width = 300
  oWS.ChartObjects(1).Height = 150
```

```
Range("O14:P23").Select
  oWS.Shapes.AddChart2(240,
xlXYScatterLines).Select
  ActiveChart.SetSourceData
oWS.Range("O14:P23")
  ActiveChart.HasTitle = False
  oWS.ChartObjects(2).Top = Range("R14").Top
  oWS.ChartObjects(2).Left = Range("R14").Left
  oWS.ChartObjects(2).Width = 300
  oWS.ChartObjects(2).Height = 150
  Range("A1").Select
```
#### **End Sub**

### **Chapter 13: A Normal Distribution What the simulation does**



The macro places a new distribution on a new sheet with a number of rows in column A that you the user chose in a *MsgBox*, based on a mean and SD of our choosing as well. Column C has the number of bins chosen, column D the frequencies for each bin, and column E what the corresponding normal distribution values would be.

#### **What you need to know**



The function NORMINV (or NORM.INV, if available) in column A returns the inverse of the normal cumulative distribution for the specified mean and standard deviation. The function NORMDIST in E returns the normal distribution for the specified mean and standard deviation.

By replacing the *Formula* property of a range with its *Value* property, we are mimicking a *Paste Special* procedure for values—so that things don't keep recalculating.

The Chart has two cases of a *FullSeriesCollection*, 1 and 2.

**Option Explicit**

**Sub Bins()**

**Dim iSize As Integer, pMean As Double, pSD As Double, iBins As String, oWS As Worksheet**

**iBins = 15**

**iSize = InputBox("New sheet: The size of your sample:" , , 100)**

**pMean = InputBox("New sheet: The mean of your sample:" , , 10)**

**pSD = InputBox("New sheet: The SD of your sample:" , , 0.2)**

**Set oWS = Worksheets.Add(, ActiveSheet)**

**Range(Cells(1, 1), Cells(iSize, 1)).Formula = "=NORMINV(RAND(), " & pMean & " , " & pSD & ")"**

**Range(Cells(1, 1), Cells(iSize, 1)).Formula = Range(Cells(1, 1), Cells(iSize, 1)).Value**

**Range("C1").Formula = "=MIN(A:A)"**

 $Range("C2")$ . Formula =  $"=MAX(A:A)"$ 

**Range(Cells(4, 3), Cells(3 + iBins, 3)).Formula =**

**"=\$C\$1+(ROW(A1))\*(ROUND((\$C\$2-\$C\$1)/(" & iBins & "),4))"**

**Range(Cells(4, 4), Cells(3 + iBins,**

```
4)).FormulaArray = "=FREQUENCY(A:A,
" &
Range(Cells(4, 3), Cells(3 + iBins, 3)).Address & ")"
  Range("E1") =
WorksheetFunction.Average(Columns(1))
  Range("E2") =
WorksheetFunction.StDev(Columns(1))
  Range(Cells(4, 5), Cells(3 + iBins,
5)).FormulaR1C1 =
"=NORMDIST(RC[-2],R1C5,R2C5,FALSE)"
  Range("C4:E18").Select
  oWS.Shapes.AddChart2(240,
xlXYScatterLines).Select
  With ActiveChart
    .SetSourceData Range("C4:E18")
    .HasTitle = False
    .FullSeriesCollection(1).ChartType =
xlColumnClustered
    .FullSeriesCollection(2).ChartType = xlArea
    .FullSeriesCollection(2).AxisGroup = 2
```
ActiveChart.Axes(xlCategory).TickLabels.NumberForm **= "#,##0.00" End With Cells(1, 1).Select End Sub**

### **Chapter 14: Distribution Simulations What the simulation does**



This macro simulates 3 types of distributions: Normal, LogNormal, or Binomial.

#### **What you need to know**



A *Select Case* statement in VBA lets us regulate specifics for each case (ND, LN, or BI).

```
Sub Simulation()
  Dim sChoice As String, n As Long, pOne As
Double, pTwo As Double, i As Long
  Dim arr() As Variant, sFormula As String, oRange
As Range, oWS As Worksheet
  Dim pMin As Double, pMax As Double, oChart As
Chart
  sChoice = InputBox("ND (normal), LN
(lognormal), BI (binomial)"
, ,
"ND")
  n = InputBox("How many numbers?"
, , 100000)
  If n > 1000000 Then MsgBox "The max is
1000000": Exit Sub
  Set oWS = Worksheets.Add(, ActiveSheet)
  Select Case UCase(sChoice)
    Case "ND":
       pOne = InputBox("What is the mean?"
, , 50)
       pTwo = InputBox("What is the standard
deviation?"
, , 5)
       sFormula = "=NORM.INV(RAND(),
" & pOne
& "
,
" & pTwo & ")"
    Case "LN":
       pOne = InputBox("What is the mean?"
, , 2)
       pTwo = InputBox("What is the standard
deviation?"
, , 0.5)
       sFormula = "=LOGNORM.INV(RAND(),
" &
```
**pOne & " , " & pTwo & ")" Case "BI": pOne = InputBox("What is the probability?" , , 0.5) pTwo = InputBox("How many trials?" , , 50) sFormula = "=BINOM.INV(" & pTwo & " , " & pOne & " ,RAND())" Case Else: MsgBox "Not a valid option": Exit Sub End Select Set oRange = Range(Cells(1, 1), Cells(n, 1)) oRange.Formula = sFormula : oRange.Formula = oRange.Value Cells(1, 4) = "Count" Cells(2, 3).Formula = "=MIN(A:A)-**  $MOD(MIN(A:A),10)$ " **:**  $pMin = Cells(2, 3)$ **Cells(11, 3).Formula = "=MAX(A:A)+10-**  $MOD(MAX(A:A),10)$ " :  $pMax = Cells(11, 3)$  $For i = 3$  To 10  $Cells(i, 3) = pMin + i * Round((pMax - pMin) /$ **10, 0) Next i Set oRange = Range(Cells(2, 4), Cells(12, 4)) oRange.FormulaArray = "=FREQUENCY(A:A, " & Range(Cells(2, 3), Cells(11, 3)).Address & ")" oRange.Cells.Borders.LineStyle = xlContinuous : Cells.EntireColumn.AutoFit**

**Cells(1, 6) = "Distribution": Cells(1, 7) = sChoice**

**Cells(2, 6) = "Sample Size": Cells(2, 7) = n :**

**Cells(3, 6) = "Mean": Cells(3, 7) = pOne**

**Cells(4, 6) = "SD": Cells(4, 7) = pTwo**

**Set oRange = oWS.Range(Cells(1, 3), Cells(11, 4))**

**Set oChart = Charts.Add**

**oChart.HasLegend = False: oChart.ChartType = xlLine**

**oChart.FullSeriesCollection(1).Smooth = True**

**oChart.SetSourceData oRange: oChart.PlotBy = xlColumns**

**oChart.Axes(xlCategory).HasMajorGridlines = True**

**oChart.Location xlLocationAsObject, oWS.Name Sheet1.ChartObjects(1).Left = 125:**

```
Sheet1.ChartObjects(1).Top = 250
```
**Sheet1.ChartObjects(1).Chart.HasTitle = False: Cells(1, 1).Select**

**End Sub**

# **Chapter 15: Discrete Distributions What the simulation does**



Let's pretend you are a persistent, but very systematic, gambler. You decide ahead of time how to spend your different kinds of banknotes, which is specified in range D1:E5. The first columns in the chart display these settings as well.

Then the macro lets the machine determine one hundred times, in column A, when and which kind of banknotes to use and in which order. This is a random process, but within the margins set in D1:E5. The results are shown in the second columns of the chart.

Although the process is random, it follows a discrete distribution which comes always very close to what you would expect.

#### **What you need to know**

For the Range E1:E5, the macro creates random percentages, which together should make for 100%. That requires some math manipulation. Then we need the function VLOOKUP to use these percentages to find the corresponding type of banknote.

However, VLOOKUP always searches *vertically*, from top to bottom,

in the *first* column of a table, and then finds a corresponding value in a column to the right, specified by a *number*. So we need a lookup column before D1:D5 in order to determine the type of banknote to use. Besides, VLOOKUP looks for the previous value in an *ascending* order, so it would find \$1 for all percentages between 0% and 60%, \$5 between 60% and 80%, and \$100 for percentages greater than or equal to 98%.

Therefore, we need cumulative totals in the first column (C), starting at 0%. The third column (E) is now redundant, but is still needed for the chart to the right in order to show the expected frequencies—versus the randomly generated frequencies.
**Option Explicit**

```
Sub Distribution()
  Dim i As Integer, arr() As Integer, n As Integer
  ReDim arr(4)
  n = WorksheetFunction.RandBetween(0, 60)
  \textbf{arr}(0) = \textbf{n} - (\textbf{n} \text{ Mod } 5)n = WorksheetFunction.RandBetween(0, 100 -
arr(0))
  \textbf{arr}(1) = \textbf{n} - (\textbf{n} \text{ Mod } 5)n = WorksheetFunction.RandBetween(0, 100 -
(arr(0) + arr(1))\text{arr}(2) = n - (n \text{ Mod } 5)n = WorksheetFunction.RandBetween(0, 100 -
(arr(0) + arr(1) + arr(2))\textbf{arr}(3) = \textbf{n} - (\textbf{n} \text{ Mod } 5)\arctan(4) = 100 - (\arctan(0) + \arctan(1) + \arctan(2) + \arctan(3))For i = 0 To 4
     Cells(i + 1, 5) = FormatPercent(arr(i) / 100, 0)
  Next i
  Range("C2:C5").Formula = "=SUM($E$1:E1)"
  Range("A1:A100").Formula =
"=VLOOKUP(RAND(),$C$1:$D$5,2)"
End Sub
```


## **Chapter 16: Peaks What the simulation does**



Here we are dealing with a population (in I) that is composed of two sub-populations (in D and G). As long as the two subpopulations have the same mean, even with different standard deviations, the entire population may look nicely symmetrical. But when the mean of one subpopulation changes, the symmetrical curve may easily lose its symmetry and may even become *bi-modal*. The macro simulates this by looping with a timer.

### **What you need to know**



We have a global variable again to stop the macro: *bStopMacro*. Stopping the macro is done with a *CommandButton* on the sheet: Developer | Design Mode | Insert | Command Button | View Code (don't forget to click the Design Mode button OFF when you are done). The VBA code behind the button is very simple. Most of the work is done in the *Module*.

The *UBound* function of an array returns the index of the last array element.

In a module:

**Option Explicit**

### **Dim bStopMacro As Boolean**

**'Place Commandbutton on the sheet to run the next Sub**

**Sub StopLooping() bStopMacro = True End Sub**

```
Sub Peaks() 'Ctr + Sh + P
  Dim vMeans As Variant, vSDs As Variant, i As
Integer, j As Integer, pTime As Double
  vMeans = Array(40, 50, 60, 70, 80, 90, 100)
  vSDs = Array(14, 16, 18, 20)
  For i = 0 To UBound(vMeans)
    Range("G2") = vMeans(i)
    For j = 0 To UBound(vSDs)
       Range("G3") = vSDs(j)
       pTime = Time + 1Do
         DoEvents
       Loop Until Timer > pTime
```
## **If bStopMacro Then bStopMacro = False: Exit**

**Sub**

**Next j**

**Next i**

**If MsgBox("Start again?" , vbYesNo) = vbYes Then Peaks End Sub**

On the sheet that has the commandButton1:

### **Option Explicit**

**Private Sub CommandButton1\_Click() StopLooping Cells(1, 1).Select End Sub**

## **Chapter 17: Confidence Margins What the simulation does**



This sheet is actually done with Excel functions and formulas as mentioned in the inserted comments. The function CONFIDENCE in Excel returns the confidence interval for a population mean, using a normal distribution. It works best for sample sizes over 32.

In this case we used a 2-tailed error level of 5% (2.5% for each tail), which equates to a 95% confidence level. This means we have a 95% confidence that the vales we found in this sample lie actually between the two values mentioned in the *Data Table* (which equates to the mean plus the confidence margin and the mean minus the confidence margin). Notice how confidence margins depend heavily on sample size and standard deviation.

The only thing VBA does on this sheet is following which cell the user clicks on inside the *Data Table*.

#### **What you need to know**

Instead of using a *Module*, the VBA code is on the sheet itself: *SelectionChange* (see the screen shot on the next page). This is a *Sub* that kicks in whenever the user selects another cell on that sheet.

Instead of using a regular *For*-loop, we used a *For-Each*-loop that scans every single cell in a range of cells. The *Boolean* variable *bFound* always starts as 0 (False) until it is set to 1 (True).

We also applied conditional formatting by adding a *FormatCondition* to the collection of *FormatConditions*, starting at 1. In this case we used a formula for this condition as shown in the VBA code which marks the correct range in columns J:Lwith a certain color.

Because adding to the *FormatConditions* keeps literally adding the same condition again and again, the macro deletes all conditions earlier in the code first.

**Option Explicit**

```
Private Sub Worksheet_SelectionChange(ByVal
Target As Range)
  Dim oRange As Range, sFormula As String,
pLower As Double, pUpper As Double
  Dim oCell As Range, bFound As Boolean
  For Each oCell In Range("B8:G16")
    If oCell = ActiveCell Then bFound = True: Exit
For
  Next oCell
  If bFound = False Then Exit Sub
  Set oRange = Range("J1:L21")
  oRange.FormatConditions.Delete
  pLower = Left(ActiveCell, 4)
  pUpper = Right(ActiveCell, 4)
  sFormula = "=and($L1>=" & pLower & "
,$L1<="
& pUpper & ")"
```
**oRange.FormatConditions.Add xlExpression, , sFormula**

**oRange.FormatConditions(1).Interior.Color = vbYellow End Sub**



# **Chapter 18: Sample Size and Confidence Interval**

### **What the simulation does**



This sheet has two macros. The first macro (see above) simply asks for input variables and calculates confidence intervals.

The second macro (see below) calculates how many cases you would need in your sample in order to reach a specific margin limit.

### **What you need to know**



The *WorksheetFunction T\_Inv\_2T* returns the t-value of the Student tdistribution as a function of the probability and the degrees of freedom. The degrees of freedom are the number of cases minus 1. The t-value works for all sample sizes, even under 32.

The Standard Error (SE) is the Standard Deviation (SD) divided by the SQRT of the number of cases. So the confidence margin is the Standard Error times the t-value.

The 2 nd macro uses Excel's *GoalSeek*tool that allows you to alter data in formulas to get a specific result that you want to reach by changing a specific value (here  $B2$ , in the  $2<sup>nd</sup>$  argument).

**Option Explicit**

**Sub ConfidenceIntervalI() Dim pValue As Double, iCases As Long, pSE As Double, pPerc As Double Dim pTInv As Double, pMin As Double, pMax As Double, pMargin As Double On Error Resume Next pValue = InputBox("Which value?" , , 5.5) iCases = InputBox("How many cases?" , , 30) pSE = InputBox("SD" , , 0.5) / Sqr(iCases) pPerc = InputBox("Confidence" , , 0.95) pTInv = WorksheetFunction.T\_Inv\_2T(1 - pPerc, iCases - 1) pMargin = pSE \* pTInv pMin = FormatNumber(pValue - pMargin, 3) pMax = FormatNumber(pValue + pMargin, 3) MsgBox pPerc \* 100 & "% confidence: " & vbCr & "between " & pMin & " and " & pMax End Sub**

**Sub SampleSize()**

**Dim pConf As Double, pGoal As Double, iRow As Integer, sAddr As String, sMsg As String**

**pConf = InputBox("Which confidence level?" , , 0.95)**

**iRow = WorksheetFunction.Match(0.95, Range("A7:A9"))**

**sAddr = Range("C7:C9").Cells(iRow, 1).Address pGoal = InputBox("Which limit do you want to reach?" , , 0.09)**

**Range(sAddr).GoalSeek pGoal, Range("B2")**

**sMsg = "To reach a confidence level of " & FormatPercent(pConf, 0) & vbCr**

 $sMsg = sMsg \& "and a limit of " \&$ 

**FormatNumber(pGoal, 3) & vbCr**

**sMsg = sMsg & "you would need a sample of at least " & FormatNumber(Range("B2"), 0) & " cases!"**

**MsgBox sMsg Range("B2") = 30 : Calculate End Sub**

## **Chapter 19: Random Repeats What the simulation does**



This time we are going to simulate several runs in order to check as to whether the normal distribution we tried to simulate earlier did come out the way we would expect.

In column B the macro simulates a series of 100 random numbers—not equally but *normally* distributed, with a mean of 100 and a SD of 10. In the range D2:F22, it simulates 20 repeats of this random number generation, with a *Data Table*, so we end up with  $20 \times 100 = 2,000$  trials (which is still a very modest number for statistical standards). As it turns out, the mean of means oscillates around 100 (cell E24) and the mean of SDs stays more or less around 10 (cell F24).

The top graph plots the mean values as found in 20 runs (E2:E22). Even the frequency distribution of all the means, calculated in range R12:T19, creates a rather *normal* distribution with a bell shape in the lower graph, although the number of cases is still very modest in statistical terms.

#### **What you need to know**

The 100 sequential numbers in column A were calculated by using the ROW function. This function returns the row number of the cell the function

happens to be in—so ROW() in A10 would return 10. If you provide a cell reference as an argument, it returns the row number of that specific cell reference—so ROW(B25) in cell A10 (or in cell B1) would always return 25.

The VBA code copies the first sheet to a new sheet, but mean and SD can be changed. It also asks whether you want to replace formulas with values. If you do, F9 will not recalculate anything, and the *Data Table* will no longer work.

The average line in the graph is based on cells D24:E25.

This time we decided to also add a so-called error-handler, in case something goes (unexpectedly) wrong. It works with *On Error GoTo [label]* at the beginning, and at the end, after *Exit Sub*, a label like "Trap" or so and a *MsgBox* that uses information from the *Err* object (see Appendix).

**Option Explicit**

**Sub NewSample()**

**Dim oWS As Worksheet, oRange As Range, oChart As ChartObject**

**Dim pMean As Double, pSD As Double**

**On Error GoTo Trap**

**pMean = InputBox("The new mean on a new sheet:" , , 50)**

**pSD = InputBox("The new SD:" , , 10)**

**Set oWS = ActiveSheet**

**oWS.Copy , Sheets(Sheets.Count)**

**Set oRange =**

**ActiveSheet.Range("A1").CurrentRegion.Offset(1, 0) oRange.Columns(2).Formula =**

**"=NORMINV(RAND(), " & pMean & " , " & pSD & ")"**

**If MsgBox("Keep formulas for F9?" , vbYesNo) = vbNo Then**

**oRange.Columns(2).Formula =**

**oRange.Columns(2).Value**

**End If**

**Range("B2").Comment.Text "A mean of " & pMean & " and SD of " & pSD & "."**

**Set oChart = ActiveSheet.ChartObjects("Chart 2") oChart.Chart.Axes(xlCategory).MinimumScale = Round(Range("S12"), 1)**

**oChart.Chart.Axes(xlCategory).MaximumScale = Round(Range("S19"), 1)**

**Range("A1").Select**

**Exit Sub**

**Trap:**

**MsgBox "There was an error: " & Err.Description End Sub**



## **Chapter 20: Flipping a Fair Coin? What the simulation does**



This simulation is about flipping a coin six times, calculating how often we hit six times "tails" (0), five times, and so on (column A). The most likely outcome is  $3x$  "heads" (X) and  $3x$  "tails" (0)—actually  $31\%$  of all cases (column F). The center curve in the graph is a "bell-shaped" curve that represents this situation. Going more to the left or to the right under the bellshaped curve, the chances decrease dramatically, but they will never become 0.000000000000.

Events with random outcomes have the property that no particular outcome is known in advance. However, in the aggregate, the outcomes occur with a specific frequency. When we flip a "fair" coin, we do not know how it will land, but if we flip the coin millions of times, we know that it will land heads up  $(X)$  very close to 50% of the time—unless...

Unless... the coin is not "fair" and has a "preference" for lower X percentages (columns C:E and the other curves in the graph). To determine whether a coin is fair or not, we would need to flip a coin millions of times. In this simulation we only simulated some 100 coin tosses. In the situation shown on the next page, we would probably declare the fair coin unfair (column U). It is clear we need many more flips for a reliable verdict.

### **What you need to know**

Place a copy of the sheet on a new sheet after  $(2<sup>nd</sup>$  argument) the last one in the collection of *Sheets* so far—that is, *Sheets(Sheets.Count)*.

In order to create a normal distribution for a binary situation—such as yes/no, correct/defect, heads/tails, success/failure—we need the function BINOMDIST (or BINOM.DIST). It returns a binomial distribution probability for problems with a fixed number of tests or trials, when the outcomes of any trial are either success or failure, when trials are independent, and when the probability of success is constant throughout the experiment.

The *Formula* property of a range requires a string, so the formula property is set with an equal sign  $(=)$  to a string that starts with a double quote, followed by another equal sign  $(=)$ , and ending with a double quote. If there is another string inside this string, we need two double quotes instead of one.

**Option Explicit**

**Sub Coins() Dim oWS As Worksheet Set oWS = ActiveSheet oWS.Copy , Sheets(Sheets.Count)**

Range("C2:G8,C11:F16,C18:F18,R2:U18,R20:U20").C **Range("A1").Select**

**MsgBox "The chances for X (head) if the coin is 20 to 50% fair:"**

**Range("C2:G8").Formula =**

```
"=BINOMDIST($B2,6,C$1,0)"
```
**MsgBox "Flip these coins 6 times randomly:"**

**Range("C11:F16").Formula = "=IF(RAND()**

```
<=C$10,
""X""
,
""0"")"
```
**MsgBox "Here are the chances of X for each coin:" Range("C18:F18").Formula =**

```
"=COUNTIF(C11:C16,
""X"")/6"
```
**MsgBox "Then we repeat these calculations 17 times:"**

**Range("R2:U2").Formula = "=C18" Range("Q2:U18").Table , Cells(100, 100) MsgBox "How often did we hit 50% chance of**

## **head vs. tail?" Range("R20:U20").Formula = "=COUNTIF(R2:R18,0.5)" End Sub**



## **Chapter 21: Simulation of Sick Cases What the simulation does**



If a certain percentage of people is sick in the population (column A), we can find out with a 95% confidence how many in a sample of 100 persons will be sick, either as a minimum (column B) or as a maximum (column C) based on that confidence level.

We can also calculate what the probability is of finding up to a certain number of sick cases (column G), given a certain sample size (B1).

We can vary the sample size (B1) as well as the number of sick cases (G1) by answering both InputBox questions. The confidence level can be manually adjusted on the sheet.

The macro simulates all of this on the sheet.

#### **What you need to know**

One of the functions we need in column G is BINOMDIST (or BINOM.DIST) again. As explained in the previous Chapter, it returns a binomial distribution probability for problems with a fixed number of tests or trials, when the outcomes of any trial are either success or failure, when trials are independent, and when the probability of success is constant throughout the experiment.

The other crucial function is BINOM.INV (which replaces

CRITBINOM in pre-2010 versions. It has 3 arguments: the number of trials, the probability of a success on each trial, and the criterion value (alpha).

The function IFERROR is also quite recent (ISERROR could be used in earlier versions, but is a bit mpore involved). If there is an error in a certain BINOMDIST calculation, it should display an empty string—which calls for four double quotes (a string inside a string).

## **Option Explicit**

```
Sub SickCases()
  Dim iSize As Integer, iSick As Integer
  iSize = InputBox("What is the sample size?"
, , 100)
  Range("B1") = iSize
  Range("B5:B15").Formula =
"=BINOM.INV($B$1,$A5,1-$B$2)"
  Range("C5:C15").Formula =
"=BINOM.INV($B$1,$A5,$B$2)"
  iSick = InputBox("How many sick cases?"
, , iSize /
4)
  Range("G1") = iSickRange("G5:G15").Formula = "=IFERROR(1-
BINOMDIST(G$1,$B$1,$F5,TRUE),
"""")"
  If MsgBox("Empty calculated cells?"
, vbYesNo) =
vbYes Then
    Range("B1") = ""
    Range("B5:B15") = ""
    Range("C5:C15") = ""
    Range("G1") = ""
    Range("G5:G15") = ""
  End If
End Sub
```


## **Chapter 22: Unbiased Sampling What the simulation does**



When taking samples, the problem is that some are more likely to be chosen than others—so we call them biased samples. Unbiased sampling requires some bias-proof techniques. Therefore, we need the unbiased verdict of mathematical tools.

In this simulation, we use four different techniques to select telephone area codes at random. Technique #1 assigns a random number, sorts by that number, and then takes the first or last *N* cases. Technique #2 selects *X*% of the area codes randomly. Technique #3 produces *N* cases randomly. Technique #4 "weighs" each area code (say, depending on population density) and then performs a *weighted* sampling of *N* cases.

The simulation scrolls through these four different techniques of unbiased sampling.

#### **What you need to know**

Case #1 sorts the random numbers after their formulas have been changed into values. The *Sort* method has many optional arguments. The 1 st argument specifies the first sort field, either as a range name (String) or Range object; it determines the values that need to be sorted. The 2<sup>nd</sup>

argument determines the sort order—by default *xlAscending*.

Case #4 may need some more explanation. In column K, we calculate the cumulative total of all previous weights. So area code 202 (in L5) is four times included in that total. In column O, we multiply the grand total (K24) with a random number between 0 and 1, and then we look up that value in range K4:L24 and determine its corresponding area code. In other words, the second area code, 202, can be found through the random numbers between  $>=1$  and  $\leq 5$ ; this amounts to 4 chances of being picked (4x more than the first area code, 201).

**Option Explicit**

```
Sub RandomSelect()
  Dim oRange As Range, iSize As Integer
  If MsgBox("Sort all areacodes randomly"
,
vbYesNo) = vbNo Then Exit Sub
  Range("B4:B270").Formula = "=RAND()"
  Range("B4:B270").Formula =
Range("B4:B270").Value
  Range("A4:B270").Sort Range("B4")
```

```
If MsgBox(Range("E3") & " sample from column
D?"
, vbYesNo) = vbNo Then Exit Sub
  Range("E4:E270").Formula = "=RAND()<$E$3"
  Range("E4:E270").Formula =
Range("E4:E270").Value
  Range("D4:E270").Sort Range("E4"),
xlDescending
```

```
If MsgBox("Random selection of " & Range("I3"),
vbYesNo) = vbNo Then Exit Sub
  Range("H4:H270").Formula = "=RAND()"
```

```
Range("H4:H270").Formula =
Range("H4:H270").Value
  iSize = Range("I3")
  Range(Range("I4"), Cells(3 + iSize, 9)).Formula =
"=INDEX($G$4:$G$270,RANK(H4,$H$4:$H$270))"
```

```
If MsgBox("Weighted sample of 10"
, vbYesNo) =
vbNo Then Exit Sub
  Range("P4:P13").Formula =
"=VLOOKUP($K$24*RAND(), $K$4:$L$24, 2)"
  Range("Q4:Q13").Formula =
"=VLOOKUP(P4,$L$4:$N$23,3,0)"
```
### **End Sub**



# **Chapter 23: Transforming a LogNormal Distribution**

**What the simulation does**



Column A holds 100 random values based on a lognormal distribution with a mean of 2 and a Standard Deviation of 0.5. Column B shows the probability of each value. In column G, the lognormally distributed values are transformed by taking their natural logarithm.

In columns D:E, we calculate the mean and SD plus their frequencies —first of the values in A, then for the transformed values in G. We also calculate if and how skewed they are.

It turns out that the transformed lognormal distribution comes close to a normal distribution.

### **What you need to know**

The function LOGNORM.INV allows us to create a series of values

that have a lognormal distribution: =LOGNORM.INV(RAND(),2,0.5).

In cell E3 (and E34) we use the SKEW function, but nested inside a TEXT function, so we can use a formatted result in the *MsgBox*: =TEXT(SKEW(A:A), "0.000"). Skewness characterizes the degree of asymmetry of a distribution around its mean.

In cell E4 (and E35) we use a thumb rule as to whether a distribution is significantly skewed or not. The formula is for E4 as follows:  $=IF(E3>$ (2\*SQRT(6/COUNT(A:A))),"Y","N")

**Option Explicit**

```
Sub TransformLogNormal()
  Dim oWS As Worksheet
  Set oWS = ActiveSheet
  oWS.Copy , Sheets(Sheets.Count)
  Range("A2:A101").Clear:
Range("B2:B101").Clear: Range("G2:G101").Clear
  If MsgBox("Create a random LogNormal
Distribution?"
, vbYesNo) = vbNo Then
    Application.DisplayAlerts = False
    Sheets(Sheets.Count).Delete
    Application.DisplayAlerts = True
    Exit Sub
  End If
  Range("A2:A101").Formula =
"=LOGNORM.INV(RAND(),2,0.5)"
  Range("B2:B101").Formula =
"=LOGNORM.DIST(A2,$E$1,$E$2,TRUE)"
  If MsgBox("Transform the data?"
, vbYesNo) =
vbNo Then Exit Sub
  Range("G2:G101").Formula = "=LN(A2)"
  MsgBox "Lognormal is " & IIf(Range("E4") =
```
**"Y" , "" , "not ") & \_**

## **"significantly skewed: " & Range("E3") & vbCr & "After transformation " & \_ IIf(Range("E35") = "Y" , "slightly " , "no longer ") & \_ "skewed: " & Range("E34") & ""**

**End Sub**



## **Chapter 24: Outlier Detection What the simulation does**



Outliers are defined as numeric values in any random data set that have an unusually high deviation from either the statistical mean or the median value. In other words, these numbers are relatively extreme. It requires sound statistics—not intuition—to locate them. A rather simple rule is that all values outside a range of three times the standard deviation around the mean could be considered outliers—provided they follow a normal distribution.

### **What you need to know**

In this simulation, however, we will use a more robust statistical detection of outliers by calculating the deviation for each number, expressed as a "modified Z-score," and testing it against a predefined threshold. Zscores stand for the amount of standard deviation relative to the statistical median (in D1). MAD (in D2) stands for Median Absolute Deviation. Any number in a data set with the absolute value of modified Z-scores exceeding 3.5 times MAD is considered an outlier.

#### Column D shows the outcome.

In the 1970's the famous statistician John Tukey decided to give the term outlier a more formal definition. He called any observation value an outlier if it is smaller than the first quartile (F1) minus 1.5 times the *IQR* (F3), or larger than the third quartile (F2) plus 1.5 times the *IQR*. The Inter-Quartile Range, *IQR*, is the width of the interval that contains the middle half of the data. Column F shows the outcome.

The graph to the right shows the observed values marked with a *square* shape if it is an outlier according to the first method, or with a *diamond* shape if it is an outlier according to the second method. Most of the time, the first method detects more outliers than the second one.
**Option Explicit**

```
Sub Outliers()
  Dim oWS As Worksheet
  Set oWS = ActiveSheet
  oWS.Copy , Sheets(Sheets.Count)
  Range("B5:B29").Formula =
"=NORMINV(RAND(),30,15)*(1-2*RAND())"
  Range("D5:D29").Formula = "=IF(ABS(D$1-B5)>
(3.5*D$2),
""outlier""
,
"""")"
  Range("F5:F29").Formula = "=IF(OR(B5>
($F$2+1.5*$F$3),B5<($F$1-
1.5*$F$3)),
""OUTLIER""
,
"""")"
  Range("D5:D29,F5:F29").FormatConditions.Add
xlExpression, ,
"=AND($D5=""outlier""
,$F5=""OUTLIER"")"
```
Range("D5:D29,F5:F29").FormatConditions(1).Interior **= vbYellow End Sub**



# **Chapter 25: Bootstrapping**

#### **What the simulation does**



When you have a series of values that are not normally distributed say, 30 values such as in column A—it is not so simple to calculate a mean, a median, a SD, or a margin. You need some kind of technique such as bootstrapping.

This sheet uses that technique by randomly selecting values from the sample in A. We do that, for instance, 15 times: first in column D, then in column E, and so on until column R. At the bottom of each column we calculate the average. Based on these averages, we are able to know what the statistical parameters are that we were looking for.

In the VBA code, we do all of this, not 15 times, but 1,000 times by storing the results of each drawing in an array, from which we calculate the bootstrapping results. Larger number of drawings are obviously less susceptible to random fluctuations. A *MsgBox* reports what the outcome is (see picture on the next page).

#### **What you need to know**

The Excel function INDEX is a more sophisticated version of VLOOKUP. It looks in a table at a certain row position and a certain column position. It uses this syntax: *INDEX(table, row#, col#).* Whereas VLOOKUP

works only with column numbers, INDEX also uses row numbers, which is very important when we want to look at a record that is located a certain number of rows above or below another record.

Each cell in D1:R30 has this: =INDEX(\$A\$1:\$A\$30,ROWS(\$A\$1:\$A\$30)\*RAND()+1) In cell U2 is the mean of means: =AVERAGE(D32:R32) In cell U3 is the number of samples: =COUNT(D32:R32) In cell U4 is the  $2.5\%$  cut off:  $=$ U3 $*0.025$ In cell U5 is the lower bound: =SMALL(\$D\$32:\$R\$32,ROUNDUP(\$U\$4,0)) In cell U6 is the upper bound: =LARGE(\$D\$32:\$R\$32,ROUNDUP(\$U\$4,0)):

**Option Explicit**

```
Sub BootStrap()
  Dim i As Long, r As Long, j As Long, oRange As
Range, sMsg As String
  Dim pValue As Double, pMean As Double, pSE As
Double, iCutOff As Integer, pMargin As Double
  Dim arrMeans() As Double, arrValues() As Double
  r = Range("A1").CurrentRegion.Rows.Count
  Set oRange = Range(Cells(1, 1), Cells(r, 1))
  ReDim arrMeans(1 To 1000)
  For j = 1 To 1000ReDim arrValues(1 To r)
    For i = 1 To rarrValues(i) =
WorksheetFunction.Index(oRange, r * Rnd() + 1)
    Next i
    arrMeans(j) =
WorksheetFunction.Average(arrValues)
  Next j
  iCutOff = WorksheetFunction.RoundUp(100 *
0.025, 0)
  pMean =
Format(WorksheetFunction.Average(arrMeans),
```
**"0.00")**

**pSE =**

**Format(WorksheetFunction.StDev\_S(arrMeans), "0.00")**

**pMargin = Format(pSE \***

**WorksheetFunction.T\_Inv\_2T(0.05, r - 1), "0.00")**

**sMsg = "Based on 1000 runs:" & vbCr**

**sMsg = sMsg & "Mean of the arrMeans: " & pMean & vbCr**

**sMsg = sMsg & "SE of the arrMeans: " & pSE & vbCr**

**sMsg = sMsg & "Margin at 95%: " & pMargin & vbCr**

**sMsg = sMsg & "Lower Bound: " & pMean pMargin & vbCr**

**sMsg = sMsg & "Upper Bound: " & pMean + pMargin**

**MsgBox sMsg**

**End Sub**



## **Chapter 26: Bean Machine Simulation**

#### **What the simulation does**



The Galton board, also known as a quincunx or bean machine, is a device for statistical experiments named after English scientist Sir Francis Galton. It consists of an upright board with evenly spaced nails (or pegs) driven into its upper half, where the nails are arranged in staggered order, and a lower half divided into a number of evenly-spaced rectangular slots. The front of the device is covered with a glass cover to allow viewing of both nails and slots. In the middle of the upper edge, there is a funnel into which balls can be poured, where the diameter of the balls must be much smaller than the distance between the nails. The funnel is located precisely above the central nail of the second row so that each ball, if perfectly centered, would fall vertically and directly onto the uppermost point of this nail's surface.

Each time a ball hits one of the nails, it can bounce right or left. For symmetrically placed nails, balls will bounce left or right with equal

probability. This process therefore gives rise to a binomial distribution of in the heights of heaps of balls in the lower slots. If the number of balls is sufficiently large, then the distribution of the heights of the ball heaps will approximate a normal distribution.

#### **What you need to know**

This sheet simulates this process. All you have to do is keep holding the keys  $Ctrl + Shift + B$  down, and the slots will fill as to be expected. If you want to start all over, with an empty board, just hit the command button in the top right corner. In the beginning, the distribution may be not be very "normal" (see picture below), but that will soon change.

Place in a Module:

#### **Option Explicit**

```
Sub Beans()
  Dim oStart As Range, oPrev As Range, oNext As
Range, c As Integer, r As Integer
  Set oStart = Range("L1")
  oStart.Interior.ColorIndex = 15
  Set oPrev = oStart
  For r = 1 To 10
     If Rnd > 0.5 Then c = c + 1 Else c = c - 1Set oNext = oStart.Cells.Offset(r, c)
     \mathbf{a}Next = \mathbf{a}Next + 1
     oNext.Interior.ColorIndex = 15
     oPrev.Interior.ColorIndex = 0
     Set oPrev = oNext
  Next r
End Sub
```
Place on Sheet1:

#### **Option Explicit**

```
Private Sub CommandButton1_Click()
  Range("A1:X11").ClearContents
  Range("L1").Select
```
#### **End Sub**



## **Chapter 27: Correlated Distributions What the simulation does**



When you create multiple distributions, you may want to make this happen with a specific correlation coefficient between them. This simulation does so for you. In columns A:B, the macro creates two sets of normally distributed values in columns A and B. However, we want these two sets (X and Z) to be correlated as requested by cell E2. This simulation does so by using a transformation with the formula mentioned above. Then, in a *MsgBox*, it compares the old correlation coefficient with the new one.

#### **What you need to know**

When there are not 2 but 3 sets involved, you could hit Ctrl  $+$  Shift  $+$ D, which does the following. It performs the so-called Cholensky decomposition with a customized array function (see VBA-code), and then converts your three sets of values by using the array function results with another array formula like this: =MMULT(A2:C31,TRANSPOSE(F8:H10)). MMULT returns the matrix product of two arrays, with one of them transposed by using the TRANSPOSE function.

#### **What you need to do**

```
Sub Correlation()
  Dim oRange As Range
  Sheet2.Select
  Set oRange = Range("A2:C31"):
oRange.ClearContents
  MsgBox "First randomized values for X, Y, and Z"
  oRange.Formula =
"=ROUND(NORMINV(RAND(),10,2),2)"
  Set oRange = Range("F8:H10"):
oRange.ClearContents
  MsgBox "Now the Cholensky Decomposition in
F8:H10"
  oRange.FormulaArray = "=Cholenksy(F3:H5)"
'see function below
  Set oRange = Range("J2:L31"):
oRange.ClearContents
  MsgBox "Now the matrix manipulation in J2:L31"
  oRange.FormulaArray =
"=MMULT(A2:C31,TRANSPOSE(F8:H10))"
End Sub
Sub Decomposition()
  Dim oRange As Range
```

```
Sheet2.Select
```
**Set oRange = Range("A2:C31"):**

**oRange.ClearContents**

**MsgBox "First randomized values for X, Y, and Z" oRange.Formula =**

**"=ROUND(NORMINV(RAND(),10,2),2)"**

**Set oRange = Range("F8:H10"):**

**oRange.ClearContents**

**MsgBox "Now the Cholensky Decomposition in F8:H10"**

**oRange.FormulaArray = "=Cholenksy(F3:H5)" 'see function below**

```
Set oRange = Range("J2:L31"):
```
**oRange.ClearContents**

**MsgBox "Now the matrix manipulation in J2:L31" oRange.FormulaArray =**

```
"=MMULT(A2:C31,TRANSPOSE(F8:H10))"
End Sub
```
**Function Cholenksy(oMatrix As Range) 'partially borrowed from Kurt Verstegen**

**Dim i As Integer, j As Integer, k As Integer, N As Integer**

**Dim arrMatrix() As Double, arrLower() As Double, pValue As Double**

**N = oMatrix.Columns.Count**

**ReDim arrMatrix(1 To N, 1 To N) : ReDim**

```
arrLower(1 To N, 1 To N)
  For i = 1 To N
     For j = 1 To N
        arrMatrix(i, j) = oMatrix(i, j).Value :
\operatorname{arrLower}(i, j) = 0Next j
  Next i
  For i = 1 To N
     For j = 1 To N
        pValue = arrMatrix(i, j)
        For k = 1 To i - 1pValue = pValue - arrLower(i, k) *
arrLower(j, k)
        Next k
         <b>i = j 
           \text{arrLower}(i, i) = \text{Sqr}(pValue)ElseIf i < j Then
           \text{arrLower}(i, i) = \text{pValue} / \text{arrLower}(i, i)End If
     Next j
  Next i
  Cholenksy =
WorksheetFunction.Transpose(arrLower)
End Function
```
## **Chapter 28: Sorted Random Sampling**

#### **What the simulation does**



Sheet1 of this simulation takes random samples from values in column A—but without any duplicates, and in a sorted order, based on a specific lot size and sample size. It does so by sampling numbers in column A, then manipulates them in column B (see picture on the next page), and displays them orderly in E6:N15. Sheet2 does something similar, but this time with dates.

#### **What you need to know**



Sheet2 has an extra secret: two hidden rows before column C. The hidden columns A and B do the same work as they did on sheet1. In F18:O27 it finds the dates corresponding to F5:O14.

**Option Explicit**

**Sub Numbers() Dim iLot As Integer, iSample As Integer Sheet1.Select Range("A1:B100,E6:N15").ClearContents iLot = InputBox("Lot size (max of 100)" , , 25): If iLot > 100 Then Exit Sub iSample = InputBox("Sample size (max of 100)" , , 15): If iLot > 100 Then Exit Sub Range("G1") = iLot: Range("G2") = iSample Range("A1:A100").Formula = "=IF(ROW(A1)>\$G\$1, """" ,RAND())" Range("B1:B100").Formula = "=IF(A1="""" , """" ,IF(RANK(A1,\$A\$1:\$A\$101)>\$G\$2, Range("E6:N15").Formula = "=IF(\$D6+E\$16>\$G\$2, """" ,SMALL(\$B\$1:\$B\$100,\$D6+E\$16))" Do Calculate**

**Loop Until MsgBox("Again?" , vbYesNo) = vbNo End Sub**

**Sub Dates()**

**Dim iLot As Integer, iSample As Integer**

**Sheet2.Select**

**Range("A1:B100,F5:O14,F18:O27").ClearContents iLot = InputBox("Lot size (max of 100)" , , 25): If iLot > 100 Then Exit Sub iSample = InputBox("Sample size (max of 100)" , , 15): If iLot > 100 Then Exit Sub Range("G1") = iLot: Range("G2") = iSample Range("A1:A100").Formula = "=IF(ROW(A1)>\$G\$1, """" ,RAND())" Range("A1:A100").EntireColumn.Hidden = True Range("B1:B100").Formula = "=IF(A1="""" , """" ,IF(RANK(A1,\$A\$1:\$A\$100)>\$G\$2, Range("B1:B100").EntireColumn.Hidden = True Range("F5:O14").Formula = "=IF(\$E5+F\$15>\$G\$2, """" ,SMALL(\$B\$1:\$B\$100,\$E5+F\$15))" Range("F18:O27").Formula = "=IF(\$E5+F\$15>\$G\$2, """" ,SMALL(\$B\$1:\$B\$100,\$E5+F\$15))" Do Calculate**

**Loop Until MsgBox("Again?" , vbYesNo) = vbNo End Sub**



# **Chapter 29: Frequencies**

#### **What the simulation does**



There is not much new in this simulation. It asks for a specific mean and SD, loops for a specific amount of runs, creates a frequency table, and then replaces the chart with a new one.

#### **What you need to know**



**Option Explicit**

**Sub Frequencies() Dim pMean As Double, pSD As Double, pArr() As Double, i As Long ActiveSheet.Shapes(2).Delete pMean = InputBox("Mean" , , Cells(2, 1)) pSD = InputBox("SD" , , Cells(2, 2)) Cells(2, 1) = pMean: Cells(2, 2) = pSD Cells(5, 1) = pMean - 4 \* pSD Cells(6, 1) = pMean - 3 \* pSD Cells(7, 1) = pMean - 2 \* pSD Cells(8, 1) = pMean - 1 \* pSD Cells(9, 1) = pMean**  $Cells(10, 1) = pMean + 1 * pSD$ **Cells(11, 1) = pMean + 2 \* pSD**  $Cells(12, 1) = pMean + 3 * pSD$  $Cells(13, 1) = pMean + 4 * pSD$ **For i = 1 To InputBox("Runs" , , 10000) ReDim Preserve pArr(i) pArr(i) = WorksheetFunction.Norm\_Inv(Rnd, pMean, pSD) Next i pMean = WorksheetFunction.Average(pArr)**

```
pSD = WorksheetFunction.StDev_S(pArr)
  Range("B5:B13") =
WorksheetFunction.Frequency(pArr,
Range("$A$5:$A$13"))
  Range("A5:B13").Select
  ActiveSheet.Shapes.AddChart2(240,
xlXYScatterSmooth).Select
  ActiveChart.SetSourceData Range("A5:B13"):
ActiveChart.HasTitle = False
  Range("A1").Select
  MsgBox "After " & i - 1 & " runs:" & vbCr &
"Mean = " & _
         FormatNumber(pMean, 3) & vbCr & "SD
= " & FormatNumber(pSD, 3)
End Sub
```
# **III. MONTE CARLO SIMULATIONS Chapter 30: The Law of Large Numbers**

**What the simulation does**



This is an example of a Monte Carlo simulation. Why are they called *Monte Carlo* simulations? The name came up in the 1940s when Los Alamos physicists John von Neumann, Stanislaw Ulam, and Nicholas Metropolis were working on nuclear weapon research during the Manhattan Project in the Los Alamos National Laboratory. They were unable to solve their problems using conventional, deterministic mathematical methods. Then one of them, Stanisław Ulam, had the idea of using random simulations based on random numbers. The Monte Carlo simulations required for the Manhattan Project were severely limited by the computational tools at the time. Nowadays we have Excel!

Currently, the technique is used by professionals in such widely disparate fields as finance, project management, energy, manufacturing, engineering, research and development, insurance, and transportation. Monte Carlo simulation furnishes you as a decision-maker with a range of possible outcomes and the probabilities they will occur for any choice of action. Always run at least 1,000 iterations of Monte Carlo models to reduce the

risk of random impact.

#### **What you need to know**

This simulation shows the effect of large numbers. Column A contains "only" 1,000 numbers (plotted in the chart lower left). Then we run the results of those 1,000 numbers 10 more times in a *Data Table*, which makes for 10,000 cases (plotted in the chart top right). Finally we let VBA loop through these results some 100 times, and average them again. Row 15 keeps track of how many runs have not been executed yet. The outcome of these 1,000,000 runs in total is plotted in the third chart (lower right).

Notice how all three charts change during execution, but the third one stays rather stable.

Needless to say that this is a time consuming process—mostly because of cell manipulation on the sheet, for the use of arrays in VBA is comparatively fast. When all the runs are completed (probably after some 60 seconds), a *MsgBox* shows the time needed for completion, which depends partly on the processing speed of your machine.

**Option Explicit**

```
Sub Repeating()
  Dim i As Integer, vArr As Variant, arrTotals() As
Long
  Dim iRepeats As Integer, n As Integer, iTime As
Long
  iTime = Timer
  Range("G19:O19").ClearContents
  iRepeats = InputBox("How many repeats?"
, , 100)
  Cells(1, 1).Select
  ReDim arrTotals(1 To 9)
  For i = 1 To iRepeats
     ActiveSheet.Calculate
     vArr = Range("G13:O13")
     For n = 1 To UBound(vArr, 2)
       \text{arrTotals}(n) = \text{arrTotals}(n) + \text{Int}(\text{vArr}(1, n))Range("G19:O19").Cells(1, n) =
Int(arrTotals(n) / i)
       Range("G15") = iRepeats - i & " runs left"
    Next n
  Next i
  Range("F18") = iRepeats & "x10,000 runs:"
  MsgBox iRepeats & "x10,000 runs took " &
```
# Int(Timer - iTime) & " seconds."<br>End Sub



## **Chapter 31: Brownian Motion What the simulation does**



Brownian motion was discovered in the early 1800s by botanist Robert Brown, who noticed under his microscope how grains of pollen appeared to constantly and randomly move in a jittery way on the surface of the water. In his 1905 paper, Albert Einstein hypothesized that Brownian motion was caused by actual atoms and molecules hitting the grains of pollen, impelling them to take a "random walk" on the surface of the liquid. Einstein's work eventually led to the inherently probabilistic nature of quantum mechanics.

This is a simulation of how a grain of pollen—or a molecule, for that matter—takes a "random walk" on the surface of the water.

Dealing with the uncertain and the unknown is the realm of probability, which helps us to put a meaningful numerical value on things we do not know. Although a single random event is not predictable, the aggregate behavior of random events is.

#### **What you need to know**

Column B displays random X-changes and column C displays random Y-changes. In D and E, we start at coordinates 0,0 and keep adding the random changes from the previous columns. In P:Q we repeat each run 14

times and stop the macro as soon as we ended up close to 0,0 again.

The VBA code creates this random path, but keeps checking when the end point is the same as the starting point  $(0,0)$ —that is when the random walk took us back very close to where we started (within a range of 0.02). When that happens, it stops the process and reports how many runs that took.

The center chart only reflects the first run (to the left), so it only shows when that run ended where it started. See the chart below.

We also used *FormatConditions* again, but only once, for otherwise the macro keeps adding the same condition.

**Option Explicit**

```
Sub Returning()
  Dim i As Integer, oRange As Range, bBack As
Boolean, n As Long
  Range("O3:Q32").Table , Range("N1")
  Range("A1").Select
  Set oRange = Range("P3:Q32")
  'oRange.FormatConditions.Add xlExpression, ,
"=AND(AND($P3>=0,$P3<0.05),AND($Q3>=0,$Q3<0.0
  'oRange.FormatConditions(1).Interior.Color =
vbYellow
  Do While bBack = False
    Calculate
    For i = 1 To 30
       If oRange.Cells(i, 1) > -0.03 And
oRange.Cells(i, 1) < 0.03 Then
         If oRange.Cells(i, 2) > -0.03 And
oRange.Cells(i, 2) < 0.03 Then bBack = True: Exit Do
       End If
    Next i
    n = n + 1Loop
  MsgBox "Back to 0 at the " & i & "th run after "
```
#### & n & " repeats of 30 runs." **End Sub**



## **Chapter 32: Ehrenfest Urn What the simulation does**



Consider two urns A and B. Urn A contains N marbles and urn B contains none. The marbles are labelled 1,2,...N. At each step of the algorithm, a number between 1 and N is chosen randomly, with all values having equal probability. The marble corresponding to that value is moved to the opposite urn. Hence the first step of the algorithm will always involve moving a marble from A to B.

What will the two urns look like after k steps? If k is sufficiently large, we may expect the urns to have equal populations, as the probabilities of drawing a marble from A or from B become increasingly similar. States in which one urn has many more marbles than the other may be said to be unstable, as there is an overwhelming tendency to move marbles to the urn that contains fewer. This phenomenon is called the "Ehrenfest Urn."

Ehrenfest sometimes used the image of two dogs; the one with fleas gradually infects the other one. In the long-time run, the mean number of fleas on both dogs converges to the equilibrium value.

#### **What you need to know**

Instead of using two urns, we use a "board" that has X 's at all positions. Each time, at a random row and column position (cells B11 and B12), an X is replaced by an O, or vice-versa. Gradually, we reach an equilibrium where the number of X's and O's have become very similar, albeit with some oscillations of course.

The VBA code finds a random row and column position to replace an X with an O or reversed. It counts the number of X's and Y's after each change and places that number sequentially in row  $J$  (for  $X$ 's) and in row  $K$ for O's. These two columns gradually feed the progressing curves in the chart.

One macro feeds the board; the other macro resets the board.

**Option Explicit**

**Dim i As Integer 'global variable**

```
Sub Equilibrium()
  Dim oRange As Range, iRow As Long, iCol As
Integer
  Set oRange = Range("A1").CurrentRegion
  With oRange
    iRow = WorksheetFunction.RandBetween(1, 8)
    iCol = WorksheetFunction.RandBetween(1, 8)
    If .Cells(iRow, iCol) = "X" Then .Cells(iRow,
iCol) = "O" Else .Cells(iRow, iCol) = "X"
    Range("J1").Offset(i) =
WorksheetFunction.CountIf(oRange,
"X")
    Range("K1").Offset(i) =
WorksheetFunction.CountIf(oRange,
"O")
    i = i + 1End With
  Do While i < 200
    Equilibrium
  Loop
End Sub
```
#### **Sub Reset() Dim oRange As Range Set oRange = Range("A1").CurrentRegion oRange.Cells = "X" Columns(10).Clear Columns(11).Clear**  $\mathbf{i} = \mathbf{0}$ **End Sub**



### **Chapter 33: Random Walk What the simulation does**



This simulation uses a *random-walk* approach, similar to Brownian motion. Imagine we are leaving home (position 0). Iif we flip a coin and get heads, we go one block north (position  $+1$ ); if we flip tails, we go one block south (position -1). We keep doing this many times and then check how far we end up being from home. (We may also ask what the probability is that we return to where we started—believe it or not, that probability is 100% if the walk is long enough!).

First we will simulate 50 steps for columns B and C, plotted in the top graph. In the *Data Table* to the right, we repeated all 50 steps 14 times. The columns O and P of the *Data Table* are plotted in the bottom graph.

As it turns out, we could make big "gains" and drift far away from where we started. But not always! If this random-walk were interpreted as a case of gambling, we could encounter many negative, perhaps even huge negative outcomes—"losses" in gambling terms. Random walks are just fascinating.
### **What you need to know**

We do use *FormatConditions* again, but not in the macro, for that would create the same condition over and over again.

In addition, we use the Excel function COUNTIFS (missing in pre-2007), which allows for multiple count criteria: a zero in column B as well as a zero in column C.

In Range N3:N22, we use a formula with a nested NA function. This function returns #N/A. The advantage of doing so is that a curve in the chart does not display #N/A, but just "skips" it.

At the end, the macro can call itself again if so desired.

## **Option Explicit**

```
Sub Walking()
  Dim oRange As Range, i As Integer, sBack As
String, sEndScores As String
  Set oRange = Range("B3:C52")
  With oRange
    .Columns(1).ClearContents
    .Columns(2).ClearContents
    .Columns(1).FormulaR1C1 = "=IF(RAND()
<0.5,R[-1]C-1,R[-1]C+1)"
    .Columns(2).FormulaR1C1 = "=IF(RAND()
<0.5,R[-1]C-1,R[-1]C+1)"
' .FormatConditions.Add xlExpression, ,
"=AND($B3=0,$C3=0)"
' .FormatConditions(1).Interior.Color = vbYellow
  End With
  Range("N3:N21").Formula =
"=IF(AND(O3=0,P3=0),0,NA())"
  Set oRange = Range("O2:P21")
' oRange.FormatConditions.Add xlExpression, ,
"=AND($O2=0,$P2=0)"
' oRange.FormatConditions(2).Interior.Color =
vbYellow
```
**sBack = WorksheetFunction.CountIfs(Range("B3:B52"), 0, Range("C3:C52"), 0) & \_**

**"x back to a position of 0,0 during 1st run"**

**sEndScores =**

**WorksheetFunction.CountIfs(Range("O2:O21"), 0, Range("P2:P21"), 0) & \_**

**"x back to start position 0,0 in 20 runs"**

**If MsgBox(sBack & vbCr & sEndScores & vbCr & "Try again?" , vbYesNo) = vbYes Then Walking End Sub**



# **Chapter 34: A Data Table with Memory**



# **What the simulation does**

In column A, we randomly choose 1,000 times 0's or 1's, with a chance for 1 's based on an *InputBox* (say, 10%, shown in cell C1). The number of 1's is calculated in cell D1, but also for other percentages. This is done by using a *Data Table*. Based on this calculation, the Data Table in columns E and F runs all of this again for the next 9 percentages. When the percentage in C1 has been chosen to be 15%, column C shows the next 9 percentages from 16% to 24%.

A *MsgBox* displays the lowest and highest value. After the first run, these two values are the same, but when you keep running the macro, the difference between the two will begin to rise.

Doing this in Excel with formulas is hard to do, because that requires self-reference, and thus leads to circular reference. This can only be done with iterations ON. VBA can solve this easily.

### **What you need to know**



To prevent the screen from flashing during operations, we can use *Application*.*ScreenUpdating*. If you set this to False, make sure you set it later back to True.

We use four *Variant* arrays, because they can hold an array or series of values, including the values found in a range of cells. However, this creates a *two*-dimensional array, starting at element 1 (not 0 this time). So in order to address one of its elements, we need *two* indexes, one for each dimension (e.g. *array(1,1)*).



VBA can let you see what is in the array

by doing the following: View | Locals Window (see picture to the left). Place a *BreakPoint* in the code after the line you want to check by clicking in the gray margin to the left of it; this creates a brown line. Then click inside the *Sub* and hit the *Run* button; the yellow line indicates where the code has come to a halt. Now the *Locals Window* shows the values of all your variables, including the arrays. Click the *BreakPoint* off, so the code no longer stops there.

**Option Explicit**

```
Sub Memorize()
```
**Dim oRange As Range, i As Integer, pPercent As Double, sMsg As String**

**Dim arrTable As Variant, arrMin As Variant,**

**arrMax As Variant, arrPerc As Variant**

```
Range("F2:G10").ClearContents
```

```
pPercent = InputBox("The chance for 1's is:"
, ,
0.1)
```

```
If pPercent > 1 Then MsgBox "Must be between 0
and 1": Exit Sub
```
**Again:**

```
Application.ScreenUpdating = False
```

```
Range("A1:A1000").Formula = "=IF(RAND()<="
```

```
& pPercent & "
,1,0)"
```
**Range("C1") = FormatPercent(pPercent, 2)**  $For i = 1, To 9$ 

**Range("C2:C10").Cells(i, 1) = pPercent + i / 100 Next i**

```
Range("D1").Formula = "=COUNTIF(A:A,1)"
```

```
Set oRange = Range("C1:D10")
```

```
oRange.Table , Range("C1")
```

```
Calculate
```

```
arrPerc = Range("C2:C10")
  arrTable = Range("D2:D10")
  If IsEmpty(arrMin) Then
    arrMin = Range("D2:D10")
    arrMax = Range("D2:D10")
  Else
    For i = 1, To 9If arrTable(i, 1) < arrMin(i, 1) Then arrMin(i,
1) = arrTable(i, 1)
       If \arctan(A) h \arctan(A) \arctan(A) Then \arctan(A)1) = arrTable(i, 1)
    Next i
  End If
  sMsg = "Percent" & vbTab & "Min" & vbTab &
"Max" & vbCr
  For i = 1, To 9sMsg = sMsg \& \ar{r}Per(i, 1) \& \text{v}bTab \& \text{...}arrMin(i, 1) & vbTab & arrMax(i, 1) & vbCr
  Next i
  Application.ScreenUpdating = True
  MsgBox sMsg
  If MsgBox("Keep running?"
, vbYesNo) = vbYes
Then GoTo Again
End Sub
```
# **Chapter 35: Juror Selection in Court What the simulation does**



Countries with a juror system in court have to face the fact that they must choose 2x12 jurors from a larger pool of candidates after checking each candidate for certain criteria.

We assume we need 24 jurors (cell E1) from a pool of 100 (cell B1). We also use the following criteria: #1 they have no opinion yet whether the defendant is guilty (column B); #2 they were not witness to the crime (column C); #3 they accept the possibility of the death penalty (column D). These criteria have a probability in the population as shown in range B4:D4. Column E decides whether all three conditions have been met. Cell F4 counts how many in the pool of candidates actually qualified to be a juror in the case.

Finally we run this setup with a *Data Table* repeated 10 times (G:H, I:J, up to Y:Z); each one running pool sizes from 100 to 1000. We average these results in column AC, and we mark pool sizes that meet the needed number of candidates (F2) with Conditional Formatting.

### **What you need to know**

All gray cells have a formula in it. This is done by selecting all cells and implementing Condition Formatting based on this formula:  $=$ ISFORMULA $(A1)$ .

In the run shown below, a pool of 100 or 150 candidates would not be enough to reach the 24 jurors needed, given the three conditions in B:D and their probabilities. But 200 would! Again, we are dealing with probabilities here, so results may vary!



**Option Explicit**

**Sub Jurors() Dim iCand As Integer, iNeeded As Integer, i As Integer, oRange As Range Application.ScreenUpdating = False Range("H4,J4, L4, N4, P4, R4, T4,V4,X4,Z4,AC4").EntireColumn.ClearContents Set oRange = Range("A5:E1005") oRange.ClearContents Range("H5:H23").ClearContents Application.ScreenUpdating = True Range("B1") = InputBox("How many candidates?" , , 100) Range("E1") = InputBox("How many jurors needed?" , , 24) With oRange .Columns(1).Formula = "=IF(ROW(A1) <=\$B\$1,TEXT(ROW(A1), ""Juror 0""), """")" .Columns(2).Formula = "=IF(ROW(A1) <=\$B\$1,IF(RAND()<B\$4, ""+"" , """"), """")"**  $\cdot$ **Columns(3).Formula** =  $"=\text{IF}(\text{ROW}(B1))$ **<=\$B\$1,IF(RAND()<C\$4, ""+"" , """"), """")"**  $\cdot$ **Columns(4).Formula** =  $"=\text{IF}(\text{ROW}(C1))$ 

```
<=$B$1,IF(RAND()<D$4,
""+""
,
""""),
"""")"
    .Columns(5).Formula =
"=IF(COUNTIF(B5:D5,
""+"")=3,1,0)"
  End With
  Application.ScreenUpdating = False
  Range("H4,J4, L4, N4, P4, R4,
T4,V4,X4,Z4").Formula = "=SUM($E$5:$E$1005)"
  With Range("G4:R23")
    For i = 2 To 20 Step 2
       .Range(Cells(1, i - 1), Cells(20, i)).Table ,
Range("B1")
       'to prevent each table from recalculating,
replace with values:
       .Range(Cells(1, i - 1), Cells(20, i)).Formula =
.Range(Cells(1, i - 1), Cells(20, i)).Value
    Next i
  End With
  Range("AC5:AC23").Formula =
"=INT(AVERAGE(H5,J5,L5,N5,P5,R5,U5,T5,V5,X5,Z5))"
  Application.ScreenUpdating = True
End Sub
```
# **Chapter 36: Running Project Costs What the simulation does**



This Monte Carlo simulation deals with risks we encounter when we have project costs that we anticipate to be between a maximum value and a minimum value for several sub-projects or various products.

Based on 10,500 runs the simulation starts a new sheet and narrows down our risks with a 95% confidence to be between a certain upper- and lowerbound. As usual, results may vary since there is randomness involved. But a Monte Carlo simulation can reduce this risk.

Manually changing maximum and minimum costs in rows 2 and 3 should affect the outcome.

### **What you need to know**



The number of runs (J6) is determined by the values in the cells above it:  $((1.96/(margin/mean))$  ^ 2) \*  $((SD/mean)$  ^ 2)

The mean  $(J1)$  is:  $=AVERAGE(G2:G3)$ .

The Standard Deviation (J2) is: =STDEVP(G2:G3,J1). The Margin  $(J3)$  is:  $=$ J $1/300$ .

The Z or t value for 95% confidence is approximately 1.96.

**Option Explicit**

**Sub ProjectCosts() Dim i As Integer, iRuns As Long Dim oWS As Worksheet, oRange As Range, oCell As Range iRuns = Range("J6") 'Formula: ((1.96/(margin/mean)) ^ 2) \* ((SD/mean) ^ 2) ActiveSheet.Copy , Sheets(Sheets.Count) Application.Calculation = xlCalculationManual Set oRange = Range(Range("B9"), Range("B9").Cells(iRuns, 5)) oRange.Formula = "=RAND()\*(B\$2-B\$3)+B\$3" Set oRange = Range(Range("G9"), Range("G9").Cells(iRuns, 1)) oRange.Formula = "=SUM(B9:F9)" Range("B5:G5").FormulaR1C1 = "=average(R[4]C:R[" & iRuns + 3 & "]C)" Range("A5") = "average" Range("B6:G6").FormulaR1C1 = "=R[-1]C + 1.96\* stdev(R[3]C:R[" & iRuns + 2 & "]C)" Range("A6") = "upper bound" Range("B7:G7").FormulaR1C1 = "=R[-2]C - 1.96\* stdev(R[2]C:R[" & iRuns + 1 & "]C)"**

**Range("A7") = "lower bound" Application.Calculation = xlCalculationAutomatic Cells.EntireColumn.AutoFit MsgBox "Based on " & iRuns & " iterations" Range("B5:G7").Formula = Range("B5:G7").Value If MsgBox("Delete the calculations that were generated?" , vbYesNo) = vbYes Then Range(Range("B9"), Range("B9").Cells(iRuns, 6)).ClearContents End If End Sub**

# **Chapter 37: Forecasting Profits What the simulation does**



Let's say we are trying to the figure out the optimal amount of production needed in order to maximize our profits. If the demand for this product is regulated by a range of probabilities, then we can determine our optimal production by simulating demand within that range of probabilities and calculating profit for each level of demand.

The simulation uses three tables to set up this calculation. The table top right (E:F) sets up the assumed probabilities of various demand levels. The table top left (A:B) calculates the profit for one trial production quantity. Cell B1 contains the trial production quantity. Cell B2 has a random number. In cell B3, we simulate demand for this product with the function VLOOKUP.

The third table, on the lower left, is a *Data Table* which simulates each possible production quantity (20,000, 30,000, to 70,000) some 1,000 times and calculates profits for each trial number (1 to 1,000) and each production quantity (10,000, etc.).

Finally, row 13 calculates the mean profit for the six different production quantities. In this example, the figures show that a production of 40,000 units results in maximum profits.

The VLOOKUP function in B3 matches the value in B1 with the closest previous match in the first column of table D2:E5; column D has cumulative totals.

In cell A18 starts a *Data Table*. A18 has a link to the profit in B11. Then it uses cell B1 (20,000) for the row input, and an empty cell (say, H12) for the column input.

### **What you need to know**

The VBA code creates each time a new sheet and plots range A13:H16 six times (after recalculation) on this new sheet. At the bottom of the new sheet, it calculates the average for the upper and lower bounds. These averages are essentially based on 6x1,000 runs. A real Monte Carlo simulation would need more iterations, of course.

Setting the *CutCopyMode* fo False is usually wise after a copy operation—otherwise the copied area remains highlighted.

**Sub Profit() Dim oData As Worksheet, oWS As Worksheet, oRange As Range, i As Integer Sheet1.Activate Set oData = ActiveSheet Set oWS = Worksheets.Add(, Sheets(Sheets.Count)) For i = 1 To 30 Step 5 oData.Calculate Set oRange = oData.Range("A13:J16") oRange.Copy oWS.Cells(i, 1).PasteSpecial xlPasteValues Next i Application.CutCopyMode = False Range("B31:G31").Formula = "=AVERAGE(B3,B8,B13,B18,B23,B28)" Range("B32:G32").Formula = "=AVERAGE(B4,B9,B14,B19,B24,B29)" oWS.Cells.NumberFormat = "\$#,##0.00": oWS.Columns(1).NumberFormat = "0" oWS.Cells.EntireColumn.AutoFit oWS.Cells(1, 1).Activate End Sub**



# **Chapter 38: Uncertainty in Sales What the simulation does**



As said before, Monte Carlo simulations are computerized mathematical techniques that allow people to account for risks in quantitative analysis and decision making.

In this case, the decision-maker supplies sales data and probabilities (the shaded cells in columns A and B).

Based on this information, the macro simulates some 10,000 distributions with a range of possible outcomes (center section) and with the probabilities they will occur for any choice of action (right section).

At the end, a *MsgBox* reports for every new trial what the average sales are for each consecutive loop.The results are pretty close to each other.

#### **What you need to know**

The situation is basically simple. The major functions we need to achieve such kinds of predictions in this case are RAND, VLOOKUP, COUNT, and COUNTIF. Again we use 1,000 simulations in the center section (F:I) to reach more reliable predictions.



**Option Explicit**

```
Sub SalesSimulation()
  Dim oRange As Range, oTable As Range, i As
Long, n As Long, sMsg As String
  Set oRange = Range("F4").CurrentRegion
  With oRange
    Set oTable = .Offset(2, 0).Resize(.Rows.Count -
2, .Columns.Count)
  End With
  oTable.ClearContents
  n = InputBox("How many runs (1,000 to
100,000)?"
, , 10000)
  Set oTable = Range(Cells(3, 6), Cells(n, 9))
'oTable.Offset(0, 0).Resize(n, Columns.Count)
  oTable.Columns(1).Formula =
"=VLOOKUP(RAND(),$C$3:$D$5,2)"
  oTable.Columns(2).Formula =
"=VLOOKUP(RAND(),$C$10:$D$13,2)"
  oTable.Columns(3).Formula =
"=VLOOKUP(RAND(),$C$18:$D$20,2)"
  oTable.Columns(4).Formula = "=F3*G3*H3"
  Do
    Application.Calculate
```
 $i = i + 1$ 

**sMsg = sMsg & "Loop" & i & " (" & n & " times): average="**

**sMsg = sMsg & FormatCurrency(Range("Q2"), 0) & vbCr**

**MsgBox sMsg**

**Loop Until MsgBox("Run again?" , vbYesNo) = vbNo End Sub**



# **Chapter 39: Exchange Rate Fluctuations**

**What the simulation does**



The profit of a certain company depends on a fluctuating exchange rate between the American and Australian dollar—or any other foreign currency. The average profit we predict in cell B14 is based on a fixed exchange rate (B5). But in reality this rate has normally distributed fluctuations with a Standard Deviation shown in cell B6. So we need to simulate such variations.

This simulation is done by using a *Data Table* combined with repeated calculations in arrays operating in the background. First the user is asked how many rows the *Data Table* should have—by default 1,000. The *Data Table* shows what the profits would be for different exchange rates.

The *MsgBox* displays what the average profit would be, plus the 25 percentile and 75-percentile profit values. Then the user has a chance to run the *Data Table* repeatedly. The results of each run are added to the *MsgBox*. When the user decides to stop any further runs, the average and two percentile values are calculated from all these runs. So the end result in the above picture is based on 10 x 1,000 normally distributed calculations.

## **What you need to know**



An essential part of this simulation

is the first column of the *Data Table* (column D). It holds this formula: =NORMINV(RAND(),0.92,0.02)—or whatever the fixed numeric values should be. In the macro we change these random settings from formulas to values, so those numbers don't keep changing while the *Data Table* makes its calculations.

The column input cell of the *Data Table* is the exchange rate value in cell B5.

You also should know that we need variables of the *Double* type for mathematical calculations, but if we want to format them as currency, we need variables of the *String* type as well.

The three arrays we use must be "redimensioned" for a new element each time we run the loop. This is done with a *ReDim* statement, but make sure you include also the *Preserve* keyword, otherwise the array loses its previous contents.

# **Option Explicit**

```
Sub ExchangeRates()
  Dim oRange As Range, iRuns As Long, i As Long,
sMsg As String
  Dim arrAvg() As Double, arr25() As Double,
arr75() As Double
  Dim pAvg As Double, p25 As Double, p75 As
Double 'for the currencies
  Dim sAvg As String, s25 As String, s75 As String
'for the formatted currencies
  Range("D1").CurrentRegion.Offset(1,
0).ClearContents
  iRuns = InputBox("How many runs?"
, , 1000)
  Range("E2").Formula = "=B5"
  Range("F2").Formula = "=B14"
  Set oRange = Range(Range("D2"),
Range("F2").Cells(iRuns, 1))
  oRange.Table , Range("B5")
  sMsg = "Runs" & vbTab & "25%" & vbTab &
vbTab & "Average" & vbTab & vbTab & "75%" &
vbCr
  Do
```

```
oRange.Columns(1).Formula =
```
**"=NORMINV(RAND(),\$B\$5,\$B\$6)"**

**oRange.Columns(1).Formula =**

**oRange.Columns(1).Value**

**ReDim Preserve arrAvg(i): ReDim Preserve arr25(i): ReDim Preserve arr75(i)**

```
arrAvg(i) =
```
**WorksheetFunction.Average(oRange.Columns(3)) arr25(i) =**

**WorksheetFunction.Percentile(oRange.Columns(3), 0.25)**

**arr75(i) =**

**WorksheetFunction.Percentile(oRange.Columns(3), 0.75)**

**sAvg = FormatCurrency(arrAvg(i), 0)**

**s25 = FormatCurrency(arr25(i), 0)**

**s75 = FormatCurrency(arr75(i), 0)**

**sMsg = sMsg & i + 1 & vbTab & s25 & vbTab & sAvg & vbTab & s75 & vbCr**

 $i = i + 1$ 

```
Loop Until MsgBox(sMsg & "Run again?"
,
```
 $v b YesNo) = v b No$ 

**pAvg = WorksheetFunction.Average(arrAvg): sAvg = FormatCurrency(pAvg, 0)**

**p25 = WorksheetFunction.Percentile(arr25, 0.25): s25 = FormatCurrency(p25, 0)**

**p75 = WorksheetFunction.Percentile(arr75, 0.75): s75 = FormatCurrency(p75, 0)**

**sMsg = sMsg & vbCr & "mean:" & vbTab & s25 & vbTab & sAvg & vbTab & s75 MsgBox sMsg End Sub**

# **IV. GENETICS Chapter 40: Shuffling Chromosomes What the simulation does**



This simulation shows what the probability is that an individual still has chromosomes derived from one particular grandparent. Since we have 23 pairs of chromosomes, on average we have 11 or 12 chromosomes that were handed down to us from one particular grandparent, two generations ago—actually a 16% chance (row 13 and 14). But the outcome can vary between 0 chromosomes or the entire set of 23 chromosomes—but these extremes are very unlikely. Genetics, the science of inheritance of traits and characteristics, is modeled probabilistically.

As an aside, the situation is much more complicated. One problem is that chromosomes do not remain identical during the formation of reproductive cells, but they can exchange parts between the two of a pair which is called crossing-over or recombination. In this simulation, we stay clear of that issue.

#### **What you need to know**

We will also use the new function BINOM.INV in this simulation. There is no pre-2010 version of this function, so if you use a file with this function in 2007, you will get an error message. In Excel 2007, an alternative would be CRITBINOM.

Cells B2:B25 hold this formula:  $=$ BINOMDIST(A2,23,0.5,0)/100. BINOMDIST needs to know the number of "successes" (running from 0 to 23 in column A), out of 23 trials (23 chromosomes), with a 50% probability of "success" in each trial, and with a non-cumulative setting in our case. Make sure to divide by 100.

**Option Explicit**

```
Sub Chromosomes()
  Dim pArr() As Double, i As Long, n As Long, sMsg
As String
```
**Dim pAvg As Double, pMin As Double, pMax As Double, pCount As Long**

```
sMsg = sMsg & "run" & vbTab & "min" & vbTab
& "avg" & vbTab & "max" & vbCr
  Do
    For i = 0 To 100000ReDim Preserve pArr(i)
      pArr(i) = WorksheetFunction.Binom_Inv(23,
0.5, Rnd)
    Next i
    n = n + 1pAvg =FormatNumber(WorksheetFunction.Average(pArr),
2)
    pMin = WorksheetFunction.Min(pArr)
    pMax = WorksheetFunction.Max(pArr)
    pCount = UBound(pArr)
    sMsg = sMsg & n & vbTab & pMin & vbTab &
pAvg & vbTab & pMax & vbCr
```
# **Loop Until MsgBox(sMsg, vbOKCancel) = vbCancel End Sub**



# **Chapter 41: Sex Determination What the simulation does**



This sheet simulates what happens when a father (XY) and a mother (XX) have one descendant, who has in turn another descendant, and so forth. It is something like a family tree.

If the descendant is a female (XX), that cell gets marked with a color. If the descendant still has the original Y-chromosome  $(Y^*)$  from the (greatgreat-grand-) father, that chromosome is marked with an asterix (\*). In the figure above, there happen to be seven female descendants, and the ancestral Y-chromosome got already "lost" by mere chance in the first generation.

The macro asks the user first how many generations they want to simulate (the maximum is set to 10). The macro keeps asking that question by calling itself again, and it does so until the user hits the *Cancel* button of the *Inputbox*. It is possible, by mere change, that the paternal X-chromosome persists for six generations (see picture below)—or even longer.

### **What you need to know**

One of the 23 pairs of chromosomes is called the sex-chromosome

pair. It either holds two similar chromosomes (XX) or two unalike chromosomes (XY; Y is actually a very short chromosome). The presence of the Y-chromosome determines maleness.

The father (XY) produces sperm cells with either an X-chromosome (50% chance) or a Y-chromosome (50% chance). If the egg cell—which has always one X-chromosome—is fertilized by a sperm cell with a Ychromosome, the descendant will be a male. So there is a 50% chance for either a male or a female descendant (in reality, there is a slight difference in chance, though).

## **Option Explicit**

```
Sub Sex()
  Dim r As Integer, c As Integer, sGens As String,
oCell As Range
  sGens = InputBox("How many generations
(<=10)?"
, , 10, 10000, 2000)
  If sGens = "" Then Exit Sub
  If CInt(sGens) > 10 Then MsgBox "Not more than
10": Exit Sub
  For Each oCell In Range("D3:O22")
    If oCell = "XX" Or oCell = "XY" Or oCell ="XY*" Then
       oCell.ClearContents:
oCell.Interior.ColorIndex = 0
    End If
 Next oCell
  c = 3For r = 3 To (2 * \text{CInt}(sGens) + 1) Step 2
    c = c + 1Cells(r, c) = IIf(Rnd > 0.5,
"XX"
, IIf(Cells(r - 2,
c - 1) = "XY*"
,
"XY*"
,
"XY"))
     Cells(r, c + 2) = IIf(Cells(r, c) = "XX", "XY",
"XX")
```
### If  $\text{Cells}(r, c) = "XX"$  Then

**Cells(r, c).Interior.Color = vbYellow Else**

 $Cells(r, c).$ Interior.ColorIndex = 0 **End If**

### **Next r**

**Call Sex 'the Sub calls itself again End Sub**


## **Chapter 42: Mendelian Laws What the simulation does**



Certain diseases, such as a particular form of dwarfism, are based on a *dominant* allele (say, *A*). Anyone who carries such an allele (*Aa*) is called a heterozygote and has the disease.

Other diseases, such as cystic fibrosis, are based on a *recessive* allele (say, *a*). Only people with two of those alleles (*aa*) show the disease and is called a homozygote. So someone can be a carrier (*Aa*) of the disease without showing its symptoms.

Then there are also diseases, such as a known form of hemophilia, that are called sex-linked because they are based on a recessive allele (say, *h*) located on the X-chromosome; such alleles come always to expression in males (XY)—because there is no second chromosome to counteract it—but in females (XX) only when both X-chromosomes have that recessive allele.

The simulation applies Mendelian laws each time for 10,000 cases. Because of such a large sample, the results come very close to what we would expect. Besides, the user can repeat these 10,000 runs again and again. There will be differences, but they fluctuate within a very narrow margin (see below). All of this is based on simple Mendelian rules.

#### **What you need to know**



This sheet simulates the chances for

passing on such an allele to the next generation. When the allele does come to expression, it is marked with conditional formatting. Because conditional formatting cannot distinguish between lowercase and uppercase characters —it's not case sensitive—we need to mark the capital with an apostrophe, or something like it.

The first case: Parents with *Aa* and *aa* have 50% *Aa* children and 50% *aa* children. The chance that a dominant allele (*A*) from such parents comes to expression in the next generation is 50%.

The second case: The offspring of parents who are both *Aa* is *AA* (25%), *Aa* (50%), and *aa* (25%). The chance that a recessive allele (*a*) comes to expression in the next generation is 25% (*aa*).

The third case: The offspring of a mother with *Hh* and a father with *H*would be *HH* (25%), *Hh* (25%), *H-* (25%), and *h-* (25%). The chance that a recessive, X-linked allele (*h*) comes to expression in the next generation is therefore 25% (*h-*).

**Option Explicit**

```
Sub Mendel()
  Dim arrDom() As Variant, arrRec() As Variant,
arrX() As Variant '3 arrays
  Dim iDom As Long, iRec As Long, iX As Long, i
As Long, n As Long, sMsg As String
  sMsg = "run" & vbTab & "Aa dom." & vbTab &
"aa rec." & vbTab & "X rec." & vbCr
Again:
  n = n + 1sMsg = sMsg & n & vbTab
  For i = 0 To 10000ReDim Preserve arrDom(i)
     arrDom(i) = IIf(Rnd < 0.5,
"'Aa"
,
"aa")
    If arrDom(i) = "'Aa" Then iDom = iDom + 1
  Next i
  sMsg = sMsg & FormatPercent(iDom / 10000, 2) &
vbTab
  For i = 0 To 10000
    ReDim Preserve arrRec(i)
     arrRec(i) = IIf(Rnd < 0.5,
"'AA"
, IIf(Rnd < 0.5,
"Aa"
,
"'aa"))
    If arrRec(i) = "'aa" Then iRec = iRec + 1
```
**Next i**

**sMsg = sMsg & FormatPercent(iRec / 10000, 2) & vbTab**

```
For i = 0 To 10000
```
**ReDim Preserve arrX(i)**

**arrX(i) = IIf(Rnd < 0.25, "HH" , IIf(Rnd < 0.33, "H'h" , IIf(Rnd < 0.5, "H-" , "'h-")))**

```
If arrX(i) = "'h-" Then iX = iX + 1
```
**Next i**

**sMsg = sMsg & FormatPercent(iX / 10000, 2) & vbCr**

```
If MsgBox(sMsg, vbOKCancel,
"Each run
10000x'') = v\textrm{bOK} Then
    i Dom = 0: iRec = 0: iX = 0
    GoTo Again
  End If
End Sub
```
## **Chapter 43: The Hardy-Weinberg Law**

### **What the simulation does**



A gene can carry various alleles. Let us assume there are only two alleles, *A* and *a*. People who have two of the same alleles are homozygotes (*AA* or *aa*). Those who carry both alleles are heterozygotes (*Aa*). Let us take the example of an allele for albinism (*a*), which is recessive, so albinos must be *aa*, whereas individuals with the genotypes *AA* and *Aa* are not albinos. If we know the percentage  $(q^2)$  of albinos  $(aa)$ , we can calculate the frequency *q* of allele *a*, as well as the frequency *p* of allele *A—*provided there are no other alleles—since *p=1-q*.

As a consequence, the frequency would be *p*<sup>2</sup> for the homozygotes *AA* (cell D4), *q*<sup>2</sup> for the homozygotes *aa* (cell D2), and *2pq* for the heterozygotes (in cell D3: *pq* for *Aa* and *qp* for *aA*). So if we know that *aa* has a frequency of 10%, we can deduce what the frequencies are for *Aa* and *AA* (see the comments in those cells shown in the figure above).

#### **What you need to know**



The Hardy-Weinberg law states that if these genotypes would *randomly* mate, the frequencies would stay the same in the next generations. We are going to simulate this with a macro. We know, based on Mendelian laws, what the offspring would be of certain pairs of parents (see H1:L10). The macro is going to randomly make these combinations and randomly determine what their offspring would be. The result, based on 10,000 runs, is displayed in a *MsgBox*. Notice how the frequencies in the next generation are extremely close to the frequencies of the parent generation—which is exactly what the Hardy-Weinberg law states.

The VLOOKUP function plays an important role in this simulation. It finds randomly the genotype of each parent and then finds randomly (with a random number between 2 and 5) the child's genotype in one of the  $2<sup>nd</sup>$  to  $5<sup>th</sup>$ columns of range H:L.

If we change the frequency of *aa* to 40%, the next generation will more or less keep that frequency because of random mating. Obviously, the total of the frequencies should be 100%

**Option Explicit**

```
Sub HardyWeinberg()
  Dim arrMales() As String, arrFemales() As String,
arrChildren() As String
  Dim iHomDom As Long, iHetero As Long,
iHomRec As Long
  Dim i As Long, pRec As Double, iRnd As Integer,
sMsg As String, iCount As Long
  pRec = InputBox("Frequency of aa"
, , 0.1)
  Range("D2") = pRec
  ReDim arrMales(0 To 10000)
  ReDim arrFemales(0 To 10000)
  ReDim arrChildren(0 To 10000)
  For i = 0 To 10000arrMales(i) =
WorksheetFunction.VLookup(Rnd, Range("B2:C4"),
2, 1)
    arrFemales(i) =
WorksheetFunction.VLookup(Rnd, Range("B2:C4"),
```
**2, 1)**

**iRnd = WorksheetFunction.RandBetween(2, 5) arrChildren(i) =**

**WorksheetFunction.VLookup(arrMales(i) &**

**arrFemales(i), Range("H2:L10"), iRnd, False)**

```
If arrChildren(i) = "A'A'" Then iHomDom =
iHomDom + 1
```
**If arrChildren(i) = "A'a" Then iHetero = iHetero + 1**

```
If arrChildren(i) = "aa" Then iHomRec =
iHomRec + 1
```
**Next i**

```
iCount = UBound(arrChildren)
```

```
sMsg = "After " & iCount & " generations:" &
vbCr
```
**sMsg = sMsg & "aa: " & FormatPercent(iHomRec / iCount, 1) & vbCr**

**sMsg = sMsg & "A'a: " & FormatPercent(iHetero / iCount, 1) & vbCr**

**sMsg = sMsg & "A'A': " &**

```
FormatPercent(iHomDom / iCount, 1)
```
**MsgBox sMsg**

**End Sub**

## **Chapter 44: Genetic Drift What the simulation does**



The Hardy-Weinberg law (see Chapter 44) states that allele frequencies remain the same over the next generations. Even in case of a recessive allele, it will not entirely disappear. However, by random chance, the percentage of alleles may, and usually does, change in the next generations. This is called "genetic drift." The effect increases when the population size decreases—the so-called "founder effect."

The macro simulates the effect of genetic drift during 50 generations assuming that the frequencies randomly fluctuate by a certain percentage. The macro asks the users which "drift factor" they want to apply (by default 2% for each generation). During this ongoing process, recessive homozygotes (*aa*) may eventually, by mere chance, disappear from stage, to the advantage of the dominant homozygotes (*AA*). This happened in the picture above.

The macro does part of its work by temporarily using the range D8:D108, which it deletes later. It is through this range that curves can be plotted in a chart. Because a chart cannot display anything after its source data are deleted, we change the chart into a picture before the macro deletes its source data.

#### **What you need to know**

If the frequency of allele *A* is 0.6 (= $p$ ), then the frequency of allele *a* must be  $1-0.6 = 0.4$  (=q)—assuming there are only two alleles for this gen. So the frequency of genotype *AA* would be *p*<sup>2</sup> and the frequency of genotype *aa* would be *q*2. The frequency of *Aa* and *aA* would then be *2pq*.

The VBA code also uses some form of so-called Error Handling (see Appendix). The simplest version of Error Handling is the following VBA line: *On Error Resume Next*. When some error occurs, this line skips over the line that caused the error, and executes the next line in the VBA code. That can easily be troubling, though. That's why it is better to use a more robust kind of Error Handling: *On Error GoTo [label]*. The label is something you chose (in our case: *ErrTrap*). Place that label at the end after *Exit Sub* but before *End Sub*. Usually after the label, we place a line that is based on the *Err* object, which deals with the latest error. One option is: *MsgBox Err.Description*, which tells the user what the actual error was. It is always wise to have some kind of Error Handling in every macro you create. (I skipped this part for most macros in this book.)

**Option Explicit**

```
Sub Drifting()
  Dim pDrift As Double, i As Long, oRange As
Range, oChart As Chart, oShape As Shape
  On Error GoTo ErrTrap
  pDrift = InputBox("Drift factor"
, , 0.02)
  Set oRange = Range("A8:A108")
  oRange.Formula = "=ROW(A1)-1"
  Range("B7") = "AA"
  Range("B8").Formula = "=C3"
  Range("C7") = "Aa"
  Range("C8").Formula = "=C4+D3"
  Range("D7") = "aa"
  Range("D8").Formula = "=D4"
  Set oRange = Range("B9:B108")
  oRange.Formula = "=NORMINV(RAND(),B8,
" &
pDrift & ")"
  Set oRange = Range("C9"
,
"C108")
  oRange.Formula = "=IFERROR(2*SQRT(B9)*(1-
SQRT(B9)),NA())"
  Set oRange = Range("D9:D108")
  oRange.Formula = "=IFERROR((1-
SQRT(B9))^2,NA())"
```
**Set oRange = Range("B7").CurrentRegion Set oChart = Charts.Add oChart.SetSourceData oRange oChart.ChartType = xlXYScatterLinesNoMarkers Sheets(1).Select ActiveChart.ChartArea.Copy Sheets(2).Select ActiveSheet.PasteSpecial Format:="Picture (JPEG)" Selection.ShapeRange.ScaleWidth 0.8, msoFalse Selection.ShapeRange.ScaleHeight 0.8, msoFalse Selection.ShapeRange.IncrementLeft 100 Selection.ShapeRange.IncrementTop 100 Application.DisplayAlerts = False Sheets(1).Delete oRange.Clear Application.DisplayAlerts = True Exit Sub ErrTrap: Err.Clear End Sub**

## **Chapter 45: Two Selective Forces What the simulation does**



It is rather common that both alleles have a selection factor working against them; let's designate those two factors with the symbols *s* and *t*. The most well-known case is sickle-cell anemia. Because there is strong selection pressure (*s*) against the homozygote (*aa*), who suffers from anemia, we would expect allele *a* to disappear from the population. However, in malaria areas it has a rather stable frequency (*q*). The explanation is that there is also a selection pressure (*t*) against the other homozygote (*AA*), who is more vulnerable to malaria than the other individuals, especially the heterozygotes (*Aa*).

Our simulation loops through six different settings for the selective factors *s* and *t*, shown in range A4:F27. The first two settings come close to the situation for sickle-cell anemia; the first one is shown in the figure above, where we see the frequencies of the heterozygotes increase at the cost of both types of homozygotes.

#### **What you need to know**



The columns J:N calculate frequencies for 33 generations (from row 2 to row 35). See the formulas here above. The columns D:F derive their information from the calculations in these columns (J:N).

## **Option Explicit**

```
Sub Selecting()
  Dim i As Integer, n As Integer, oRange As Range, j
As Integer
  Set oRange = Range("D4:F27")
  For i = 1 To 24
    If i Mod 4 \leq 1 Then oRange.Range(Cells(i, 1),
Cells(i, 4)).ClearContents
  Next i
  MsgBox "This starts looping through 6 settings for
t and s."
  For i = 4 To 24 Step 4
    Range("E1") = Cells(i, 2)
    Range("E2") = Cells(i, 3)
    For n = 1 To 3
       Set oRange = Range(Cells(i + n, 4), Cells(i + 4))n, 6))
       oRange.FormulaArray = "=INDEX(L2:N34,
"
& Cells(i + n, 1) & "
,0)"
       oRange.NumberFormat = "0.00%"
       oRange.Formula = oRange.Value
    Next n
    If MsgBox("Factor t is " & Range("E1") & "
```
## **factor s is " & \_ Range("E2"), vbOKCancel) = vbCancel Then Exit Sub Next i End Sub**



## **Chapter 46: Differential Fitness What the simulation does**



This simulation is similar to the previous one. Again, we assign relative fitness factors—for instance, genotype AS (fitness factor 1 in cell M4) is more "fit" than genotype SS (fitness factor 0.4 in cell). So gradually, up to a certain point, the frequency of AS will increase, while the frequency of genotype SS (sickle cell anemia, for instance) will decrease in future generations.

All the gray cells on the sheet have formulas in it. We assume that each combination of parents has up to 4 children each generation (columns F:I). Most formulas are identical to the ones used in Chapter 45. The main difference is that the range P2:S10 is based on the different fitness factors for each genotype. The offspring is not only determined by Mendel's laws but also by the fitness of that specific genotype. That's why certain cells remain empty in P2:S10.

This will obviously affect frequencies in the next generation. The simulation calculates the average frequencies of the three genotypes based on 10,000 couples with each couple having up to 4 children. The simulation calculates the results for the next generation and compares them with the original frequencies in the  $1<sup>st</sup>$  generation of the parents. It is to be expected that there is a change of frequencies—but again, not always, for there is still randomness involved. Sometimes, the effect is quite dramatic (see the picture below).



#### **What you need to know**

Only the gray cells on the sheet have formulas in it; the rest is manual input. To mark the cells with formulas in them, conditional formatting can be a helpful tool. Select all the cells and then use conditional formatting with the following formula: =ISFORMULA(A1). The function ISFORMULA came available in more recent versions of Excel.

### **Option Explicit**

**Sub Fitness() Dim arrParents() As String, arrChild() As String, i As Long, sMsg As String Dim pFreqAA As Double, pFreqAS As Double, pFreqSS As Double Dim pAA As Double, pAS As Double, pSS As Double, iCount As Long, iBlank As Long pFreqSS = Range("D2") pFreqAA = Range("D3") pFreqAS = Range("D4") sMsg = "Frequencies for" & vbTab & "SS" & vbTab & "AA" & vbTab & "AS" & vbCr sMsg = sMsg & "1st generation: " & vbTab & FormatPercent(pFreqSS, 0) & vbTab & FormatPercent(pFreqAA, 0) & vbTab & FormatPercent(pFreqAS, 0) & vbCr Range("P2:S10") = "" Range("P2:S10").Formula = "=IF(RAND() <VLOOKUP(G2,\$L\$2:\$M\$4,2,0),G2, """")"**  $For i = 0$  To  $10000$ **ReDim Preserve arrParents(i) ReDim Preserve arrChild(i)**

**arrParents(i) =**

**WorksheetFunction.VLookup(Rnd, Range("B2:C4"), 2, 1) & WorksheetFunction.VLookup(Rnd,**

**Range("B2:C4"), 2, 1)**

**arrChild(i) =**

**IIf(WorksheetFunction.RandBetween(0, 6) > 1,**

**WorksheetFunction.VLookup(arrParents(i),**

```
Range("O2:S10"),
```
**WorksheetFunction.RandBetween(2, 5), False), "")**

**If**  $\text{arrChild}(i) = "AA"$  **Then**  $pAA = pAA + 1$ 

If  $\text{arrChild}(i) = "AS"$  Then  $pAS = pAS + 1$ 

If  $\text{arrChild}(i) = "SS"$  Then  $pSS = pSS + 1$ 

**If arrChild(i) = "" Then iBlank = iBlank + 1 Next i**

**iCount = UBound(arrChild) - iBlank**

 $sMsg = sMsg \& \text{``2nd generation:''} \& \text{vbTab} \& \text{``}$ **FormatPercent(pSS / iCount, 0) & vbTab & FormatPercent(pAA / iCount, 0) & vbTab & FormatPercent(pAS / iCount, 0) & vbCr**

```
'For more generations, Range("D2") needs to be
reset to (pSS/iCount)
```
**MsgBox sMsg End Sub**

## **Chapter 47: Molecular Clock What the simulation does**



Genes may undergo changes, called mutations. Mutations to nonessential portions of the DNA are useful for measuring time—the so-called molecular clock. It is assumed that such mutations occur with a uniform probability per unit of time in a particular portion of DNA, because they are not exposed to selection. If *P* is the percentage of *no*-mutations in a year, then *P*<sup>N</sup> is the probability of *no*-mutations over *N* years.

On average, given two individuals who had a common ancestor many generations ago, you would expect—assuming that mutations are so rare that it is very unlikely that a mutation in the same segment has occurred in two individuals—that the percentage of segments that are mutated in one or the other is, on average,  $2(1 - P<sup>N</sup>)$ . This is an estimate of the percentage of segments to be found different when comparing two individuals with a common ancestor *N* years ago.

This macro provides a simplified version of the technique that has been used to locate the first common ancestors of all human beings in evolution—the first female and the first male, so to speak. Non-essential DNA sections can be tested for single-nucleotide-polymorphisms (SNPs,

pronounced "snips"), which are single base pair changes in DNA that occur throughout the genome, including its "silent" DNA sections.

## **What you need to know**



Place in cell C6:  $=2*(1-C4\textdegree\textdegree C5)$ . This is the mutation percentage after a certain numbers of years this case 50,000 years as shown in cell C4).

Notice the following: If two individuals have a 10% difference, their most recent common ancestor lived 100,000 years ago if the mutation rate for those DNA segments is 0.9999995, but 250,000 years ago based on a rate of 0.9999998, or even 50,000 years ago based on a rate of 0.9999999. So small differences in mutation rate can have an enormous impact. Apparently, the accuracy of the molecular clock depends heavily on the accuracy of the mutation rate.

### **Option Explicit**

```
Sub Ancestry()
  Dim pTarget As Double, sTarget As String, pPerc
As Double, iStepYrs As Long
  Dim iUnchanged As Long, iYrs As Double, iRate
As Double, sMsg As String
  sTarget = InputBox("Percentage of DNA
difference?"
, ,
"10%")
  If \text{Right}(s \text{Target}, 1) \leq \frac{1000 \text{ N}}{1000 \text{ N}} Then s \text{Target} = s \text{Target}& "%"
  pTarget = Left(sTarget, Len(sTarget) - 1) / 100
  Range("F5") = sTarget 'OR:
FormatPercent(pTarget, 2)
  iStepYrs = Range("C5")
  iUnchanged = Range("C4") * 10000000
  sMsg = "For " & sTarget & " we found:" & vbCr
  For iYrs = iStepYrs To (iStepYrs + 10 * iStepYrs)Step iStepYrs
     For iRate = (iUnchanged - 8) To iUnchanged
       pPerc = 2 * (1 - (iRate / 10000000) ^ iYrs)
       If pPerc < (pTarget + 0.005) And pPerc >
(pTarget - 0.005) Then
          sMsg = sMsg & "Years ago: " & iYrs &
```
## **vbTab & "at rate: " & iRate / 10000000 & vbCr End If Next iRate Next iYrs If Len(sMsg) < 25 Then sMsg = sMsg & "No results" MsgBox sMsg End Sub**



## **Chapter 48: DNA Sequencing What the simulation does**





This is a very simple simulation of

what was done in the Human Genome Project. Today, "dideoxy sequencing" is the method of choice to sequence very long strands of DNA. DNA is composed of 4 different nucleotides—A, C, G, and T. The composition of a DNA string is randomly generated in column A. It is clear that this composition is not known yet until we use a technique in the middle section that we are going to describe soon. The end result is shown in the columns AQ and AR by using formulas on the sheet, but the macro also does this work in the background and then displays the outcome in a *MsgBox*.

### **What you need to know**

To determine the unknown sequence of nucleotides in a DNA section of interest, the double-stranded DNA is separated into single strands

(denaturation). In the next step, a new DNA strand is made, complementary to the template strand, by using the bacterial enzyme DNA polymerase. During this step, A-nucleotides will be "paired" withT-nucleotides, and Cnucleotides with G-nucleotides—they are called complementary.

Then follows a key step. In addition to the four regular single nucleotides, the reaction mixture also contains small amounts of four dideoxy-nucleotides which lack a group necessary for chain extension. Once in a while—by low chance, because of its much lower concentration—a dideoxy-nucleotide will be incorporated into the growing DNA strand instead of the regular nucleotide. This will prevent the DNA chain from growing further. Since each of these four special nucleotides is labeled with a different fluorescent dye, a certain type of laser can later detect them. We marked them with an asterix (\*) in our simulation.

So DNA chains end up being very short, very long, and of every possible length in between. The newly synthesized DNA strands are then passed through a laser beam that excites the fluorescent dye attached to the dideoxy-nucleotide at the end of each strand. This color is then detected by a photocell, which feeds the information to a computer. Finally, the computer does the rest of the work by piecing the short sequences together like a puzzle.

**Option Explicit**

**Sub Sequencing() Dim pNoLabel As Double, i As Integer, j As Integer, sMsg As String Dim arrDNA() As String, arrStrand() As String, sNucl As String, bFound As Boolean pNoLabel = InputBox("Choose % unlabeled between 0.85 and 0.95" , , 0.9) If pNoLabel > 0.95 Then Exit Sub Range("B1") = pNoLabel**  $sMsg = "With " & FormatPercent(1 - pNoLabel, 0)$ **& " labeled nucleotides:" & vbCr ReDim arrDNA(0 To 10)**  $For i = 0$  To 10 **arrDNA(i) =**  $WorksheetFunction.VLoop(WorksheetFunction.Ran)$ **4), Range("A2:B5"), 2, 0)**  $sMsg = sMsg \& \arrDNA(i) \& \text{vbfTab}$ **ReDim arrStrand(0 To 39)**  $For i = 0$  To 39 **arrStrand(j) = IIf(Rnd > Range("B1"), Left(WorksheetFunction.VLookup(arrDNA(i), Range("B2:C5"), 2, 0), 1), " ")**

```
If \text{arrStrand}(j) \ll  " " Then \text{sNucl} =arrStrand(j): bFound = True
    Next j
    sMsg = sMsg & Join(arrStrand) & vbTab
     sMsg = sMsg & IIf(bFound, sNucl,
"-") & "->"
& arrDNA(i) & vbCr
    sNucl = "": bFound = False
  Next i
  MsgBox sMsg
```
**End Sub**



## **V. SCIENCE**

# **Chapter 49: Matrix Elimination**

### **What the simulation does**



If you need to solve equations, it can be helpful to use *matrixes*. This file has a few examples of such equations. Let's focus on the last one: four equations with four unknown X-values. The equation uses four different coefficients for *a*, as shown in matrix *[A]* (C14:F17). These four equations should equate to the Y-values shown in matrix *[Y]* (H14:H17).

You need to determine what the four X-values must be to solve the equations. Here's what you do. 1. Invert matrix *[A]* by using the multi-cell array function MINVERSE. 2. Multiply the matrix *Inv[A]* with the matrix *[Y]* by using the array function MMULT. 3. You could have combined both steps by using a nested function instead: =MMULT(MINVERSE([*A*]),[*Y*]). 4. This creates vertical array results, so to plot them horizontally you need also the TRANSPOSE function.

So we end up with: =TRANSPOSE(MMULT(MINVERSE([*A*]),[*Y*]))). Thanks to this technique of matrix elimination, you can solve the equations and find the four X-values for  $a<sub>1</sub>$  through  $a<sub>4</sub>$  in the cells C18:F18. These four X-values make the four equations, based on the *a* values specified in the first matrix, equate to the Y-values specified in the second matrix. To test the outcome in a cell like J14, use this formula:

#### =C14\*\$C\$18+D14\*\$D\$18+E14\*\$E\$18+F14\*\$F\$18.



#### **What you need to know**

The VBA code applies all these formulas in the background, without using formulas on the sheet, but be aware that they are array functions, so we need the VBA property *FormulaArray*.

In addition we used a different type of *InputBox*: *Application*.*InputBox*. This kind of *InputBox* lets the user select manually and directly a certain range of cells by using the mouse. If you want the *InputBox* to return a range—instead of a range address or so—you must set its last argument to the number 8. You can also include a default range address for what the user had selected already.

**Option Explicit**

```
Sub MatrixElimination()
  Dim oMatrixA As Range, oMatrixY As Range,
oResults As Range, sMsg As String, i As Integer
  On Error GoTo ErrTrap 'Set
Tools|Options|General: Break on unhandled errors
  Set oMatrixA = Application.InputBox("Select
range of A-coefficients"
, ,
Range("C14:F17").Address, , , , , 8)
  Set oMatrixY = Application.InputBox("Select
corresponding range of Y's"
, ,
Range("H14:H17").Address, , , , , 8)
  Set oResults =
oMatrixA.Rows(oMatrixA.Rows.Count + 1)
  oResults.FormulaArray =
"=TRANSPOSE(MMULT(MINVERSE(" &
oMatrixA.Address & "),
" & _
                            oMatrixY.Address &
"))"
```
**sMsg = "Results for X-values:" & vbCr For i = 1 To oResults.Cells.Count sMsg = sMsg & "X" & i & ":" & vbTab & oResults.Cells(1, i) & vbCr**

### **Next i MsgBox sMsg Exit Sub**

## **ErrTrap:**

**MsgBox "There was an error: " & Err.Description**  $Err$ . Number =  $0$ 

## **End Sub**



## **Chapter 50: Integration with Simulation**

### **What the simulation does**



Instead of performing integration the mathematical way, you can also use a simulation. With a large number of runs, you can get very close to the analytic result found based on an integral. To do so, consider a circle inscribed within a square with sides of *s* units. The radius of the circle equates to *s*/2. Now, ten-thousand darts (F2) are randomly thrown at the diagram and then we count the number of darts that fall inside the circle (F3).

Although this is basically an integration problem that has an analytical solution, we can also simulate it with a Monte Carlo technique that gives us an approximation of the analytical integral. The advantage of using this example is that we can compare the simulation result (F4) with the analytical result (F5), telling us how close we came to the "real" solution.

### **What you need to know**

I won't explain this part, but the integral would be  $(-x^3 + 10x^2 +$ *5x)dx*. This formula is used in cell F5. The graph plots the analytic solution based on columns I and J. The curve is within a 10 by 200 rectangle.



The VBA code creates an array of  $X$ 's with a random number between 0 and 10, plus an array of Y's with a random number between 0 and 200 (so the curve is within a 10 by 200 rectangle). Then it checks in a  $3<sup>rd</sup>$  array whether the "dart" is inside or outside the circle by using the integral formula: *IIf(pY(i)* >  $-pX(i)$  ^ 3 + 10 \*  $pX(i)$  ^ 2 + 5 \*  $pX(i)$ , 0, 1). So 1 is "in,"  $0$  is "out."

The simulation does all of this 10,000 times—or whatever the user decides. After each trial, the macro shows the previous results and the new result in a *MsgBox*.

**Option Explicit**

```
Sub Integration()
  Dim i As Long, n As Long, pX() As Double, pY()
As Double, pInOut() As Integer
  Dim iCount As Long, iSimulArea As Long, sMsg
As String, iLoops As Integer
  n = InputBox("How many runs?"
, , 10000)
  Do
     For i = 0 To n - 1ReDim Preserve pX(i)
       pX(i) = Rnd * 10 '=RAND()*10
       ReDim Preserve pY(i)
       pY(i) = Rnd * 200
       ReDim Preserve pInOut(i)
       pInOut(i) = IIf(pY(i) > -pX(i) \land 3 + 10 \ast pX(i)
\hat{P} 2 + 5 \hat{P} pX(i), 0, 1)
    Next i
    Range("F2") = n
    iCount = WorksheetFunction.Sum(pInOut)
    Range("F3") = iCount
    iSimulArea = 2000 * iCount / n
     Range("F4") = iSimulArea
     MsgBox "Throws: " & n & vbCr & "in circle: "
```
**& iCount & vbCr & "simul.area: " & iSimulArea iLoops = iLoops + 1**

**sMsg = sMsg & "Loop " & iLoops & " area: " & vbTab & iSimulArea & vbCr**

**Loop Until MsgBox(sMsg & vbCr & "Keep looping?" , vbYesNo) = vbNo End Sub**


# **Chapter 51: Two Monte Carlo Integrations**

### **What the simulation does**



This time, we discuss only two equations as an example:  $Y=X$  (on the 1<sup>st</sup> sheet) and Y=X $\frac{1}{2}$  (on the 2<sup>nd</sup> sheet), and we do so without using any integration formula.

### **What you need to know**



VBA generates two arrays of random X-values and random Y-values. They are plotted in the left graph.Then another set of two arrays, according to the formulas shown in VBA. Those two are plotted in the right graph. In a 5<sup>th</sup> array, we assign 1's when the two previous columns have X- and Yvalues in it, so we can calculate the area under the curve. All of this is done 100,000 times.

```
Sub Integration()
  Dim pXmin As Double, pXmax As Double, pYmin
As Double, pYmax As Double
  Dim oWS As Worksheet, pX() As Double, pY() As
Double, i As Long, iCount As Long
  Dim pXif() As Double, pYif() As Double, pInOut()
As Double, pSum As Double
  If MsgBox("Do you want to be on Sheet1?"
,
vbYesNo) = vbYes Then
    Sheet1.Select
  Else
    Sheet2.Select
  End If
  iCount = InputBox("How many runs?"
, , 100000)
  Set oWS = ActiveSheet
  pXmin = Range("B4"): pXmax = Range("C4")
  pYmin = Range("B5"): pYmax = Range("C5")
  For i = 0 To (iCount - 1)ReDim Preserve pX(i)
    pX(i) = pXmin + (pXmax - pXmin) * RndReDim Preserve pY(i)
    pY(i) = pYmin + (pYmax - pYmin) * RndReDim Preserve pXif(i)
    If oWS.Name = Sheet1.Name Then
```

```
pXif(i) = \text{If}(pY(i) < pX(i), pX(i), 0)'=IF(C8<B8,B8,0)
    Else
       pXi(f(i)) = \text{Hf}(pY(i) < (pX(i) \land 2), pX(i), 0)'=IF(C8<B8,B8,0)
    End If
    ReDim Preserve pYif(i)
    pYif(i) = \text{If}(pXif(i) = 0, 0, pY(i))ReDim Preserve pInOut(i)
    pInOut(i) = If(pYif(i) = 0, 0, 1)pSum = pSum + pInOut(i)Next i
  Range("F4") = pSum
  Range("F5") = iCount
  Range("F1") = (pXmax - pXmin) * (pYmax -
pYmin)
  Range("F2") = Range("F1") * Range("F4") /
Range("F5")
  MsgBox "Arae under the curve: " &
FormatNumber(Range("F2"), 2)
End Sub
```
The 2<sup>nd</sup> sheet (Y=X^2) has a few differences with the 1<sup>st</sup> sheet (Y=X):



# **Chapter 52: Monte Carlo Approach of Pi**

**What the simulation does**



This simulation estimates what Pi is by using a custom (user-defined) function *PiEstimate*, which has one argument: the number of times you want to run this calculation. By default it runs two random numbers internally 10,000 times.

The function *PiEstimate* is used in a *Sub* called *PiSimulation* which places that function in three columns of 1,000 rows. And then it calculates the average of these 3,000 cells. Notice that the results in each of these cells can vary quite a bit, but their average in E1 is rather stable.

#### **What you need to know**

Because Excel has also a PI function, we can compare its value (cell A1) with the value we received through our simulation (E1). There are only very minor deviations, because of the large number of runs.

Notice that the custom function has *Application.Volatile* not enforced. What that line would do is recalculating the function each time something on the sheet changes. We don't want that here.



**Option Explicit**

```
Function PiEstimate(n As Long)
  Dim pRand As Double, pInside As Double, i As
Integer, pApprox As Double
  Dim XRand As Double, YRand As Double, RRand
As Double
  'Application.Volatile True 'recalculates whenever
anything changes on the sheet
  \bf{p}Inside = \bf{0}For i = 1 To n
    XRand = Rnd
    YRand = Rnd
    RRand = XRand \wedge 2 + YRand \wedge 2
    If (RRand \leq 1) Then
      pInside = <b>plnside + 1</b>End If
  Next i
  pApprox = 4 * pInside / n
  PiEstimate = pApprox
End Function
Sub PiSimulation()
  Dim i As Integer
```
**MsgBox "Be patient until the next MsgBox appears"**

```
Cells.EntireColumn.AutoFit
Cells.EntireColumn.NumberFormat = "0.00000"
Range("A1").Formula = "=Pi()"
```

```
For i = 1 To 6 Step 2
```

```
Range(Cells(5, i), Cells(1004, i)).Formula =
"=PiEstimate(10000)"
```
**Cells(3, i) =**

**WorksheetFunction.Average(Cells(5, i), Cells(1004, i))**

**Next i**

```
Range("E1").Formula = "=AVERAGE(A5:E1004)"
  MsgBox "Mean of 3x1,000 runs is " &
FormatNumber(Range("E1"), 5)
```
**End Sub**



## **Chapter 53: A Population Pyramid What the simulation does**



This simulation shows how a population pyramid may change over the course of 100 years. The simulation is based on several grossly oversimplified assumptions.

Assumption #1: The population starts at 100,000 (cell D11).

Assumption #2: The birth rate is partially randomized (row 12) and is based on participation by everyone over 20 years old.

Assumption #3: Every age group has a certain survival value (column B) which is subject to small fluctuations, determined by a randomize factor (*InputBox*, by default 2%).

With three InputBoxes you can determine your randomize factor (by default 0.02), the minimum birth rate (by default 0.1), and the maximum birth rate (by default 0.4). Then the macro loops through 100 years in steps of 10 and shows the situation after that number of years.

#### **What you need to know**

The cells B16:B25 use the function HLOOKUP, which searches for a value in the top row of a table or an array of values, and then returns a value in the same column from a row you specify in the table or array. It has the following syntax: HLOOKUP(value, table or array, row index number, exact

match or not). So the formula in B16 is: =HLOOKUP([Years],\$D\$1:\$N\$11,ROW(A2),0)., where ROW(A2), copied down, becomes ROW(A3), etc. So it finds the number of years horizontally in the first row of D1:N11, and then returns the  $2<sup>nd</sup>$  cell down,  $3<sup>rd</sup>$  cell, etc. For 100 years, B16:B25 should be the same as N2:N11.

The cells C16:C25 calculate how far each bar in the chart should be offset to the right, which is done with the formula: =(MAX(\$B\$16:\$B\$25)- B16)/2.

The chart is a stacked bar chart, and plots A2:A11 against B6:B25 and C6:C25.

**Option Explicit**

**Sub Pyramid()**

**Dim iYears As Integer, pSurvivalFluct As Double, pMinRate As Double, pMaxRate As Double**

**MsgBox "You can manually change survival rates in the cells B2:B11"**

```
pSurvivalFluct = InputBox("What is the
randomize factor?"
, , 0.02)
```

```
pMinRate = InputBox("Minimum birthrate"
, ,
0.1)
```
**pMaxRate = InputBox("Maximum birthrate" , , 0.4)**

**'iYears = InputBox("The situation after how many years?" , , 100)**

**Do**

```
Range("C2:C11").Formula =
```
**"=NORMINV(RAND(),B2, " & pSurvivalFluct & ")" Range("C2:C11").Formula =**

**Range("C2:C11").Value**

```
Range("D12:N12").Formula =
```
**"=RANDBETWEEN(" & (pMinRate \* 100) & " , " & (pMaxRate \* 100) & ")/100"**

**Range("D12:N12").Formula =**

**Range("D12:N12").Value For iYears = 10 To 100 Step 10 Range("B15") = iYears Range("B16:B25").Formula = "=HLOOKUP(" & iYears & " ,\$D\$1:\$N\$11,ROW(A2),0)" MsgBox "After " & iYears & " years." Next iYears Range("B16:B25").Formula = Range("B16:B25").Value Loop Until MsgBox("Another run?" , vbYesNo) = vbNo End Sub**



## **Chapter 54: Predator-Prey Cycle What the simulation does**



The so-called Lotka-Volterra model, dealing specifically with the relationship between predator and prey (or hunter and target) makes the following simplified assumptions: The change in the prey's numbers is given by its own growth minus the rate at which it is preyed upon (E2). On the other hand, the change in growth of the predator population is fueled by the food supply, minus natural death (E3). The equations that were used are explained on the sheet.

#### **What you need to know**



This simulation loops randomly through the values in I2:K4 to determine the three settings for A2:C2. Based on these settings, it plots the corresponding charts next to each other on a new sheet. The title of each chart specifies what the specific three values for A2:C2 were (see also Chapter 97).

```
Sub LotkaVolterra()
  Do
    Range("A2") =
Cells(WorksheetFunction.RandBetween(2, 4), 9)
    Range("B2") =
Cells(WorksheetFunction.RandBetween(2, 4), 10)
    Range("C2") =
Cells(WorksheetFunction.RandBetween(2, 4), 11)
    CreateCharts 'see Sub below
  Loop Until MsgBox("Loop again?"
, vbYesNo) =
vbNo
End Sub
Sub CreateCharts()
  Dim oRange As Range, i As Integer, oChart As
Chart, sCaption As String
  Dim oWS As Worksheet, bWS As Boolean, oAS As
Worksheet
  Set oAS = ActiveSheet
  For Each oWS In Worksheets
    If oWS.Name = "Chart" Then bWS = True
  Next oWS
  If bWS = False Then
    Set oWS = Worksheets.Add(, ActiveSheet):
```
**oWS.Name = "Chart" Else Set oWS = Worksheets("Chart") End If oAS.Select Set oRange = Range("B5").CurrentRegion Set oChart = Charts.Add With oChart .SetSourceData oRange: .ChartArea.Border.Weight = xlThick .ChartType = xlXYScatterSmoothNoMarkers .HasTitle = True: .Axes(xlCategory).MaximumScale = 500 .FullSeriesCollection(1).XValues = .FullSeriesCollection(1).XValues .FullSeriesCollection(2).Values = .FullSeriesCollection(2).Values sCaption = oAS.Range("A2") & "|" & oAS.Range("B2") & "|" & oAS.Range("C2") .ChartTitle.Caption = sCaption: .Location xlLocationAsObject, oWS.Name End With oWS.Activate For i = 1 To oWS.ChartObjects.Count With oWS.ChartObjects(i) .Width = ActiveWindow.Width \* 0.4: .Height = ActiveWindow.Height \* 0.6**

**.Left = ((i - 1) Mod oWS.ChartObjects.Count) \* ActiveWindow.Width \* 0.41**

**.Top = Int((i - 1) / oWS.ChartObjects.Count) \* 150**

**End With**

**Next i**

**MsgBox "Here is the Chart": oAS.Activate End Sub**

## **Chapter 55: Taking Medication What the simulation does**



When taking medication, we want to reach a rather steady concentration of the medicine inside the body. The concentration rises each time we take a pill, but then it also declines because the body metabolizes and/or excretes it.

We simulate this process based on at least 5 parameters. The three important ones are the number of pills a day (B1), the strength of each pill (B3), and the elimination factor (B4). You may want to change these variables manually to find out what the best regimen is.

#### **What you need to know**

The simplest model would be as follows: If  $u(t)$  is the concentration of the medication in the body, then  $du = b f(t) dt - cu dt$ . In words: the change in concentration equals (the amount of medication entering the body at time *t* during the period *dt*) minus (the amount of medication leaving the body during a small time interval *dt*). Instead of differentiating the equation, we use an Excel simulation.

The formula in cell B10 and down is complex and looks like this:

 $=$ IF(AND(A10>INT(\$B\$1\*A10)/\$B\$1,A10<INT(\$B\$1\*A10)/\$B\$1+\$B\$6),8 In VBA, we build this formula up in two pieces to keep the line more manageable.

The formula in C11 and down determines the concentration at a specific point in time: =C10+\$B\$5\*(\$B\$2\*B11-\$B\$3\*C10).

The simulation loops through the number of pills, running from 1 to 5 pills, and another loop that builds up the cells 11 to 211 in columns A:C. Since the 2<sup>nd</sup> loop has a *Timer* interval in it, we see the data and the chart gradually building up.

**Option Explicit**

```
Sub Medication()
  Dim n As Integer, i As Integer, pTime As Double,
sStr As String
  Dim pDosage As Double, pElim As Double, pUnit
As Double, pInterv As Double
  pDosage = Range("B3"): pElim =
Range("B4"): pUnit = Range("B6"): pInterv =
Range("B7")
  For n = 1 To 5 'for number of pills
    Range("B1") = nRange(Cells(11, 1), Cells(211, 3)).ClearContents
    For i = 11 To 211
       Cells(i, 1) = Cells(i - 1, 1) + pInterv
       sStr = "INT(R1C2*RC[-1])/R1C2"
       Cells(i, 2).FormulaR1C1 =
"=IF(AND(RC[-1]>" & sStr & "
,RC[-1]<" & sStr &
"+R6C2),8,0)"
       Cells(i, 2).Formula = Cells(i, 2).Value
       Cells(i, 3) = Cells(i - 1, 3) + pInterv *
(pDosage * Cells(i, 2) - pElim * Cells(i - 1, 3))
       pTime = Timer + 0.005
       Do While Timer < pTime
```
**DoEvents Loop Next i sStr = "This is for " & n & " pills per day." If n < 5 Then If MsgBox(sStr & vbCr & "Continue?" , vbYesNo) = vbNo Then Exit Sub Else MsgBox sStr End If Next n End Sub**



# **Chapter 56: The Course of an Epidemic**

**What the simulation does**



In this simple simulation, we follow the course of an epidemic (e.g. the flu) based on certain variables in column H. In general, epidemics follow a more or less fixed pattern. Initially only a few people get sick, but soon the number of sick cases rises exponentially until stabilization sets in, and more and more people have recovered.

We need some essential parameters, although they may not always be exactly known. We will only focus on transmission rate, recovery rate, and death rate—without going into issues such as mutation rate for the virus or bacterium.

The model that we apply is the standard *SIR* model, commonly used for many infectious diseases. The name of the model reflects the three groups of individuals that it models: *S*usceptible people, *I*nfected people, and *R*ecovered people. There are a number of important thresholds in this model. Reaching, or failing to reach, these thresholds is a crucial feature of managing the spread of infectious diseases. The system is sensitive to

certain changes and not to others, so this may give us some insight as to when and where the problem should be attacked.

In order to make the appropriate calculations, we use the Euler's method, without explaining it any further. You can find it explained elsewhere.

#### **What you need to know**

The simulation gradually fills 300 cells in each of the columns A:E with the appropriate equations. It does this in steps, thanks to a *Timer* loop. To keep track of its progress, cell N1 is being updated during the process. This is also done with some kind of simple progress bar in cell J8 by using the function REPT. This function repeats a certain charcter as often as the  $2<sup>nd</sup>$ argument indicates.

At the end of the simulation, a *MsgBox* reports how many people were susceptible, infected, recovered, or died during the course of the epidemic

**Option Explicit**

```
Sub Epidemic()
  Dim sMsg As String, pTime As Double, i As Long
  Range("A3:E302").ClearContents
  'If MsgBox("Are the values in column H as you
want them?"
, vbYesNo) = vbNo Then Exit Sub
  For i = 3 To 302
    Cells(i, 1).FormulaR1C1 = "=R[-1]C+R1C8"
'A2+$H$1"
    Cells(i, 2).FormulaR1C1 = "=R[-1]C-
(R6C8*R[-1]C*R[-1]C[1])*R1C8"
    Cells(i, 3).FormulaR1C1 = "=R[-1]C+
(R6C8*R[-1]C[-1]*R[-1]C-R7C8*R[-1]C)*R1C8"
    Cells(i, 4).FormulaR1C1 = "=R[-1]C+((1-
R8C8)*R7C8*R[-1]C[-1])*R1C8"
    Cells(i, 5).FormulaR1C1 = "=R[-1]C+
(R8C8*R7C8*R[-1]C[-2])*R1C8"
    Range("N1") = "done " & FormatPercent(i /
302, 0)
    Range("J8") = WorksheetFunction.Rept(">"
, i /
302 * 100)
      If i / 302 <= 0.25 Then
```

```
If i Mod 5 = 0 Then
```
**pTime = Timer Do While Timer < pTime + 1.5 DoEvents Loop End If End If Next i sMsg = "Total recovered: " & FormatNumber(Range("D302"), 0) & vbCr sMsg = sMsg & "Total deaths: " & FormatNumber(Range("E302"), 0) & vbCr sMsg = sMsg & "Total never sick: " & FormatNumber(Range("B302"), 0) & vbCr sMsg = sMsg & "Max sick at once: " & FormatNumber(WorksheetFunction.Max(Columns(3)), 0) MsgBox sMsg If MsgBox("Do you want to keep the formulas on**

```
the sheet?"
, vbYesNo) = vbNo Then
```

```
Range("A3:E302").Formula =
```

```
Range("A3:E302").Value
```

```
End If
```
**End Sub**



# **Chapter 57: Boltzmann Equation for Sigmoidal Curves**

**What the simulation does**



This simulation deals with curves that are of the logistic, s-shaped, or sigmoidal type, so we could use the Boltzmann equation as explained in the figure above (where E is the independent variable in column A, and V the half-way activity). The values in columns C:E and H are all calculated (see figure on the next page), except for the values in H1 and H2, which are based on an educated guess.

Something similar can be done for EC50 or IC50 determination.The term "half maximal effective concentraion" (EC50) refers to the concentration of a drug, antibody, or toxicant which induces a response halfway between the baseline and maximum after a specified exposure time. It is commonly used as a measure of a drug's *ef ective* potency. (IC50, on the other hand, is the "half maximal *inhibitory* response.")

The columns D and E calculate the confidence interval on both sides of the curve of observed values based on cell H8 (see Chapter 18).



#### **What you need to know**

In order to get a more accurate value for the half-way value and the slope, we need to set the *Sum of Squared Residuals* (H6) to a minimum, which means that the difference between what we observed and what we expected according to the equation is minimal.

We can do so by using Excel's *Solver* tool. Make sure *Solver* is active in VBA: Tools | References | Solver ON. Now the macro can call Solver. On the screen shot to the left, cell H6 is set to a minimum by changing the variable cells H1:H2 (the educated guesses). Since there can be several solutions to this problem, it is wise to add some constraints—for instance, that H1 should be between -5 and -15.

**Option Explicit**

```
Sub Boltzman()
```
**Dim pHalfX As Double, pSlope As Double**

**Range("C2:E20").ClearContents:**

**Range("H1:H8").ClearContents**

```
pHalfX = InputBox("Guess half-X-value for half-Y
at 0.5"
, , -10)
```
**pSlope = InputBox("Guess what the slope would be" , , 10)**

```
Range("H1").Formula = pHalfX:
```
**Range("H2").Formula = pSlope**

```
Range("H3").Formula = "=AVERAGE(B:B)"
'mean Y
```
**Range("H4").Formula = "=COUNT(B:B)-**

**COUNT(H1:H2)" 'degrees of freedom**

**Range("H5").FormulaArray =**

**"=SQRT(SUM((B2:B20-C2:C20)^2)/H4)" 'Standard Error Y**

**Range("H6").FormulaArray = "=SUM((B2:B20- C2:C20)^2)" 'Sum Squared Residuals**

```
Range("H7").Formula = "=TINV(0.05,H4)"
```
**'Critical t-value**

**Range("H8").Formula = "=H7\*H5" 'Confidence**

#### **Interval**

### **Range("C2:C20").Formula = "=(1/(1+EXP((\$H\$1- A2)/\$H\$2)))"**

**Range("D2:D20").Formula = "=C2+\$H\$8" Range("E2:E20").Formula = "=C2-\$H\$8" 'Tools | References | Solver ON SolverOkDialog "H6" , 2, 0, "H1:H2" , 1, "GRG Nonlinear" End Sub**

 $^{\rm B}$ Ð  $\mathsf A$ Ċ E F. G  $H$ 1 Voltage Data Boltzmann **Upper CI** Lower CI Half-value  $-15$  $\boxed{0} = [1/(1+EXP((SH$1-A2)/$H$2))]$ =C2+\$H\$8 =C2-\$H\$8 Slope  $2 - 60$ 5 =(1/(1+EXP((\$H\$1-A3)/\$H\$2))) =C3+\$H\$8 =C3-\$H\$8 =AVERAGE(B:B)  $3 - 55$  $|0\rangle$ Mean-Y  $4 - 50$  $0.05$  =  $(1/(1+EXP((5H$51-A4)/$H$52)))$ =C4+\$H\$8 =C4-\$H\$8 df =COUNT(B:B)-COUNT(H1:H2)  $5 - 45$  $0.08 = (1/(1+EXP((5H51-AS)/SH52))) = CS+SH58 = CS-SH58$ SE-Y =SQRT(SUM((B2:B20-C2:C20)^2)/H4)  $6 - 40$  $\overline{0.1}$  =(1/(1+EXP((\$H\$1-A6)/\$H\$2))) =C6+\$H\$8 =C6-\$H\$8 SumSqRes =SUM((B2:B20-C2:C20)^2)  $7 - 35$  $|0.15|$  = (1/(1+EXP((\$H\$1-A7)/\$H\$2))) = C7+\$H\$8 = C7-\$H\$8 Crit. T =TINV(0.05,H4)  $8 - 30$  $\frac{0.18}{1}$  = (1/(1+EXP((\$H\$1-A8)/\$H\$2))) = C8+\$H\$8 = C8-\$H\$8  $=$ H7\*H5  $CI$ 

## **Chapter 58: Interpolation What the simulation does**



Interpolation is a process of estimating a missing value by using existing, observed values. For example, in a graph, you might want to mark a specific point on the curve that has not been measured; so it has to be interpolated. The graph must be of the *XY* type because interpolation works with values in between—and such values do not exist in charts carrying a *category* axis.

This time the simulation is not done with a macro script in a *Module*, but it is activated by the sheet itself when the user changes the number in cell E1. In the VBA editor, double-click the sheet in the panel to the left (see figure below). Then you select *Worksheet* from the dropdown in the left top corner followed by *Change* in the right top corner. This creates a *Sub Worksheet\_Change* in your VBA code.



### **What you need to know**

To plot an interpolation insert in your XY-graph you need three sets of coordinates (E5:F7) based on the observed value just before your target value and the one just after your target value. To find these coordinates you need three Excel functions: MATCH, INDEX, and TREND.

The function MATCH is needed to locate in which row the value of E1 was found. MATCH has 3 arguments: what to match (E1), in which range (column A), and with which match type 1 for an ascending list (0 for an exact match, and -1 for a descending list). This locates the target value (E1) in column A, by looking for the closest previous value in an ascending order (1).

Now INDEX can find the corresponding value in the same row and in one row farther down  $(+1)$ —that is, for column A: E2+E3; for column B: F2:F3.

To calculate the interpolated X-value between E2 and E3, and the interpolated Y-value between F2 and F3, we need the TREND function. It has this syntax: TREND(2 known Y's, two known X's, target X). This way, we are able to find E6:E7 and F5:F6. Cells E5 and F6 should be 0 if both axes start at 0.

**Private Sub Worksheet\_Change(ByVal Target As Range)**

**Dim oRange As Range, vIndex As Variant, vMatch As Variant**

**Dim vMinX As Variant, vMinY As Variant, vTrend As Variant**

**If Target.Address <> "\$E\$1" Then Exit Sub Set oRange = Range(Cells(2, 1),**

**Cells(Range("A1").CurrentRegion.Rows.Count, 2)) If Range("E1") >=**

**WorksheetFunction.Max(oRange.Columns(1)) Then Exit Sub**

**Range("E1:F1").Merge**

**vMatch =**

**WorksheetFunction.Match(Range("E1"),**

**oRange.Columns(1), 1)**

**vIndex = WorksheetFunction.Index(oRange,**

**vMatch, 1): Range("E2") = vIndex**

**vIndex = WorksheetFunction.Index(oRange,**

**vMatch, 2): Range("F2") = vIndex**

**vIndex = WorksheetFunction.Index(oRange,**

**vMatch + 1, 1): Range("E3") = vIndex**

**vIndex = WorksheetFunction.Index(oRange,**

**vMatch + 1, 2): Range("F3") = vIndex**  $vMinX =$ 

```
WorksheetFunction.Min(oRange.Columns(1)):
Range("E5") = vMinXRange("E6") = Range("E1"): Range("E7") =
Range("E1")
  vTrend =
WorksheetFunction.Trend(Range("F2:F3"),
Range("E2:E3"), Range("E1"))
  Range("F5") = vTrend: Range("F6") = vTrendvMinY =WorksheetFunction.Min(oRange.Columns(2)):
Range("F7") = vMinYIf MsgBox("A separate graph?"
, vbYesNo) = vbYes
Then Charting
End Sub
Sub Charting()
  Dim r As Long, pMin1 As Double, pMin2 As
Double, sX As String, sY As String
  Dim oChart As Chart, oRange As Range
  Set oRange = Range("A1").CurrentRegion: r =
oRange.Rows.Count
  sX = Range(Cells(2, 1), Cells(r, 1)).Address: sY =
Range(Cells(2, 2), Cells(r, 2)).Address
  Set oRange = Union(Range(sX), Range(sY)): Set
oChart = Charts.Add(, ActiveSheet)
  With oChart
    .ChartType = xlXYScatterSmooth:
```
**.SetSourceData oRange .HasTitle = True: .HasLegend = True:.Axes(xlCategory).HasMajorGridlines = True .Axes(xlCategory).HasMinorGridlines = True: pMin1 = WorksheetFunction.Min(Columns(1)): pMin2 = WorksheetFunction.Min(Columns(2)) .Axes(xlValue).MinimumScale = IIf(pMin1 < pMin2, Int(pMin1), Int(pMin2)) .Axes(xlValue).HasMinorGridlines = True .ChartTitle.Caption = "Graph based on columns " & \_ vbCr & Cells(1, 1) & " and " & Cells(1, 2) & " for X=" & Range("E1") .SeriesCollection(1).Name = Cells(1, 1): .SeriesCollection(2).Name = Cells(1, 2) End With With oChart.SeriesCollection.NewSeries .XValues = Range("E5:E7"): .Values = Range("F5:F7") .Name = "insert": .ChartType = xlXYScatterLines .HasDataLabels = True: .DataLabels.Select Selection.ShowCategoryName = True: Selection.ShowValue = True End With oChart.SizeWithWindow = True**

## **End Sub**
### **Chapter 59: A Rigid Pendulum What the simulation does**



Sheet5 has two *Commandbuttons* which run VBA code on Sheet5 when you click on the buttons. This way the pendulum can start swinging, can pause swinging, or can be reset. The calculations in the background (columns M through Z) are based on the values that can be manually set in column B. The VBA code only regulates when the calculations are being updated.

#### **What you need to know**

This simulation is partly borrowed from George Lungu. The major factor involved in the equations for calculating the frequency of a pendulum is the length of the rod or wire, provided the initial angle or amplitude of the swing is small. The mass or weight of the bob is not a factor in the frequency of the simple pendulum, but the acceleration of gravity is in the equation. Knowing the length of the pendulum, you can determine its frequency. Or, if you want a specific frequency, you can determine the necessary length.

The period of the motion for a pendulum is how long it takes to swing back-and-forth, measured in seconds. Period is designated as *T*. The frequency of a pendulum is how many back-and-forth swings there are in a second, measured in hertz. Frequency is usually designated as *f*. The period *T* is the reciprocal of the frequency: *T=1/f* and *f=1/T*.

The equation for the period of a simple pendulum starting at a small angle (*a*) is:  $T=2pi*SORT(L/g)$  or  $T=2\pi\sqrt{(L/g)}$ .

Notice how columns Y and Z change dramatically and quickly while the macro runs.



**'This code is on Sheet5 Private Sub Reset\_\_Click() Range("B22") = "RESET" Range("B16") = 0 End Sub Private Sub Release\_\_Click() i = Range("B16") If Not (Range("B22") = "ON") Then Range("B22") = "ON" Else Range("B22") = "PAUSE" Exit Sub End If Do If i < 3000 And Range("B22") = "ON" Then DoEvents**  $i = i + 1$ **Range("B16") = i If Range("B22") = "PAUSE" Then Exit Sub If Range("B22") = "RESET" Then Range("B16") = 0: Exit Sub Else**  $\mathbf{i} = \mathbf{0}$ 

### **Range("B16") = 0 End If Loop End Sub**

## **Chapter 60: A Piston Sinusoid What the simulation does**



The periodic rotation of the piston-crankshaft assembly in an engine generates a sinusoid when we plot the angle of rotation of the crankshaft versus the distance from the piston to the center of the circle. If the radius of the circle is changed, then the sinusoid also changes.

This file simulates the engine and the resulting sinusoid. The VBA code runs *a* (the minimum distance from the piston to the top of the circle) from 1 to 7, and the radius from 0 to 360. During each loop, the accompanying graph nicely builds up in a timed fashion.

#### **What you need to know**

Sheet1 uses equations implemented on Sheet2. The simulation is partly borrowed from David Hill. It plots the angle of rotation of the crankshaft versus the distance from piston to the center of the circle. Here are the needed equations on Sheet2.



### **Option Explicit**

**Sub Sinusoid() Dim i As Integer, j As Integer, pTime As Double Range("J27") = "no": Range("J27").Select**  $For i = 1$  To 7 **Sheet2.Range("C6") = i**  $For j = 0$  To 360 **Sheet2.Range("E1") = j pTime = Timer + 0.005 'Timer: secs since midnight; pause by .005 seconds Do While Timer < pTime DoEvents Calculate If Range("J27") = "yes" Then Exit Sub Loop Next j Next i End Sub**



# **Chapter 61: The Brusselator Model What the simulation does**



The Brusselator model was proposed by Prigogine and his coworkers in 1967 at Free University of Brussels. This model was created for the explanation of the mechanism of a Bray-Liebhafsky reaction proposed by Bray and Liebhafsky at University of California, Berkeley. This model is one of the oscillating reactions which can be seen in real cases.

#### **What you need to know**

The sheet has sliders that you can manually move. If you run the VBA code instead, it loops from 35 to 100 for cell D3 (behind the control) and from 100 to 240 for cell D4. If you want to stop the loops, type "yes" in cell D2 (and Enter). The cells C3:C5 do not have values in them but a formula that is connected to cells hidden behind the sliders.



#### **Option Explicit**

**Sub Oscillation() Dim i As Integer, j As Integer, pTime As Double Range("D2") = "no": Range("D2").Select**  $For i = 35$  To 100 **Range("D3") = i For j = 100 To 240 Range("D4") = j pTime = Timer + 0.005 'Timer: secs since midnight; pause by .005 seconds Do While Timer < pTime DoEvents Calculate If Range("D2") = "yes" Then Exit Sub Loop Next j Next i End Sub**



# **Chapter 62: A Hawk-Dove Game What the simulation does**



Game theory is the study of mathematical models of conflict and cooperation. The name "Hawk-Dove" refers to a situation in which there is a competition for a shared resource and the contestants can choose either conciliation or conflict; this terminology is most commonly used in biology and economics.

The traditional payoff matrix for the Hawk-Dove game includes the value of the contested resource, and the cost of an escalated fight. It is assumed that the value of the resource is less than the cost of a fight. Sometimes the players are supposed to split the payoff equally, other times the payoff is assumed to be zero. These values can be found in columns J, M, and N.

A "mixed" evolutionary strategy (ESS) is where two strategies permanently coexist. For a given set of payoffs, there will be one set of frequencies where this mix is stable. A mixed ESS can be achieved if individuals either play one strategy all of the time in a population where the two strategies are at the equilibrium frequencies (for example, 60% of the individuals always call and 40% always act as satellites), or all individuals

play a mixed strategy where each behavior in the mix is performed at the equilibrium frequency.

### **What you need to know**

The VBA code loops for the "gain" setting (cell J2) from 10 to 90 by increments of 10, and displays each time an *InputBox*, which can be cancelled to stop the loop.

Unlike a *MsgBox*, an *InputBox* can be positioned on the screen (through the  $4<sup>th</sup>$  and  $5<sup>th</sup>$  argument). When an *Inputbox* is cancelled, it returns an empty string (""). So we can check for an empty string and then exit the *For*-loop.

**Option Explicit**

**Sub HawkDove()**

**Dim iGain As Integer, sMsg As String, iTrick As String**

```
Range("B2:B10").Formula = "=A2*$F$2+(1-
A2)*$G$2"
```

```
Range("C2:C10").Formula = "=A2*$F$3+(1-
A2)*$G$3"
```

```
For iGain = 10 To 90 Step 10
```

```
Range("J2") = iGain
```

```
Sheet1.Calculate
```

```
sMsg = "The intersect for gain " & iGain & "
equals: " & _
```

```
FormatNumber(Range("B19"), 3)
'to position the MsgBox use an InputBox instead
iTrick = InputBox(sMsg, ,
"next"
, 1000, 2500)
If iTrick = "" Then Exit Sub
```

```
Next iGain
Range("J2") = 50
```
**End Sub**



# **VI. BUSINESS**

# **Chapter 63: Prognosis of Sales**

**What the simulation does**



This is basically a simple simulation. It gives a prognosis for each product based on its previous performance. It assumes that each product will sell next year according to a random distribution based on the average of pervious years' sales and the standard deviation of those sales. It does so with the Excel function NORMINV. The simulation also plots the 25<sup>th</sup> and 75 th percentile. Obviously, results will vary, but using a high number of loops (10,000) limits fluctuations.

#### **What you need to know**

The simulation loops slowly through each product, from B through K, thanks to a *Timer* interval. It shows progress by assigning a color to each finished cell of averages in row 22.







**Option Explicit**

**Sub Prognosis()**

**Dim r As Long, c As Integer, oRange As Range, i As Long, iTime As Long**

**Dim pAvg As Double, pSD As Double, arrRuns() As Double**

**MsgBox "Prognosis per column based on 10,000 iterations."**

**With Range("A1").CurrentRegion**

```
.Rows(.Rows.Count + 3).Interior.Color =
vbWhite
```

```
r = .Rows.Count
    For c = 2 To . Columns. Count
      pAvg =WorksheetFunction.Average(.Columns(c))
      pSD =
WorksheetFunction.StDev(.Columns(c))
       ReDim arrRuns(0 To 9999)
      For i = 0 To 9999
         arrRuns(i) =
WorksheetFunction.Norm_Inv(Rnd, pAvg, pSD)
      Next i
      i Time = Timer + 1
```

```
Do Until Timer > iTime
         DoEvents
       Loop
       Cells(r + 2, c) =WorksheetFunction.Percentile(arrRuns, 0.25)
       Cells(r + 3, c) =WorksheetFunction.Average(arrRuns)
       Cells(r + 4, c) =WorksheetFunction.Percentile(arrRuns, 0.75)
       With .Cells(r + 3, c).Interior
         If .Color = vbYellow Then .Color = vbWhite
Else .Color = vbYellow
       End With
    Next c
  End With
End Sub
```
# **Chapter 64: Cycle Percentiles What the simulation does**



This is a simple macro to show the user during a nice cycle of views what the best or worst sales were—in which months and on which days.

The macro does so by cycling through percentile views in steps of 10. It allows the user to specify whether to go up from the  $10<sup>th</sup>$  to  $90<sup>th</sup>$  percentile, or down from the  $90<sup>th</sup>$  percentile to the  $10<sup>th</sup>$  percentile. It also calculates the total amount of sales for each percentile view.

#### **What you need to know**

There is nothing really new in this VBA code. Based on a *Boolean* variable, set through a *MsgBox*, the cycle goes either up or down.

For the percentile scores, we used the Excel function PERCENTILE. This function works in all Excel versions. In version 2010 and later, it can be replaced with PERCENTILE.EXC or PERCENTILE. INC. The former function does not include  $k=1$ , whereas the latter one does. So the latter one is equivalent to the older function PERCENTILE.

Depending on the percentile step, certain numbers are "hidden" by assigning a white font. This is done by adding to the collection of *FormatConditions*. To prevent that these pile up, we delete all *FormatConditions* in the range of sales figures at the end.

To make everything work properly, the macro also needs to "play" with *ScreenUpdating* settings.



**Option Explicit**

```
Sub PercentileUpOrDown()
  Dim oRange As Range, oFormat As
FormatCondition
  Dim bDown As Boolean, i As Integer, iPerc As
Integer, pPerc As Double, sMsg As String
  If ActiveSheet.Name <> Sheet1.Name Then Exit
Sub
  Set oRange = Range("A1").CurrentRegion
  Set oRange = oRange.Offset(1,
1).Resize(oRange.Rows.Count - 1,
oRange.Columns.Count - 1)
  If MsgBox("Go Down? (No = Go Up)"
, vbYesNo) =
vbYes Then bDown = True: iPerc = 100
  For i = 1, To 9Application.ScreenUpdating = False
    If bDown Then iPerc = iPerc - 10 Else iPerc =
iPerc + 10
    pPerc =
WorksheetFunction.Percentile_Exc(oRange, iPerc /
100)
    Set oFormat =
```
**oRange.FormatConditions.Add(xlExpression,**

**xlFormula, "=B2<" & pPerc) 'not A1 Application.ScreenUpdating = True oFormat.Font.Color = vbWhite '.Interior.Color = RGB(0, 0, 0) with max of 255 sMsg = "Above the " & iPerc & "th percentile: " & FormatCurrency(pPerc) & vbCr & "Next?" If MsgBox(sMsg, vbOKCancel) = vbCancel** Then  $i = 9$ **Application.ScreenUpdating = False oRange.FormatConditions.Delete Application.ScreenUpdating = True Next i End Sub**

# **Chapter 65: Cost Estimates What the simulation does**



The cells A2:C3 are based on manual input, with the low estimates in row 2 and the high estimates in row 3.

For each of the columns A, B, and C, we simulate normally distributed values with a mean between low (row 2) and high (row 3) as well as a standard deviation of 2 units on either side. On the sheet, we use only 100 repeats up to row 103—which is rather risky. Column D calculates the monthly costs for each case.

To reduce the risk of estimating costs, the macro repeats these 100 steps some 10,000 times by storing the results for each run in arrays. Arrays work very swiftly and make our estimates less subject to random fluctuations.

At the end of the macro, a  $MsgBox$  displays the  $5<sup>th</sup>$  and  $95<sup>th</sup>$  percentile for these 1,000,000 projections. A new run of the macro will yield different results, but they differ only slightly.

#### **What you need to know**



#### **Option Explicit**

```
Sub Costs()
  Dim i As Long, d5Perc As Double, d95Perc As
Double, sMsg As String
  Dim arr5Perc() As Double, arr95Perc() As Double
  With Range("A4:D103")
    .ClearContents
    MsgBox "First normally distributed random
calculations:"
    Application.Calculation = xlCalculationManual
    .Columns(1).Formula =
"=NORMINV(RAND(),SUM(A$2:A$3)/2,
(MAX(A$2:A$3)-MIN(A$2:A$3))/4)"
    .Columns(2).Formula =
"=NORMINV(RAND(),SUM(B$2:B$3)/2,
(MAX(B$2:B$3)-MIN(B$2:B$3))/4)"
    .Columns(3).Formula =
"=NORMINV(RAND(),SUM(C$2:C$3)/2,
(MAX(C$2:C$3)-MIN(C$2:C$3))/4)"
    .Columns(4).Formula = "=A4/130*B4*C4"
    MsgBox "Now follow 10,000 runs with arrays:"
    ReDim arr5Perc(0 To 9999): ReDim arr95Perc(0
To 9999)
```

```
For i = 0 To 9999
       .Calculate
       arr5Perc(i) =
WorksheetFunction.Percentile(.Columns(4), 0.05)
       arr95Perc(i) =
WorksheetFunction.Percentile(.Columns(4), 0.95)
    Next i
  End With
  d5Perc = WorksheetFunction.Average(arr5Perc)
  d95Perc = WorksheetFunction.Average(arr95Perc)
  sMsg = "After 10,000 x 100 runs of monthly costs:"
& vbCr
  sMsg = sMsg & "the 5th percentile is:" & vbTab &
vbTab
  sMsg = sMsg & FormatCurrency(d5Perc, 2) &
vbCr & "the 95th percentile is:"
  sMsg = sMsg \& \text{vbfTab} \&FormatCurrency(d95Perc, 2)
  MsgBox sMsg
End Sub
```


# **Chapter 66: A Filtering Table What the simulation does**



Range G6:J14 contains a 2-dimensional table with information that the macro has extracted from the database A1:E25. The macro also creates a filter in A27:E28 which regulates what the table G6:J14 displays (in this case, whatever was sold with quantities over 400.

The filter works through the labels, or headers, of the database. The filter sums the totals by using the function DSUM at the origin of the table (G6).



#### **What you need to know**

To create a list of unique entries in row1 and column1 of the table

(G6:J14), we can use *AdvancedFilter*. It has four arguments: Action (e.g. xlFilterCopy), CriteriaRange (optional), CopyToRange, Unique (True).

Since *AdvancedFilter* returns a vertical list of unique entries, we need to manipulate the two lists. This can be done by storing the two lists in a *Variant* array that is 2-dimensional. The array helps us to place the lists in a 2-dimensional table by using a loop for the  $1<sup>st</sup>$  dimension inside a loop for the 2<sup>nd</sup> dimension. The function *UBound*(array, 1) returns the index number of the last element in the 1 st dimension; *UBound*(array,2) does that for the 2<sup>nd</sup> dimension.

In cell G5, the macro implements DSUM. Unlike SUM, it accepts also certain criteria as to what to sum. It has 3 arguments: the database, the field label, and the criteria range (A27:E28).

**Option Explicit**

```
Sub Filtering()
```
**Dim vArr As Variant, i As Integer, j As Integer, sFilter As String**

**Dim oFilter As Range, oRange As Range Range("G6").CurrentRegion.Delete xlShiftToLeft With Range("A1").CurrentRegion**

**i = .Rows.Count**

**.Range(Cells(i + 2, 1), Cells(i + 3, 5)).Delete xlShiftUp**

**MsgBox "Prepare the matrix and the filter"**

**.Columns(1).AdvancedFilter xlFilterCopy, , Range("G6"), True**

**.Columns(2).AdvancedFilter xlFilterCopy, , Range("H6"), True**

```
Set oFilter = .Range(Cells(i + 2, 1), Cells(i + 3,
5))
```
**oFilter.Rows(1) = .Rows(1).Value End With With Range("G6") vArr = .CurrentRegion .CurrentRegion.ClearContents MsgBox "Fix the matrix"**

```
For i = 2 To UBound(vArr, 1) '1 is label |
UBound(x,1) is 1st dimension
       For j = 2 To UBound(vArr, 2) '1 is label |
UBound(x,2) is 2nd dimension
         .Offset(i - 1, 0) = vArr(i, 1).Offset(0, i - 1) = vArr(i, 2)Next j
    Next i
    MsgBox "Implement the filter"
    Set oRange = Range("A1").CurrentRegion
     .Cells(1, 1).Formula = "=DSUM(" &
oRange.Address & "
,E1,
" & oFilter.Address & ")"
'E1 is the Totals label
     .Cells(1, 1).CurrentRegion.Table Range("B28"),
Range("A28")
     .Cells(1, 1).CurrentRegion.NumberFormat =
"$##0.00"
    .Cells(1,
1).CurrentRegion.EntireColumn.AutoFit
  End With
  oFilter.Cells(2, 4) = InputBox("Sold filter (or
Cancel)"
, ,
">400")
  oFilter.Cells(2, 5) = InputBox("Total filter (or
Cancel)"
, ,
">300")
End Sub
```


# **Chapter 67: Profit Changes What the simulation does**



This simulation creates and populates five different *Data Table* ranges. The first three have a column input of D2, which holds the price per unit. However, we have a powerful "trick" here: there is no value in cell D2 but a formula that multiplies its value with (1+D2), so the *Data Table* can use price changes in percentages in its  $1<sup>st</sup>$  column, and the corresponding price in the 3<sup>rd</sup> column.

#### **What you need to know**

Since cells such as B2 and B3 don't contain a value but a formula, the macro locks and protects all cells, so no formulas can be overwritten. The *Protect* method of VBA can do so; it has many arguments; the 5<sup>th</sup> one is *UserInterfaceOnly*; when set to True, macro's can still change cells, but users cannot.



A *Variant* type of variable can hold an array, even an array that comes from the VBA function *Array*. In our simulation, the *Array* function holds the addresses of 5 cell ranges, and returns a 1-dimensional array. (You can always check this in your code by placing a *BreakPoint* after the array line and then opening the *Locals Window*.) Based on this list, the corresponding ranges can be cleared.

A combination of *Of set* and *Resize* allows VBA to change ranges. For example. *Range*("A1:D4").Offset(1,1).Resize(4,4).Address would change the range from A1:D4 to B2:E5.
**Option Explicit**

```
Sub Profits()
```
**Dim oUnitPrice As Range, oCostPrice As Range, oUnitsSold As Range**

**Dim oUnitAndCost As Range, oUnitAndSold As Range**

**Dim pUnitPrice As Double, pCostprice As Double, iSold As Long, vArr As Variant, i As Integer**

**vArr = Array("E3:F13" , "H3:I13" , "K3:L13" , "E16:I20" , "E24:I28")**

 $For i = 0$  To **UBound**(vArr)

**Range(vArr(i)).ClearContents**

**Next i**

**Sheet1.Protect , , , , True 'no changes on sheet except throug macro (=true)**

**pUnitPrice = InputBox("Best estimate of the unit price?" , , 125)**

**Range("B2").Formula** =  $"=(1+D2)*"$  & pUnitPrice **pCostprice = InputBox("Best estimate of the cost price?" , , 25)**

**Range("B6").Formula** =  $"=(1+G2)*"$  & pCostprice **iSold = InputBox("Best estimate of items sold?" , , 100000)**

```
Range("B3"). Formula = "=(1+J2)*" & iSold
  Set oUnitPrice = Range(vArr(0)).Offset(-1,
-1).Resize(Range(vArr(0)).Rows.Count + 1,
Range(vArr(0)).Columns.Count + 1)
  Set oCostPrice = Range(vArr(1)).Offset(-1,
-1).Resize(Range(vArr(1)).Rows.Count + 1,
Range(vArr(1)).Columns.Count + 1)
  Set oUnitsSold = Range(vArr(2)).Offset(-1,
-1).Resize(Range(vArr(2)).Rows.Count + 1,
Range(vArr(2)).Columns.Count + 1)
  Set oUnitAndCost = Range(vArr(3)).Offset(-1,
-1).Resize(Range(vArr(3)).Rows.Count + 1,
Range(vArr(3)).Columns.Count + 1)
  Set oUnitAndSold = Range(vArr(4)).Offset(-1,
-1).Resize(Range(vArr(4)).Rows.Count + 1,
Range(vArr(4)).Columns.Count + 1)
  oUnitPrice.Table , Range("D2")
  oCostPrice.Table , Range("G2")
  oUnitsSold.Table , Range("J2")
  oUnitAndCost.Table Range("G2"), Range("D2")
  oUnitAndSold.Table Range("J2"), Range("D2")
End Sub
```


# **Chapter 68: Risk Analysis**

**What the simulation does**



If the demand for some product is regulated by a range of probabilities (G2:H4), then you can determine your optimal production by simulating demand within that range of probabilities and calculating profit for each level of demand.

The top left section (B:C) calculates the profit for one trial production quantity. Cell C1 has a trial production quantity. Cell C2 has a random number. In cell C3, we simulate demand for this product with the function VLOOKUP: =VLOOKUP(RAND(),G2:H5,2,1).

The macro creates a *Data Table* which simulates each possible production quantity (10,000, 20,000, 40,000 or 60,000) some 1,000 to 100,000 times and calculates profits for each trial number (1 to 1,000) and each production quantity (10,000, etc.). At the origin of the *Data Table* (A13) is a reference to the profit calculation in C8. The *Data Table* uses cell C1 (a specific production quantity) for the row input, and an empty cell (say, G14) for the column input.

Finally, row 10 calculates the mean profit for the four different production quantities. In the example shown at the end, the results indicate that production of 40,000 units results in maximum profits. Row 11 does something similar, but now for the standard deviation. Notice that the SD increases when the quantities increase.

#### **What you need to know**

The VLOOKUP function in C3 matches the value in C1 with the closest match in the first column of table F2:G5. The corresponding value from the second column in table F2:G5 is then entered into C3.

How does the *Data Table* work? Consider cell D14: the column input cell value of 1 is placed in a blank cell (G14) and the random number in cell C2 recalculates. The corresponding profit is then recorded in cell D14. Next the column cell input value of 2 is placed in the blank cell G14, and the random number in C2 again recalculates. The corresponding profit is entered in cell D15. And so on. A *Data Table* has an amazing power!



```
Sub Risks()
  Dim oRange As Range, oTable As Range, i As Long
  Range("B10:E11").ClearContents
  Range("C2").Formula =
"=VLOOKUP(RAND(),G2:H5,2,1)"
  Set oRange = Range("B14").CurrentRegion
  With oRange
    Set oTable = .Offset(1, 1).Resize(.Rows.Count -
1, .Columns.Count - 1)
  End With
  oTable.ClearContents
  i = InputBox("How many runs (1,000 - 100,000)?"
,
, 10000)
  Set oRange = Range(Cells(13, 1), Cells(13 + i, 5))
  oRange.Table Range("C1"), Range("G14")
  i = i + 3Range("B10:E10").FormulaR1C1 =
"=AVERAGE(R14C:R[" & i & "]C)"
  Range("B11:E11").FormulaR1C1 =
"=STDEV(R14C:R[" & i-1 & "]C)"
  MsgBox "Results based on 1,000 x " & Format(i -
3,
"#,##0") & " runs."
```
### **End Sub**



## **Chapter 69: Scenarios What the simulation does**



Predictions of expenses and revenues are subject to lots of uncertainty. Nevertheless, let's say we want to predict these under a few defined scenarios, such as the most likely, the best case, and the worst case scenario, in order to project a range of possible profit levels.

We use several tables to set up this calculation. The top left table shows the 3 scenarios that were actually chosen. There are actually six scenarios—two for each case—with settings as displayed in the  $2<sup>nd</sup>$  table (A13:F17).

The main calculations occur in the *Data Table* in the lower-right corner. It is two-dimensional, but has a "hidden" third dimension: the 3 scenarios that were actually chosen in the top left table. All values in column H depend on these 3 scenarios.

The user has a choice of six different scenarios—1 and 2 for the most likely scenario, 3 and 4 for the worst-case scenario, and 5 and 6 for the best-case scenario. So there are actually 8 possible combinations as is

shown in B20:B27 (135, 136, etc.). The macro loops through these comnbinations and shows the results for each combination in the table B19:E27.

#### **What you need to know**

The cells B3:F5 use the function HLOOKUP, which stands for Horizontal lookup. It is similar to VLOOKUP, only it searches horizontal data rather than columnar data. HLOOKUP is used in the top left table to locate the correct input in the scenario table A14:F17. Because the scenario numbers are in a row (row 14), we need a *horizontal* lookup—HLOOKUP, not VLOOKUP.

```
Sub Scenarios()
  Dim vArr As Variant, i As Integer, sCombo As
String, iRow As Integer, oTable As Range
  Range("C20:E27").ClearContents
  Range("I14:L1013").ClearContents
  i = InputBox("How many runs (100-1000)?"
, , 100)
  Set oTable = Range(Cells(13, 8), Cells(13 + i, 12))
'Starts at $H$13
  oTable.Table , Range("F11")
  vArr = Array(135, 136, 145, 146, 235, 236, 245, 246)
  For i = 0 To 7
    sCombo = vArr(i)Cells(2, 2) = Left(sCombo, 1): Cells(2, 4) =
Mid(sCombo, 2, 1): Cells(2, 6) = Right(sCombo, 1)
    Application.Calculate
    iRow =
WorksheetFunction.Match(CInt(sCombo),
Range("B20:B27"))
    Range("C20:E27").Cells(iRow, 1) =
Range("L4")
    Range("C20:E27").Cells(iRow, 2) =
Range("L6")
```
### **Range("C20:E27").Cells(iRow, 3) = Range("L8") Cells.EntireColumn.AutoFit MsgBox "Results for scenarios " & Range("K2") Next i End Sub**



## **Chapter 70: Market Growth What the simulation does**



When talking about GDP growth (*G*ross *D*omestic *P*roduct) and the relationship between GDP growth and market growth, or the increase in market share, we are dealing with three uncertain inputs. The obvious approach is to use the best estimate for each of these inputs.

A better approach might be using a probability distribution, rather than using the single best estimate. Monte-Carlo modelling would use the probability distributions of the inputs. Rather than using the distributions themselves as inputs, we use the distributions to generate random inputs.

Based on a certain market volume (cell D1) and a certain market share (cell F1), the simulation calculates possible sales volumes (column G). It uses random distributions in 100 to 1,000 runs to estimate GDP growth (column A), the relationship between GDP and market size (column B), and the market share growth (column E).

Then it repeats this set of runs another 100 to 1,000 times, in columns J:K. After at least 10,000 runs, we get an rather good estimate of the minimum and maximum sales volumes in column N. Needless to say that these figures can still vary quite a bit, because Monte Carlo simulations become more reliable when based on at least 1,000,000 runs.

#### **What you need to know**

The model we use is basically very simple:

- C3: market growth = GDP growth  $\times$  multiple
- D3: market size = current size  $\times$  (market growth + 1)
- F3: market share  $=$  current market share  $+$  gain
- G3: sales volumes = market size  $\times$  market share

### **Option Explicit**

```
Sub Market()
  Dim i As Long, n As Long, oRange As Range,
oTable As Range
  Set oRange = Range("B6").CurrentRegion
  With oRange
    Set oRange = .Offset(1, 0).Resize(.Rows.Count -
1, .Columns.Count)
  End With
  oRange.ClearContents
  Set oTable = Range("J7").CurrentRegion
  With oTable
    Set oTable = .Offset(1, 1).Resize(.Rows.Count -
1, .Columns.Count - 4)
  End With
  oTable.ClearContents
  i = InputBox("How many row calculations (100-
1000)?"
, , 100)
  n = InputBox("How many table runs (100-1000)?"
,
, 100)
  Range("J6") = i & "x" & n & " = " & i * n & "
calculations"
```
**Set oRange = Range(Cells(7, 2), Cells(6 + i, 8))**

**oRange.Columns(1).Formula = "=NORMINV(RAND(),\$B\$3,\$B\$4)" oRange.Columns(2).Formula = "=NORMINV(RAND(),\$C\$3,\$C\$4)" oRange.Columns(3).Formula = "=B7\*C7" oRange.Columns(4).Formula = "=\$D\$1\*(D7+1)" oRange.Columns(5).Formula = "=NORMINV(RAND(),\$F\$3,\$F\$4)" oRange.Columns(6).Formula = "=\$F\$1+F7" oRange.Columns(7).Formula = "=E7\*G7" Set oTable = Range(Cells(7, 10), Cells(6 + n, 11)) oTable.Cells(1, 1).Formula = "=AVERAGE(" & oRange.Columns(7).Address & ")" oTable.Cells(1, 2).Formula = "=AVERAGE(" & oRange.Columns(7).Address & ")" oTable.Table , Range("I6") Range("N7").Formula = "=MIN(" & oTable.Columns(2).Address & ")" Range("N8").Formula = "=MEDIAN(" & oTable.Columns(2).Address & ")" Range("N9").Formula = "=MAX(" & oTable.Columns(2).Address & ")" Range("J6") = "Results of " & i & " x " & n & " runs." MsgBox Range("J6") End Sub**



## **Chapter 71: A Traffic Situation What the simulation does**



A Monte Carlo simulation really illustrates how we can tame the uncertainty of the future with ranges and probabilities, but it also shows how impossible it is to be extremely precise.

Column A: We simulate driving 2 miles on a highway, with 90% probability we will average 65 MPH, but with a 10% probability that a traffic jam will result in an average speed of 20 MPH (column A).

Column B: Then there is a traffic light that goes through a 120 second cycle with 90 seconds for "red" and 30 seconds for "green." If we hit it on green then there is no delay, but if we hit it on red we must wait for green.

Column C: Finally, we have 2 more miles to go: 70% of the time at 30 MPH, 10% at 20 MPH, 10% at 40 MPH, and 10% of the time it takes us 30 minutes. This can be calculated with a VLOOKUP function based on H2:I5.

Instead of using a fixed value for input variables, we can model an input variable with a probability distribution and then run the model a large number of times and see what impact the random variation has on the output.

Again, it is wise to run at least 1,000 iterations in the columns A:E. This is to ensure that we have a statistical chance of getting sufficient outliers (extreme values) to make the variance analysis meaningful. This is

important because as the number of iterations increases, the variance of the average output decreases.

#### **What you need to know**

The simulation also adds a *Data Table* that shows how the median and the average can slightly vary when repeated some 12 times (see screen shot on the next page).

Much more could have been done to this simulation—such as using arrays, more looping, and higher numbers of runs—but I leave that up to you.

```
Sub TrafficCommute()
  Dim oRange As Range, oTable As Range
  Dim sMsg As String, pMedian As Double, pAvg As
Double
  Set oRange = Range("A1").CurrentRegion
  With oRange
    Set oRange = .Offset(1, 0).Resize(.Rows.Count -
1, .Columns.Count)
  End With
  oRange.ClearContents:
Range("I9:J19").ClearContents
  MsgBox "New calculations"
  oRange.Columns(1).Formula = "=IF(RAND() <
0.9, 111, 360)"
  oRange.Columns(2).Formula = "=MAX(0,
(RAND() * 120) - 30)"
  oRange.Columns(3).Formula =
"=VLOOKUP(RAND(),$H$2:$I$5, 2)"
  oRange.Columns(4).Formula = "=SUM(A2:C2)"
  oRange.Columns(5).Formula = "=D2/60"
  Range("I8").Formula = "=MEDIAN(E:E)":
Range("J8").Formula = "=AVERAGE(E:E)"
```

```
Set oTable = Range("H8:J19")
  oTable.Table , Range("G7")
  With oTable
    sMsg = "For 1000 x 12 runs:" & vbCr
    pMedian =
FormatNumber(WorksheetFunction.Median(.Columns(2)),
```

```
3)
```

```
sMsg = sMsg & "Median: " & vbTab & pMedian
& " mins." & vbCr
```

```
pAvg =
```
**FormatNumber(WorksheetFunction.Average(.Columns(3)), 3)**

```
sMsg = sMsg & "Average: " & vbTab & pAvg &
" mins." & vbCr
```
**End With MsgBox sMsg End Sub**



### **Chapter 72: Quality Control What the simulation does**



Here we are dealing with an assembly line that creates between 100 and 1,000 products (B1) per period of time. One particular variable of this product is supposed to be close to a value of 15 (B2) but is allowed to vary with a SD of 2 (B3), as shown some 1,000 times in column A.

To ensure quality, we take a certain percentage of samples (E1) in which we accept 2% defects (E2, or whatever is in there). Based on such a sample we decide, with 95% confidence (E3), to accept or reject the entire production lot.

Since this process is far from certain but depends heavily on probabilities, we repeat this process a number of times in the *Data Table* far to the right.

At the end of the simulation, the macro reports several averages in a *MsgBox*.

#### **What you need to know**

In cell D8, the VBA code inserts the following formula (copied down to E1007):

 $=$ IF(AND(ROW(D7)+1< $=$ (\$B\$1+7),COUNT(\$D\$7:D7)

<(\$B\$1\*\$E\$1)),IF(RAND()<=\$E\$1,A8,""),"")

In cell  $E8$ :  $=IF(D8\diamond$ "", $IF((ABS(SB$2-))$ D8)/\$B\$3)>1.96,"reject","OK"),"")

The function used in G6 is CRITBINOM. It determines the greatest number of defective parts that are allowed to come off an assembly line sample without rejecting the entire lot. It has 3 arguments: The number of trials, the probability of a success on each trial, and the criterion value (alpha). Recently, this function has been replaced withBINOM.INV.



```
Sub QualityControl()
  Dim oRange As Range, oTable As Range, sFormula
As String, sMsg As String
  Dim pAvgProd As Double, pAvgSampl As Double,
pAvgCount As Double, iReject As Integer
  Set oRange = Range("D8:E1007")
  With oRange
    .ClearContents
    sFormula = "=IF(AND(ROW(D7)+1<=
($B$1+7),COUNT($D$7:D7)
<($B$1*$E$1)),IF(RAND()<=$E$1,A8,
""""),
"""")"
'double quotes inside double quotes
    .Columns(1).Formula = sFormula
    sFormula = "=IF(D8<>""""
,IF((ABS($B$2-
D8)/$B$3)>1.96,
""reject""
,
""OK""),
"""")"
    .Columns(2).Formula = sFormula
  End With
  Set oTable = Range("J3").CurrentRegion
  With oTable
    Set oTable = .Offset(3, 1).Resize(.Rows.Count -
3, .Columns.Count - 1)
  End With
```
**With oTable .ClearContents Set oTable = .Offset(-1, -1).Resize(.Rows.Count + 1, .Columns.Count + 1) oTable.Table , Range("I1") End With With oTable pAvgProd = WorksheetFunction.Average(.Columns(2)) pAvgSampl = WorksheetFunction.Average(.Columns(3)) pAvgCount = WorksheetFunction.Average(.Columns(4)) iReject = WorksheetFunction.CountIf(.Columns(7), "reject") End With**  $sMsg =$  "The mean or average of  $22x1000$  runs:" & **vbCr sMsg = sMsg & "all products: " & vbTab & FormatNumber(pAvgProd, 4) & vbCr sMsg = sMsg & "all samples: " & vbTab & FormatNumber(pAvgSampl, 4) & vbCr sMsg = sMsg & "all sample counts: " & vbTab & FormatNumber(pAvgCount, 4) & vbCr**  $sMsg = sMsg \&$  "number of rejects: "  $\&$  vbTab  $\&$ **iReject MsgBox sMsg**

### **End Sub**

## **Chapter 73: Waiting Time Simulation What the simulation does**



We simulate here the flow of patients in something like a walk-in clinic. Based on experience, we know the probabilities of patients coming in with 5, 10, or 15 minutes between arrivals (B2:C4). We also know the probabilities that the treatment takes 5, 10, or 15 minutes (F2:G4). Let's assume there are usually 10 patients in the morning (which we won't simulate, though). And there is only one nurse or doctor in the clinic.

Now we can simulate the flow of patients through the system (A7:G16). The chart shows how visit times can vary randomly. Since there is much volatility involved, we repeat this process some 100 to 1,000 times through the help of a VBA array in the background, so we can calculate what the average maximum visit time is, based on waiting time and treatment time. The simulation reports its results in a *MsgBox*.

#### **What you need to know**

To randomly assign arrival times and treatment times, we need an extra column in front of the two probability tables shown on top of the sheet. These two columns must start at 0 and then cumulatively increase, so we can use VLOOKUP to assign these times in a random manner.

Other formulas on the sheet are shown in the screen shot on the next page.

```
Sub WaitingTime()
  Dim oRange As Range, iMaxVisitTime As Integer,
arrVisTime() As Integer, i As Integer, n As Long
  Set oRange = Range("B7:G16")
  With oRange
    .ClearContents
    .Columns(1).Formula =
"=VLOOKUP(RAND(),$A$2:$B$4,2,TRUE)"
    .Columns(2).Formula = "=SUM($B$7:B7)"
    .Columns(3).Cells(1, 1).Formula = "=C7"
    Range("D8:D16").Formula =
"=IF(C8<F7,F7,F7+(C8-F7))"
    .Columns(4).Formula =
"=VLOOKUP(RAND(),$E$2:$F$4,2,TRUE)"
    .Columns(5).Formula = "=D7+E7"
    .Columns(6).Formula = "=F7-C7"
    .Calculate
  End With
  n = InputBox("How many runs (100-1000)?"
, , 100)
  ReDim arrVisTime(0 To n - 1)
  For i = 0 To n - 1Range("B7:G19").Calculate
```
### **iMaxVisitTime = Range("G19") arrVisTime(i) = iMaxVisitTime**

#### **Next i**

**MsgBox "After " & n & " runs, the average of " & vbCr & \_**

**"maximum wait times is " & WorksheetFunction.Average(arrVisTime) & " mins." End Sub**



## **Chapter 74: Project Delays What the simulation does**



Here we have a sequence of tasks that start at a certain day, have a certain duration, and then end, to be followed by the next task. So the entire project is supposed to be finished on the date shown in cell E11.

Usually, however, there are random changes in the duration (column F) —say, up to 2 days shorter or longer than anticipated. Such random changes would obviously affect the end date of the total project. In cell H11, we calculate what the actual end date of the project would be.

We run this project some 100 times in a *Data Table* (G14:H151), so we can calculate what on average the "real" end date of the project would be after random changes in duration per task. We then calculate how the final end dates for each run are distributed in a frequency chart (in the right lower corner of the sheet).

#### **What you need to know**

There are some fomulas on this sheet (see screen shot on the next page). The only new function used in the VBA code is Excel's DAYS function. It returns the number of days between two dates, where the first argument indicates the end date, and the  $2<sup>nd</sup>$  argument the start date. If the number of days is negative, then the end date is earlier than the start date.

The way Excel handles dates may need some explanation. Excel stores dates as sequential serial numbers so that they can be used in calculations. By default, Jan 1, 1900 is serial number 1, and January 1, 2008 is serial number 39448 because it is 39447 days after January 1, 1900. This number can also have decimals to indicate the time of the day. So basically 39447 is January 1, 2008 at 12 AM, and 39447.5 is 12 PM on that day.

The chart in the upper right of the sheet is a so-called Gantt chart. In Excel, it is a *stacked* bar chart with two series of values, of which the first series, or stack, has no fill color or line color, so it is actually invisible. We have actually 2 charts here. They both use B2:B11 as categories. One is based on series G2:G11 (invisible) and series F2:F11. The other one is plotted from series C2:C11 (invisible) and series D2:D11. The second chart has a plot area with no fill, so you can lay it over the first one with a slight offset down.

```
Sub ProjectDelays()
  Dim oTable As Range, i As Integer, sMsg As String,
dAvgDate As Date, iOff As Long
  With Range("E2:H11")
    .ClearContents
    .Columns(1).Formula = "=C2+D2-1"
    .Columns(2).Formula =
"=D2+RANDBETWEEN(-2,2)"
    .Columns(3).Formula = "=IF(ROW()=2,C2,
H1+1)"
    .Columns(4).Formula = "=G2+F2-1"
  End With
  Set oTable = Range("G14").CurrentRegion
  Range("H15:H115").ClearContents
  oTable.Table , Range("F13")
  Range("E14:E33") =
WorksheetFunction.Frequency(oTable.Columns(2),
Range("D14:D33"))
  'OR: Range("E14:E33").FormulaArray =
"=FREQUENCY(R14C8:R115C8,R14C4:R33C4)"
  dAvgDate =
Round(WorksheetFunction.Average(oTable.Columns(2)),
```
**0)**

**iOff = WorksheetFunction.Days(dAvgDate, Range("E11")) '+ IIf(iOff >= 0, 1, -1) If**  $dAvgDate = Range("E11")$  Then  $iOff = 0$ **sMsg = "Average finish date of 100 runs: " & FormatDateTime(dAvgDate, vbShortDate) & vbCr sMsg = sMsg & "On average " & Abs(iOff) & " days " & IIf(iOff >= 0, "later" , "earlier") sMsg = sMsg & " than " & Range("E11") MsgBox sMsg End Sub**



# **VII. FINANCE**

## **Chapter 75: Buy or Sell Stock?**

#### **What the simulation does**



Based on the performance of a certain stock, we want to anticipate its value the next day, so we can decide whether to buy or to sell.

Since there is much uncertainty involved, we need to consider the mean and standard deviation of its past history, and based on this information, the macro projects some 10,000 normally distributed values in order to somewhat harnass volatility.

Part of the decision is determined by how far we want to go back in history. So the macro goes back in the entire history shown in column A by steps of 5 days, and then makes a provisional decision as to either buy or sell for each step. This decision is obviously debatable. The macro uses the following rule: if the average of 10,000 runs is greater than 0.01 times the SD, go for "buy"; if it is less than 0.01 times the SD, go for "sell." This rule can be adjusted at any time, of course.

Finally, the macro displays the verdict of all periods and lets the user determine which decision to make based on this information.



#### **What you need to know**

The background calculations are stored in an array with 10,000 elements. The average and standard deviation are based on those 10,000 values. There will always be volatility (and unexpected events!), but they can be better harnassed by using huge amounts of numbers.

```
Sub BuySell()
  Dim i As Long, oCurReg As Range, oRange As
Range, iOffset As Long, n As Long
  Dim pAvg As Double, pSD As Double, arrVal() As
Double, sMsg As String, sVerdict As String
  Dim pAvgAvg As Double, pLatestVal As Double
  Set oCurReg = Range("A1").CurrentRegion
  With oCurReg
    iOffset = oCurReg.Rows.Count
    pLatestVal = .Cells(iOffset, 2)
    For i = iOffset To 2 Step -5
       Set oRange = .Range(Cells(iOffset - i + 1, 2),
Cells(iOffset, 2))
       pAvg = WorksheetFunction.Average(oRange)
       pSD = WorksheetFunction.StDev(oRange)
       ReDim arrVal(0 To 9999)
       For n = 0 To 9999
         arrVal(n) =
WorksheetFunction.Norm_Inv(Rnd, pAvg, pSD)
      Next n
       pAvgAvg =
WorksheetFunction.Average(arrVal)
```
$s\text{Vertical} + p\text{S}$  **=**  $\text{If}(p\text{AvgAvg} > (p\text{LatestVal} + p\text{S} \text{D}^*)$ **0.01), "buy" , IIf(pAvgAvg < (pLatestVal - pSD \* 0.01), "sell" , "-"))**

**sMsg = sMsg & "Latest " & i & vbTab & pAvgAvg & vbTab & sVerdict & vbCr Next i**

**MsgBox sMsg**

**End With**

**End Sub**



## **Chapter 76: Moving Averages What the simulation does**



This file has 3 sheets and 3 similar macros for "moving averages" and "exponential smoothing." It simulates what happens when we reduce the amount of "noise" with a certain factor.

### **What you need to know**



**Sub MovingAverage() Dim oChart As Chart, oSelect As Range, oSeries As Series Dim oTrendCol As Trendlines, oTrend As Trendline Sheet12.Activate: Range("A1").Select Set oSelect = ActiveCell.CurrentRegion : Set oChart = Charts.Add oChart.SetSourceData oSelect oChart.ChartType = xlXYScatterLines oChart.HasLegend = False: oChart.HasTitle = False oChart.Axes(xlCategory).HasMajorGridlines = True oChart.Location xlLocationAsNewSheet Set oSeries = oChart.SeriesCollection(1) Set oTrendCol = oSeries.Trendlines Set oTrend = oTrendCol.Add(xlMovingAvg, , InputBox("Period" , , 3)) oTrend.Border.LineStyle = xlDot : Application.DisplayAlerts = False If MsgBox("Delete?" , vbYesNo) = vbYes Then oChart.Delete Application.DisplayAlerts = True End Sub**

```
Sub AvgSmoothed()
  Dim i As Integer, oRange As Range
  Sheet10.Activate: Range("A1").Select
  i = InputBox("Number of intervals to be
averaged"
, , 2)
  With Range("C1")
    .Value = "Avg on " & i
    Set oRange = .Range(Cells(2, 1),
Cells(.CurrentRegion.Rows.Count, 1))
    oRange.Clear
    Set oRange = .Range(Cells(i + 1, 1),
Cells(.CurrentRegion.Rows.Count, 1))
    oRange.FormulaR1C1 = "=AVERAGE(RC[-1] :
R[-" & i - 1 & "]C[-1])"
    oRange.NumberFormat = "0.00"
  End With
End Sub
```

```
Sub Damping()
```
**Dim pDamp As Double, oRange As Range Sheet11.Activate: Range("A1").Select pDamp = InputBox("Damping factor" , , 0.15) With Range("C1")**

**.Value = pDamp : .Offset(1, 0).Formula = "=B2"**

**Set oRange = .Range(Cells(3, 1),**

**Cells(.CurrentRegion.Rows.Count, 1)) oRange.Clear Set oRange = .Range(Cells(3, 1), Cells(.CurrentRegion.Rows.Count, 1)) oRange.Formula = "=\$C\$1\*B2+(1-\$C\$1)\*C2" oRange.NumberFormat = "0.00": oRange.Font.Bold = True End With End Sub**

# **Chapter 77: Automatic Totals and Subtotals**

### **What the simulation does**



At the bounds of the database A1:E13, the first macro, *Totals*, adds summaries of your choosing—SUM, STDEV, MEDIAN, and so on. The second macro, *SubTotals*, creates subtotals and lets the users determine which columns they like to use for sorting and summing. Then it offers the option to copy this summary of subtotals to a new sheet.

### **What you need to know**

The macro assumes that your database does not have formulas in it, so it can use the VBA property *HasFormula* to determine where the database ends.

### **What you need to do**

### **Sub Subtotals()**

**Dim oSelect As Range, oSort As Range, oTotal As Range, oWS As Worksheet**

**Sheet1.Activate: Range("A1").Select**

**With ActiveCell.CurrentRegion Set oSort = Application.InputBox("Sort by Label" , , "G1" , , , , , 8) .Sort oSort, xlAscending, , , , , , xlYes Set oTotal = Application.InputBox("SUM by Label" , , "D1" , , , , , 8) .Subtotal oSort.Column, xlSum, Array(oTotal.Column) Set oWS = ActiveSheet ActiveSheet.Outline.ShowLevels 2 '[row-levels], [col-levels] Set oSelect = Application.InputBox("Which range to copy" , , Range("D1:D24,G1:G24").Address, , , , , 8) Set oSelect = oSelect.SpecialCells(xlCellTypeVisible) Set oWS = Worksheets.Add(, ActiveSheet) oSelect.Copy Cells(1, 1) : oSelect.Font.Color = vbRed oSelect.Rows(1).Font.Color = vbBlack .EntireColumn.AutoFit: Cells().EntireColumn.AutoFit Application.CutCopyMode = False ; .Range("A1").RemoveSubtotal End With End Sub**

```
Sub Totals()
  Dim r As Long, c As Long, sOper As String,
oRange As Range, oCurReg As Range, n As Integer
  Sheet2.Select: Range("A1").Select
  With ActiveCell.CurrentRegion
     r = .Rows.Count: c = .Columns.Count
    If .Cells(r, c).HasFormula = False Then
.BorderAround , xlThick
    sOper =
InputBox("SUM/AVERAGE/MAX/STDEV/MODE/ME),
"SUM")
     sOper = UCase(sOper)
    Do Until .Cells(r, c).HasFormula = False
       r = r - 1: c = c - 1: n = n + 1Loop
    If n > 0 Then
       If MsgBox("Add " & sOper & " (instead of
replace)?"
, vbYesNo) = vbYes Then
         r = r + n: c = c + nEnd If
    End If
     \text{.Cells}(1, c + 1) = \text{sOper:} \text{.Cells}(r + 1, 1) = \text{sOper}Set oRange = .Range(.Cells(r + 1, 2), .Cells(r + 1, 2))c))
     oRange.FormulaR1C1 = "=" & sOper & "
(R2C:R[-" & n + 1 & "]C)"
```
**oRange.NumberFormat = .Cells(r,**

**c).NumberFormat**

Set  $oRange = .Range(.Cells(2, c + 1), .Cells(r + 1))$  $1, c + 1)$ 

**oRange.FormulaR1C1** =  $"=" ="$  & **sOper** & " **(RC2:RC[-1])"**

**oRange.NumberFormat = .Cells(r, c).NumberFormat**

**If MsgBox("Delete summary?" , vbYesNo) = vbYes Then**

**With Range("B2").CurrentRegion For r = .Rows.Count To 1 Step -1 If .Cells(r, 2).HasFormula Then .Rows(r).ClearContents Next r** For  $c = .$  **Columns. Count** To 1 Step  $-1$ **If .Cells(2, c).HasFormula Then .Columns(c).ClearContents Next c End With End If End With End Sub**



# **Chapter 78: Fluctuations of APR What the simulation does**



Let's pretend we are trying to predict what the total return would be over a period of years if the initial deposit is fixed and the annual percentage rate (APR) is fluctuating. So this sheet calculates how a fixed deposit compounds over a specific number of years with a fluctuating APR.

We use three tables to set up this calculation. In the left table, we set up our parameters and use a simple calculation of return without considering any volatility. In the middle table, we simulate how APR could fluctuate during the time period—in this case 30 years—if the volatility is 0.3% (cell B4). Since this middle table represents only one of the many possible outcomes, we need to run additional scenarios to model fluctuations in return. In the *Data Table* to the right, we run these additional scenarios of the middle table some 25 times.

The macro summarizes the results of 25 runs for what your savings would be after 30 years—minimum, average, and maximum.

### **What you need to know**



Compounding a certain amount of

money is based on a very simple formula: the starting amount multiplied by (1+APR) raised to the power of the number of years—or:  $X^*(1+APR)$ <sup> $\gamma$ </sup>yrs. This is the formula used in the left table.

The middle table uses the function NORMINV to simulate fluctuations in the annual percentage rate each year.

The *Data Table* to the right runs the end result of the middle table at least 25 times by using the array formula  $\{=\text{TABLE}(0, G1)\}$ —pointing to any empty cell outside the table (e.g., cell G1). The more runs, the more reliable the outcome is.

The chart is linked to columns D:F. One curve, the upward one, is for the compounding savings amount; the other curve shows APR fluctuations.

### **Option Explicit**

```
Sub Savings()
  Dim oRange As Range, oTable As Range,
oFormulas As Range, n As Integer
  Dim sMsg As String, sMin As String, sMax As
String, sAvg As String
  Set oRange = Range("D1").CurrentRegion
  oRange.ClearContents
  Set oTable = Range("H1").CurrentRegion
  oTable.ClearContents
  n = InputBox("For how many years (max of 30)?"
,
, 30)
  If n > 30 Then Exit Sub Else Range("B2") = nSet oRange = Range("D1").Range(Cells(1, 1),
Cells(n + 1, 3))
  oRange.Cells(1, 1) = "Year": oRange.Cells(1, 2) =
"APR": oRange.Cells(1, 3) = "Savings"
  Set oFormulas = oRange.Range(Cells(2, 1), Cells(n
+ 1, 3))
  With oFormulas
    .Columns(1).Formula = "=ROW(A1)"
    .Columns(2).Formula =
```
**"=NORMINV(RAND(),\$B\$3,\$B\$4)"**

**.Columns(3).Cells(1, 1).Formula = "=\$B\$1\* (1+E2)^D2" .Columns(3).Range(Cells(2, 1), Cells(n, 1)).Formula = "=F2\*(1+E3)" oTable.Cells(1, 2).Formula = "=" & .Columns(3).Cells(n, 1).Address End With Set oTable = Range("H1").Range(Cells(1, 1), Cells(26, 2)) oTable.Table , Range("G1") With oTable sMin = FormatCurrency(WorksheetFunction.Min(.Columns(2)), 2)**  $sAvg =$ FormatCurrency(WorksheetFunction.Average(.Column

**2)**

**sMax =**

**FormatCurrency(WorksheetFunction.Max(.Columns(2)), 2)**

**End With**

**sMsg = "Minimum savings: " & vbTab & sMin & vbCr**

**sMsg = sMsg & "Average savings: " & vbTab & sAvg & vbCr**

**sMsg = sMsg & "Maximum savings: " & vbTab & sMax & vbCr**

## **MsgBox sMsg End Sub**



# **Chapter 79: Net Present Value What the simulation does**



When you have three scenarios (likely, best, worst) for your costs, benefits, and growth rate (in A1:D4), you probably want a random outcome between the extremes of best and worst. Then ultimately you want to calculate the net present value (NPV) of your cash flows (in cell K10).

Here is some terminology. Having projected a company's free cash flow for the next five years, you want to figure out what these cash flows are worth today. That means coming up with an appropriate discount rate which you can use to calculate the net present value (NPV) of the cash flows. A discount rate of 5% is used in column I (see screen shot below).

The most widely used method of discounting is exponential discounting, which values future cash flows as "how much money would have to be invested currently, at a given rate of return, to yield the cash flow in the future."

After running your 5 year projection (H1:K8), the simulation repeats this with some 10,000 runs ithrough a VBA array. The simulation calculates the average NPV and its standard deviation in cell K10 and K11 for the latest run. The *MsgBox* keeps track of the results for previous runs.

Based on this information, you may want to find out what the

distribution of NPV values would be given the average of K10 and the standard deviation of K11. This is done below them in cells J17:K51, ranging from 2.5% to 97.5%. The graph shows the results, with the "average" featuring at 50% (see screen shot on the next page).

## **What you need to know**



### **Option Explicit**

```
Sub NPV()
  Dim i As Long, n As Long, pNPV As Double,
arrNPV() As Double, sMsg As String
  Dim pSum As Double, pAvg As Double, pSD As
Double, sAvg As String, sSD As String
  n = InputBox("How many iterations (1000 to
10,000)?"
, , 1000)
  sMsg = "After " & n & " calculations:" & vbCr
  Do
    ReDim arrNPV(0 To n - 1)
    For i = 0 To n - 1Range("A1:K8").Calculate
      arrNPV(i) = Range("K8")
      pSum = pSum + arrNPV(i)Next i
    pAvg = pSum / n: sAvg =FormatCurrency(pAvg, 2): pSum = 0pSD = WorksheetFunction.StDev_S(arrNPV):
sSD = FormatCurrency(pSD, 2)
    Range("K10") = sAvg: Range("K11") = sSD
    sMsg = sMsg & "Mean NPV:" & sAvg & vbTab
& vbTab & "SD NPV:" & vbTab & sSD & vbCr
```
## **Loop Until MsgBox(sMsg & vbCr & "Repeat?" , vbYesNo) = vbNo End Sub**



# **Chapter 80: A Loan with Balance and Principal**

**What the simulation does**



This is basically a simple macro. We enter estimates for loan amount, term of the loan, and annual percentage rate through an *InputBox* three times. Then the macro calculates, on a new sheet, the monthly payments, the total of payments, and the total of interest.

Since there is not much "uncertainty" involved—all variables are fixed—don't expect any volatility here.

## **What you need to know**

We need the Excel function PMT. Its syntax is: PMT(rate, nper, pv, [fv], [type]). It calculates the payment for a loan (*pv* or present value) based on constant monthly payments and a constant interest rate (*rate* per month) for a certain period of time (*nper* in months). The last two other arguments we can ignore here. Since we are dealing here with months, make sure to divide rate (APR) by 12, and multiply the number of years by 12. Be aware PMT returns a negative value (a value that is owed), unless you enter the present value as a negative amount.

In addition, we need the Excel functions IPMT to calculate the interest, and PPMT to calculate the principal. They have basically the same syntax. All formulas are shown here below.



### Here is the new sheet for \$50,000 and an APR of 4.5%:



```
Sub Loan()
  Dim cLoan As Currency, pAPR As Double,
iDuration As Integer, i As Integer
  Dim oWS As Worksheet
  cLoan = InputBox("Loan amount"
, , 65000)
  pAPR = InputBox("Fixed APR"
, , 0.056) / 12
  iDuration = InputBox("Number of years"
, , 30) *
12
  Set oWS = Worksheets.Add(, ActiveSheet)
  oWS.Name = cLoan & "-" &
FormatPercent(pAPR, 2) & "-" & iDuration
  Cells(1, 1) = "Period"
  Cells(1, 2) = "Month"
  Cells(1, 3) = "Balance"
  Cells(1, 4) = "Monthly"Cells(1, 5) = "Interest"
  Cells(1, 6) = "Principal"Cells(1, 7) = "Cum. Interest"
  Cells(1, 8) = "Cum. Principal"
  Application.Cursor = xlWait
  With Range("A1")
    For i = 1 To iDuration
       .Offset(i, 0).Formula = "=ROW()-1"
       '=DATE(YEAR(B5),MONTH(B5)+1,1)
```
**.Offset(i, 1).Formula = "=DATE(YEAR(TODAY()), MONTH(TODAY())+" & i & " ,1)" .Offset(i, 1).NumberFormat = "mmm-yy"**  $' =$ Loan and then  $=$ C3+F3 **.Offset(i, 2).FormulaR1C1 = IIf(i = 1, cLoan, "=R[-1]C3+R[-1]C6") '=PMT(pAPR,iDuration,cLoan) .Offset(i, 3).Formula = "=PMT(" & pAPR & " , " & iDuration & " , " & cLoan & ")" '=IPMT(pAPR,period,iDuration,cLoan) .Offset(i, 4).FormulaR1C1 = "=IPMT(" & pAPR & " ,RC1, " & iDuration & " , " & cLoan & ")" '=PPMT(pAPR,period,iDuration,cLoan) .Offset(i, 5).FormulaR1C1 = "=PPMT(" & pAPR & " ,RC1, " & iDuration & " , " & cLoan & ")" '=SUM(\$E\$2:E2) .Offset(i, 6).FormulaR1C1 = "=SUM(R2C5:RC5)" '=SUM(\$F\$2:F2) .Offset(i, 7).FormulaR1C1 = "=SUM(R2C6:RC6)" Next i End With Cells.EntireColumn.AutoFit Application.Cursor = xlDefault End Sub**

# **Chapter 81: S&P500 Performance What the simulation does**



Based on data from 1950 to 2012, we have an average daily return value (in cell B2) and a daily standard deviation value (in cell B3) for S&P500 performance. This information we use to calculate what the percentage would be at the end of a week (in cell F6).

Then we repeat this volatile calculation some 10,000 times with a VBA array of 10,000 elements. There is going to be quite some volatility, but because we have a reasonable sample size now, we can find a more reliable average and SD through the array of 10,000 values. We can repeat this several times, while the *MsgBox* keeps track of the results. That may give is a bit more certainty in the midst of uncertainties.

### **What you need to know**



The historical values in column B are used in column E with a NORMINV Excel function.

In column F, we calculate the cumulative end-of-week result: (daily % +1) \* (previous cumulative  $\%$  + 1) – 1.

**Option Explicit**

```
Sub Performance()
  Dim oRange As Range, arrVals() As Double, i As
Long, n As Integer
  Dim pAvg As Double, pSD As Double, sMsg As
String
  Do
    ReDim arrVals(0 To 9999)
    n = n + 1For i = 0 To 9999
       Range("E2:F6").Calculate
       \text{array}(i) = (Cells(6, 5) + 1) * (Cells(5, 6) + 1)- 1
    Next i
    pAvg = WorksheetFunction.Average(arrVals)
    pSD = WorksheetFunction.StDev(arrVals)
    sMsg = sMsg & "Average: " &
FormatPercent(pAvg, 3) & vbTab & _
            "SD: " & FormatPercent(pSD, 3) & vbCr
    MsgBox n & " x 10,000 runs:" & vbCr & sMsg
  Loop Until MsgBox("Another run?"
, vbYesNo) =
vbNo
End Sub
```


# **Chapter 82: Stock Market What the simulation does**



The left section of this sheet contains hard-coded data, comparing past S&P 500 values (C) with the past values of a traditional portfolio (B).

The right section analyses this information from the most recent month  $(12/1/06)$  down to the previous month  $(11/1/06)$  and much further back in time, if needed. The overview "grows" back in time if you copy its first row down as far as you want to go back in history.

In addition, when new records are added at the bottom of the left section, the first row in the right section will automatically update the history from the most recent data down.

The macro does all of this automatically, once you decide on the number of rows "back in history."

#### **What you need to know**

The only new function is COUNTA. The COUNTA function works

like COUNT, but it also counts cells with text in them, such as the headers above each column.

As said before, the function INDEX is a more sophisticated version of VLOOKUP. It looks in a table at a certain row position and a certain column position. It uses this syntax: *INDEX(table, row#, col#).* Whereas VLOOKUP works only with column numbers, INDEX also uses row numbers, which is very important when we want to look at a record that is located, for instance, 3 or 12 rows above another record (like in columns G and J).

This time we use the function ROW again, but for a different reason to make the month go down:  $row# - ROW(Al) + I$ . Each time we copy that formula one row down, the formula subtracts one more row:  $-$  ROW(A2), then –  $ROW(A3)$ , and so forth.

### **Option Explicit**

```
Sub Stock()
  Dim oRange As Range, oTable As Range
  Dim vArr As Variant, i As Long, n As Long
  vArr = Array("Month"
,
"Traditional"
,
"Trad-
3mo"
,
"BenchMark"
,
"S&P500"
,
"S&P-3mo"
,
"BenchMark")
  Set oRange = Range("A1").CurrentRegion
  Set oTable = Range("E1").CurrentRegion
  oTable.Clear
  Range("E1:K1") = vArr
  n = InputBox("How many months?"
, , 12)
  Set oTable = Range(Cells(2, 5), Cells(1 + n, 11))With oTable
    .Columns(1).Formula =
"=INDEX($A:$C,COUNTA($A:$A)-ROW(A1)+1,1)"
    .Columns(2).Formula =
"=INDEX($A:$C,COUNTA($A:$A)-ROW(B1)+1,2)"
    .Columns(3).Formula =
"=INDEX($A:$C,COUNTA($A:$A)-ROW(C1)+1-
3,2)"
    .Columns(4).Formula = "=F2/G2-1"
    .Columns(5).Formula =
```

```
"=INDEX($A:$C,COUNTA($A:$A)-ROW(A1)+1,3)"
    .Columns(6).Formula =
"=INDEX($A:$C,COUNTA($A:$A)-ROW(A1)+1-
3,3)"
```
**.Columns(7).Formula = "=I2/J2-1"**

**For i = 2 To .Columns.Count**

**.Columns(i).Cells.NumberFormat = "0.00" Next i**

**.Columns(1).Cells.NumberFormat = "m/d/yy" .BorderAround , xlThick**

**.Cells.Font.Bold = True**

**End With End Sub**



# **Chapter 83: Stock Volatility What the simulation does**



There is much uncertainty on the stock market. Monte Carlo simulations are a great tool to get a bit more certainty in the midst of numerous uncertainties.

The information needed is in the left top corner. The expected return in cell B3 is based on history: an expected return of 10% divided by 250 trading days per year. The volatility in cell B4 is also based on past performance: an annualized volatility of 25% divided by the square root of trading days per year.

The simulation plots in column B the changes in stock value up to a maximum of 250 trading days. To harness our uncertainty a little better, the macro runs at least 1,000 to 10,000 iterations to beat volatility. This is to ensure that we have a statistical chance of getting sufficient outliers (extreme values) to make the variance analysis meaningful.

The simulation does all of this without a *Data Table*—which saves us some "overhead costs." Instead it uses a VBA array of 10,000 entries. It finds the value after the first 10 days, repeats this 10,000 times, and stores these 10,000 values in the array; the average of these values is entered in cell F20. Then it does this again, but now for 30 days (G20), and so on, up to 250 days at the most. The chart shows the results of one run (columns A:C) and of 10,000 runs (F20:R20).

### **What you need to know**

The sheet itself has only formulas in rows A:C (column C is solely for a baseline in the chart). The formulas from row 7 down are generated by the macro.



**Option Explicit**

```
Sub Volatility()
  Dim oRange As Range, i As Long, n As Long, c As
Integer, j As Integer
  Dim arrVals() As Double, oTotals As Range
  Set oRange = Range("A7").CurrentRegion
  oRange.ClearContents
  n = InputBox("How many days ahead (10-250)?"
, ,
250)
  If n > 250 Then Exit Sub Else n = n + 1Range("B2").Activate
  With oRange
    .Cells(1, 2) = "value": .Cells(1, 3) = "base":
.Cells(2, 2).Formula = "=B2"
    .Range(Cells(2, 1), Cells(n, 1)).Formula =
"=ROW(A1)"
    .Range(Cells(3, 2), Cells(n, 2)).Formula =
"=B7+B7*($B$3+$B$4*NORMINV(RAND(),0,1))"
    .Range(Cells(2, 3), Cells(n, 3)).Formula =
"=$B$7"
  End With
  Set oTotals = Range(Cells(20, 6), Cells(20, 18))
```
**oTotals.ClearContents**

**With oTotals For c = 10 To n Step 20 ReDim arrVals(0 To 9999) For i = 0 To 9999 oRange.Calculate arrVals(i) = WorksheetFunction.VLookup(c, oRange.Range(Cells(2, 1), Cells(n, 2)), 2, True) Next i**  $j = j + 1$  $\mathbf{Cells}(1, j) =$ **WorksheetFunction.Average(arrVals) Calculate DoEvents Next c End With End Sub**


### **Chapter 84: Return on Investment What the simulation does**



In this simulation, we want to calculate our return on an investment, but also take into consideration the cost of inflation and taxes for our investment.

The sheet simulates the return on investment (ROI) when buying bank CDs for a certain amount of money  $(B1)$ , with the assumption that these have a fixed interest rate (B2), a certain fixed inflation rate (B4), and that we are taxed at 25% for CD profits (B3). We also assume that we want to keep our CD value at its original power by, at least theoretically, putting in more money each year (B8). We do all of this for a certain number of years (B6).

The core part of this simulation is calculating the return on investment (ROI) in cell B11, based on all the cells above it. The macro also creates a *Data Table* to be placed in D6:K13. This table shows at what return rates and inflation rates our investment becomes profitable. It uses a link to that calculation in B11. Based on this calculation, the two-dimensional *Data Table* shows what the ROI is for a range of changes in CD interest and in inflation rate.

### **What you need to know**



**Option Explicit**

**Sub CDReturn() Dim i As Integer, oTable As Range Range("B6:B11").ClearContents Range("D6").CurrentRegion.Clear i = InputBox("For how many years?" , , 10) Range("B6") = i Range("B7").Formula = "=B1\*(1-B4)^B6" Range("B8").Formula = "=B1-B7" Range("B9").Formula = "=B1\*B2\*B6" Range("B10").Formula = "=B9\*B3" Range("B11").Formula = "=(B9-B8- B10)/(B1+B8)" Set oTable = Range(Cells(6, 4), Cells(13, 11)) With oTable .Cells(1, 1).Formula = "=B11" .Range(Cells(1, 2), Cells(1, 8)).Formula = "=COLUMN(D1)/100" .Range(Cells(1, 2), Cells(1, 8)).Borders(xlEdgeBottom).Weight = xlMedium .Range(Cells(2, 1), Cells(8, 1)).Formula = "=ROW(A4)/100" .Range(Cells(2, 1), Cells(8,**

### **1)).Borders(xlEdgeRight).Weight = xlMedium .Table Range("B2"), Range("B4") .Cells.NumberFormat = "0.00%;[Red] -0.00%" .Cells(8, 1).Offset(1, 0) = "inflation rate" .Cells(1, 8).Offset(0, 1) = "CD interest" End With End Sub**



### **Chapter 85: Value at Risk What the simulation does**



*Value-at-Risk*, or *VaR*, is the potential maximum loss in a portfolio (and a certain standard deviation) at a given confidence interval over a given period of time (which could be a day, a month, or a year). We calculate the minimum expected return, which is done with the function NORMINV in B7 (although investments do not always follow a normal distribution!).

### **What you need to know**

The *VaR* is for a single time period (say, one trading day). To convert that value to a longer range, simply multiply the *VaR* by the square root of the number of single periods within the longer period. Say, you calculated the *VaR* for one day and want it for a month, use the number of trading days in a month, say 22, and multiply your *VaR* with  $\sqrt{22}$ .

*VaR* is not your worst case loss. At a confidence level of 95%, the *VaR* is your minimum expected loss 5% of the time—not your maximum

### expected loss. So don't be surprised.



```
Sub TableBox()
```
**Dim cPort As Currency, pAvg As Double, pSD As Double, pConf As Double**

**Dim sStart As String, i As Integer, oRange As Range**

**Range("A6").CurrentRegion.ClearContents cPort = InputBox("Portfolio" , , Cells(1, 2)):**

 $Cells(1, 2) = cPort$ 

**pAvg = InputBox("Average" , , Cells(2, 2)):**

 $Cells(2, 2) = pAvg$ 

**pSD = InputBox("Standard Deviation" , , Cells(3, 2)): Cells(3, 2) = pSD**

**pConf = InputBox("Confidence Level" , , 0.95):**  $Cells(4, 2) = pConf$ 

```
sStart = InputBox("Start table in"
, ,
"A6")
```
**If Range(sStart) <> "" Then**

**Range(sStart).CurrentRegion.Delete**

**With Range(sStart)**

**.Offset(0, 0) = "Confidence": .Offset(0, 1) = "Min. return"**

**.Offset(0, 2) = "New value": .Offset(0, 3) = "Value at risk"**

**.Offset(0, 4) = "Monthly VaR"**  $For i = 1, To 10$ 

**.Offset(i, 0) = FormatPercent(pConf - (i - 1) \* 0.05, 0) Next i .Offset(1, 1).Formula = "=NORM.INV(1- B4,B2,B3)" .Offset(1, 2).Formula = "=B1\*(" & .Offset(1, 1).Address & "+1)" .Offset(1, 3).Formula = "=B1-" & .Offset(1, 2).Address .Offset(1, 4).Formula = "=" & .Offset(1, 3).Address & "\*SQRT(22)" Set oRange = Range(.Offset(1, 0), .Offset(10, 4)) ; oRange.Table , Range("B4") oRange.Columns(2).NumberFormat = "0.00" oRange.Columns(3).NumberFormat = "\$#,##0.00\_);[Red](\$#,##0.00)" oRange.Columns(4).NumberFormat = "\$#,##0.00\_);[Red](\$#,##0.00)" oRange.Columns(5).NumberFormat = "\$#,##0.00\_);[Red](\$#,##0.00)" Cells.Columns.AutoFit End With 'Conditional Formatting with Bars (only in later versions of Excel) With oRange.Columns(5) Dim oBar As Databar .Select**

**Set oBar = Selection.FormatConditions.AddDatabar oBar.MinPoint.Modify newtype:=xlConditionValueAutomaticMin oBar.MaxPoint.Modify newtype:=xlConditionValueAutomaticMax oBar.BarFillType = xlDataBarFillGradient oBar.Direction = xlContext oBar.NegativeBarFormat.ColorType = xlDataBarColor oBar.BarBorder.Type = xlDataBarBorderSolid oBar.NegativeBarFormat.BorderColorType = xlDataBarColor oBar.AxisPosition = xlDataBarAxisAutomatic End With Range("B1").Select End Sub**

### **Chapter 86: Asian Options What the simulation does**



This simulation concerns an Asian option, which is valued by determining the average underlying price over a period of time. Simply put, an option contract is an agreement between two people that gives one the right to buy or sell a stock at some future date for some preset price. To price an Asian option by its mean, we need to know, at least to some degree, the path that the stock will take as time progresses.

An Asian option (or "average value option") is a special type of option contract. The payoff is determined by the average underlying price over some pre-set period of time. This is different from the usual European options and American options which are valued at the expiration of the contract.

One advantage of Asian options is that these reduce the risk of market manipulation. Another advantage is the relatively low cost of Asian options. Because of the averaging feature, Asian options reduce the volatility inherent in the option; therefore, Asian options are typically cheaper than European or American options.

#### **What you need to know**

To simplify things, we will track the stock over 5 years in yearly increments (B7:H7). To derive the average value in I7, we multiply the initial stock price (column B) by the first randomly generated log-normal

number (with the functions EXP and NORMINV in C7:H7) to obtain a value for year 1 (I won't go into further explanations). The result must be multiplied by the second randomly generated number (column C), and so on.

To make the predictions more reliable, we give it 10,000 runs in this simulation. This is done with a VBA array (so we won't need a *Data Table*). For each trial, the simulation recalculates row 7 and stores the payoff amount (J7) for each run in an array of 10,000 elements. Then the simulation calculates the average payoff and its standard deviation in the array.

The Standard Error of the mean (SE) is the Standard Deviation (SD) divided by the square root of the number of cases. A confidence level of 95% evaluates to the mean  $\pm$  (1.96  $*$  SE).

The macro reports in a *MsgBox* what the payoff amount would be with 95% confidence.

**Option Explicit**

```
Sub AsianOption()
  Dim arrPayoffs() As Double, i As Long
  Dim pAvg As Double, pSD As Double, pSE As
Double
  Dim sLower As String, sUpper As String, sAvg As
String, sSD As String
  ReDim arrPayoffs(0 To 99999)
  For i = 0 To 99999
    Range("B7:J7").Calculate
    arrPayoffs(i) = Range("J7")
  Next i
  pAvg = WorksheetFunction.Average(arrPayoffs)
  pSD = WorksheetFunction.StDev(arrPayoffs)
  pSE = pSD / Sqr(100000)
  sLower = FormatCurrency(pAvg - (1.96 * pSE), 2)
  sUpper = FormatCurrent(pAvg + (1.96 * pSE), 2)MsgBox "After 100,000 runs, we have " & vbCr &
"95% confidence that the payoff is:" & _
      vbCr & "between:" & vbTab & sLower &
```
**vbCr & "and:" & vbTab & sUpper End Sub**





# **VIII. MISCELLANEA**

## **Chapter 87: Cracking a Password**

### **What the simulation does**



This is not a real password cracker, of course, but we can still mimic part of the process. First of all, in real life you don't know the password yet. Second, the password can be, and should be, rather long. Neither condition can be met in this simulation.

Let us assume that the password is " $p(a)$ s." This is a 3-letter word, so even if we only use the characters a-z (no capitals), then we would still have 26^3 possible combinations—which amounts to 17,576 different arrangements. But we would like to use other characters as well. So don't make the password longer than 3 characters, for that could take an enormous amount of processing time. Even in the simple example shown above, we were "lucky enough" to find one matching combination after 479,657 trials. Run times may vary considerably, of course.

### **What you need to know**

There is a VBA function called *Chr* (in Excel it's the CHAR function) which returns the character that comes with a certain *asci* number. To find out what the *asci* number of a certain key is, we could use the VBA function *Asc* (in Excel it's the CODE function); for instance, Chr("a") would give us the number 97.

The sheet shows 125 asci numbers in column A and the corresponding characters in B, just for your information. To limit ourselves to "readable" characters, we use the Excel function RANDBETWEEN to get a random character between the asci-numbers 33 and 122

The macro also uses the *Application.StatusBar* property to report progress on the status bar after every 1,000 runs.



### **Option Explicit**

```
Sub Password()
  Dim i As Long, j As Integer, sPass As String,
sGuess As String
  sPass = InputBox("Which password?"
,
"Watch the
Status Bar"
,
"p@s")
  'More than 3 chars could take very long
  If Len(sPass) > 3 Then MsgBox "No more than 3
chars": Exit Sub
  Range("A1").Select
  Do
    For j = 1 To Len(sPass)sGuess = sGuess \&Chr(WorksheetFunction.RandBetween(33, 122))
    Next j
    If sGuess = sPass Then Exit Do
    i = i + 1DoEvents
    If i Mod 1000 = 0 Then Application.StatusBar =
i & " runs"
    sGuess = ""Loop
```
**MsgBox "Found the password " & sPass & " after**

### **" & i & " trials." End Sub**





### **Chapter 88: Encrypting Text What the simulation does**



This file has two sheets. It uses two different macros: one for the 1<sup>st</sup> sheet, and the other for the  $2<sup>nd</sup>$  sheet. They both encrypt and decrypt cells in this case cells with Social Security numbers (SSN). Both macros use a costom function that I gave the name *Encrypt* (the first code on the next page). This function has been given two arguments, the second of which is *Boolean* and determines whether to encrypt the SSN or decrypt the encrypted SSN. In the former case, it shifts asci numbers up by 20 (or so); in the latter case it shifts them down by that amount. Obviously, it is one of the simplest algorithms one could think of.

The difference between macros (*Sub*) and functions (*Function*) is a bit semantic. Functions return something—a word, a value—just like the function SUM returns the total of values. Subs, on the other hand, change things. Let's leave it at that.

The first macro (the second code on the next page) places in column D of the 1<sup>st</sup> sheet an encrypted SSN, and then decrypts it again in column E. It does so by setting the *Formula* property of those cells that uses the function *Encrypt*.

The second macro (the third code on the next page) does something similar, but this time by directly calling the *Encrypt* function.

### **What you need to know**

To make the encrypted version a bit harder to crack, we used the VBA function *StrReverse*, which puts the text, a *String*, in a reversed order.

**Option Explicit**

**'A simple algorithm, so if law enforcement detects illegal use of it, the code can be cracked easily**

```
Function Encrypt(sInput As String, bEncrypt As
Boolean) As String
  Dim i As Integer, sChar As String, sNew As String
  sInput = StrReverse(UCase(sInput))
  For i = 1 To Len(sInput)sChar = Mid(sInput, i, 1)
    sChar = Chr(Asc(sChar) + IIf(bEncrypt, 20,
-20))
     sNew = sNew & sChar
  Next i
  \text{Energy} = \text{sNew 'OR:} = \text{LCase(sNew)}End Function
Sub CreateFormulas()
  Dim iRows As Long
  Sheet1.Activate: Range("A1").Select
  iRows = Range("A1").CurrentRegion.Rows.Count
  Range("D1").Range(Cells(2, 1), Cells(iRows,
1)).ClearContents
  Range("E1").Range(Cells(2, 1), Cells(iRows,
```

```
1)).ClearContents
```

```
If MsgBox("Encrypt and decrypt with formula?"
,
vbYesNo) = vbNo Then Exit Sub
```
**Range("D1").Range(Cells(2, 1), Cells(iRows,**

```
1)).Formula = "=Encrypt(B2,TRUE)"
```

```
Range("E1").Range(Cells(2, 1), Cells(iRows,
```

```
1)).Formula = "=Encrypt(D2,FALSE)"
```

```
End Sub
```

```
Sub Encrypting()
  Dim sText As String, i As Long
  Sheet3.Activate
  Columns("D:E").ClearContents
  MsgBox "Encrypting and decrypting column B"
  For i = 2 To
Range("A1").CurrentRegion.Rows.Count
    Cells(i, 4) = Encrypt(Cells(i, 2), True)Cells(i, 5) = Encrypt(Cells(i, 4), False)
    Cells.EntireColumn.AutoFit
  Next i
End Sub
```
# **Chapter 89: Encrypting a Spreadsheet**

### **What the simulation does**



With an *Application.InputBox*, the user can indicate which part of a sheet to encrypt. Then the macro uses the function *Encrypt* (the same function as used in the previous chapter) to encrypt each cell in this selected range and place it on a new sheet. This is done with a *For-Each*-loop.

Next the macro asks the user whether they want to create a CSV-file of this encrypted sheet (see below). If the user says yes, another *Sub* is called, *SaveAsText*, which opens NotePad and copies the encrypted text onto it.

### **What you need to know**



It is thanks to a global variable, *bEncrypt*, that the macro *Processing* "knows" whether to encrypt or decrypt.

**Option Explicit Dim bEncrypt As Boolean**

```
Sub Processing()
  If bEncrypt = False Then
    bEncrypt = True: Encrypting
  Else
    bEncrypt = False: Encrypting
  End If
End Sub
```

```
Sub Encrypting()
  Dim oWS1 As Worksheet, oWS2 As Worksheet,
oCell As Range, oSelect As Range, sAddr As String
  Set oWS1 = ActiveSheet
  Set oSelect = Application.InputBox("Range"
, ,
Range("A1").CurrentRegion.Address, , , , , 8)
  Set oWS2 = Sheets.Add(, oWS1)
  For Each oCell In oSelect
    sAddr = oCell.Address ; oWS2.Range(sAddr) =
Encrypt(oCell.Value, bEncrypt)
  Next oCell
  oWS2.Cells.EntireColumn.AutoFit
  If MsgBox("Do you want an encrypted CSV file?"
,
```
**vbYesNo) = vbYes Then SaveAsText If bEncrypt = False Then Exit Sub If MsgBox("Do you want to decrypt next?" , vbYesNo) = vbYes Then bEncrypt = False: Encrypting End Sub**

```
Function Encrypt(sTxt As String, bEncr As Boolean)
  Dim i As Long, sChar As String, sNew As String
  For i = 1 To Len(sTxt)sChar = Mid(sTxt, i, 1) : sChar =
Chr(Asc(sChar) + IIf(bEncr, 20, -20))
    sNew = sNew & sChar
  Next
  Encrypt = sNew
End Function
```

```
Sub SaveAsText()
  Dim vExe As Variant, oSelect As Range
  Set oSelect = Application.InputBox("Range"
, ,
Range("A1").CurrentRegion.Address, , , , , 8)
  oSelect.Copy : vExe = Shell("notepad.exe"
,
vbNormalFocus)
  AppActivate vExe ; SendKeys "^V"
, True
End Sub
```
## **Chapter 90: Numbering Records What the simulation does**



This macro automatically "numbers" each record in a database by inserting a column before the first column and then populating it with various options:

- Consecutive numbering
- With leading zeros
- Starting at a specific number
- Repeating from 1 to n
- Repeating each number n times

At the end of all these options, the macro lets the user sort range (J11:J16) in a randomly sorted way. The sorting is based on random numbers in column I. The randomly sorted list uses the Excel functions VLOOKUP and SMALLas shown in the comment of cell L11.

#### **What you need to know**

The Excel functions that can be used here are ROW, RIGHT, MOD, QUOTIENT, VLOOKUP, and SMALL.

QUOTIENT returns the integer portion of a division; its  $1<sup>st</sup>$  argument holds the numerator, the  $2<sup>nd</sup>$  argument the divisor.







 $\sqrt{4}$  $\frac{5}{6}$  $\overline{\prime}$  $\bf 8$  $\,9$  $10\,$  $11\,$  $12\,$  $13$  $14$ 15

 $16$ 



### **Option Explicit**

**Sub Numbering() Dim oRange As Range Range("A1").EntireColumn.Insert Range("A1") = "ID" Set oRange = Range("A1").CurrentRegion Set oRange = oRange.Offset(1, 0).Resize(oRange.Rows.Count - 1, 1) With oRange MsgBox "Consecutive numbering." .Formula = "=ROW(A1)" .Formula = .Value MsgBox "With leading zeros." .Formula = "=RIGHT(""000"" & ROW(A1),3)" .Copy: .PasteSpecial xlPasteValuesAndNumberFormats Application.CutCopyMode = False: Range("A1").Select MsgBox "Starting at 1001." .Formula = "=ROW(A1001)" .Formula = .Value: Application.CutCopyMode = False**

**MsgBox "Repeating from 1 to 5."**

**.Formula = "=MOD(ROW(A1)-1,5)+1" .Formula = .Value MsgBox "Repeating each number 5 times." .Formula = "=QUOTIENT(ROW(A1)-1,5)+1" .Formula = .Value End With MsgBox "The last step deletes column A" Range("A1").EntireColumn.Delete Do While MsgBox("In H11:K16, we sort data randomly. Again?" , vbYesNo) = vbYes Calculate Loop**

**End Sub**



# **Chapter 91: Sizing Bins for Frequencies**

### **What you need to know**



In this macro, an *Application.Inputbox* asks the user which values from A1:E20 should be covered in the frequency table of columns G:H. The macro also checks how many bins the user wants to create, so the VBA code can properly calculate the bin sizes.

### **What the simulation does**

The VBA code creates a *Range Name* for the range that has been selected, so that this *Name* can be used in formulas. At the beginning of the code, a previously assigned *Name* has to be deleted, if there is one. But if this *Name* did not exist yet, the code would run into trouble for it cannot delete what is not there—that's what the line *On Error Resume Next* tries to prevent.

An alternative would be to declare a variable of the *Name* type: *Dim oName as Name*. And then make a loop like this: *For Each oName in Names* | *If oName = "data" then oName.Delete* | *Next oName.*

The FREQUENCY function returns the frequencies for each bin, but also returns one additional value for what we could call the "left-overs." If that extra bin is not 0, then some or more values have been left out. That is a final check that not all values have been covered.

The formula in the bins range that creates the bins would look like this:

=INT(MIN(data)+(ROW(A1)\*(MAX(data)-MIN(data))/" & iBin & ")).

**Option Explicit**

**Sub BinSizing() Dim iBin As Integer, oData As Range, oBins As Range, oFreqs As Range On Error Resume Next Sheet1.Names("data").Delete Set oData = Application.InputBox("Range" , , Range("A1").CurrentRegion.Address, , , , , 8) oData.Name = "data" iBin = InputBox("How many bins (5-10...-30)?" , , 20) If iBin > 30 Then Exit Sub Columns("G:H").ClearContents Set oBins = Range(Cells(1, 7), Cells(iBin, 7)) oBins.Formula = "=INT(MIN(data)+(ROW(A1)\* (MAX(data)-MIN(data))/" & iBin & "))" Set oFreqs = Range(Cells(1, 8), Cells(iBin + 1, 8)) '+1 for the left-overs oFreqs.FormulaArray = "=FREQUENCY(data, " & oBins.Address & ")" oData.Select End Sub**



# **Chapter 92: Creating Calendars**

### **What the simulation does**



This macro creates a calendar for the month and year of your choosing, either in a *MsgBox* (picture above) or on the sheet itself (picture below)

### **What you need to know**



The VBA function *DateSerial* returns a date based on 3 arguments (year, month, day). The VBA function *WeekDay* returns the day of the week from 1 (Sunday) to 7 (Saterday). So the VBA expression *WeekDay*(2) would return "Monday."

### **What you need to do**

### **Sub Calendar() Dim dStart As Date, dDay As Date Dim i As Integer, sCal As String dStart = InputBox("Start" , , Date)**  $For i = 0$  To 30

 $dDay = dStart + i$ 

**If Weekday(dDay) <> 1 And Weekday(dDay) <> 7 Then**

**sCal = sCal & vbCr & Format(dDay, "ddd" & vbTab & "mm/dd/yy")**

**Else sCal = sCal & vbCr End If Next i MsgBox sCal End Sub**

```
Sub MonthDisplay()
```

```
Dim dDate As Date, sCal As String, i As Integer,
iMonth As Integer, iYear As Integer
  iMonth = InputBox("Month"
, , Month(Now()))
  iYear = InputBox("Year"
, , Year(Now()))
  sCal = MonthName(iMonth) & " " & iYear &
vbCr
  sCal = sCal & "S" & vbTab & "M" & vbTab &
"T" & vbTab & "W" & vbTab & "T" & vbTab & "F"
& vbTab & "S" & vbCr
  dDate = DateSerial(iYear, iMonth, 1 : dDate =
dDate - Weekday(dDate) + 1
  Do
    For i = 1 To 7
      If Month(dDate) = iMonth Then sCal = sCal
& Day(dDate)
      sCal = sCal & vbTabdDate = dDate + 1
    Next i
    sCal = sCal & vbCrLoop While Month(dDate) = iMonth
  MsgBox sCal
End Sub
```

```
Sub SheetCalendar()
  Dim dDate As Date, iMonth As Integer, iYear As
```
**Integer**

```
Dim sRange As String, r As Integer, i As Integer
  sRange = Application.InputBox("Start in cell"
, ,
"A1")
  iMonth = InputBox("Month"
, , Month(Now()))
  iYear = InputBox("Year"
, , Year(Now()))
  With Range(sRange)
     .Value = MonthName(iMonth) & " " & iYear
     .Range(Cells(1, 1), Cells(1, 7)).Merge
     .HorizontalAlignment = xlCenter
    r = 2For i = 1 To 7.Cells(r, i) = Left(WeekdayName(i), 3)
    Next i
     dDate = DateSerial(iYear, iMonth, 1)
     dDate = dDate - Weekday(dDate) + 1
    Do
       r = r + 1For i = 1 To 7If Month(dDate) = iMonth Then .Cells(r, i)
= Day(dDate) Else .Cells(r, i) = ""
         dDate = dDate + 1
       Next i
    Loop While Month(dDate) = iMonth
     .CurrentRegion.BorderAround , xlThick
  End With
End Sub
```
# **Chapter 93: Populating a Jagged Array**

**What the simulation does**



This simulation creates random sales per row—which could be per day, per week, or whatever. Since the number of sales per row can vary, a simulation like this can best be done with a so-called jagged array.

The "main" array has 26 elements (0 to 25). But each one of these 26 elements holds another array of elements. So we end up with an array of arrays—a 1-dimensional "main array" with 1-dimensional "subarrays." The dimension of each subarray is determined randomly.

### **What you need to know**

The simulation loops through the 26 elements of the main array and starts each time a subarray with a random amount of (random) elements, the sales. Once the subarray is finished, the simulation stores it in the main array: *arrMain(i) = arrSub*. Make sure the main array is of the *Variant* type, for only a *Variant* can store another array.

To populate the cells on the sheet, you need to address each element in the main array as well as in the subarray. This is done as follows:  $\frac{arr\frac{1}{j}}{i}$  with *j* refering to a subarray element, and *i* to a main array element.

On the last line, the simulation calculates the total sales amount.

In case you want to create the jagged array on a new sheet, the VBA code has also a *Sub* called *InsertSheet*.

**Option Explicit**

```
Sub JaggedArray()
  Dim arrMain(25) As Variant, arrSub() As String
  Dim i As Integer, j As Integer, iRand As Integer
  Dim cSubTotal As Currency, cGrandTotal As
Currency
```

```
Range("A1").CurrentRegion.Cells.Interior.ColorIndex
= 0
  Range("A1").CurrentRegion.ClearContents
  'Loop thru Main Array and create Sub arrays of
random length
  For i = 0 To UBound(arrMain)
    iRand = Int(Rnd() * 15)
    ReDim arrSub(iRand)
    For j = 0 To UBound(arrSub)
       arrSub(j) = FormatCurrency(Rnd() * 1000)
    Next j
    arrMain(i) = arrSub
  Next i
  'Call InsertSheet below if you like
  For i = 0 To UBound(arrMain)
    For j = 0 To UBound(arrMain(i))
```

```
ActiveCell.Offset(i, j) = arrMain(i)(j)
       cSubTotal = cSubTotal + arrMain(i)(j)
    Next j
    ActiveCell.Offset(i, j) = cSubTotal
     cGrandTotal = cGrandTotal + cSubTotal:
cSubTotal = 0ActiveCell.Offset(i, j).Interior.ColorIndex = 15
  Next i
  ActiveCell.Offset(i, j) = cGrandTotal
  ActiveCell.Offset(i, j - 1) = "GrandTotal"
  Cells.EntireColumn.AutoFit
End Sub
Sub InsertSheet()
  Dim oWS As Worksheet, sName As String
Again:
```

```
sName = InputBox("Which name?")
```

```
If sName = "" Then Exit Sub
```
**For Each oWS In Worksheets**

**If LCase(oWS.Name) = LCase(sName) Then GoTo Again Next oWS Set oWS = Worksheets.Add(, ActiveSheet) oWS.Name = sName End Sub**

### **Chapter 94: Filtering a Database What the simulation does**



The first macro creates an *AdvancedFilter* on a new sheet. It loops through all the headers and asks the users if they want a filter for label1, label2, etc. (see next picture).

The second macro asks users to select the item they want to filter for (bottom picture).

#### **What you need to know**





**Option Explicit**

```
Sub FilterDB()
```
**Dim oData As Range, oFilter As Range, i As Integer, sSet As String, oWS As Worksheet Set oData = ActiveCell.CurrentRegion oData.Rows(1).Copy Set oWS = Worksheets.Add(, ActiveSheet) ActiveCell.PasteSpecial For i = 1 To oData.Columns.Count sSet = InputBox("Set filter (or leave empty) " & oData.Cells(1, i))** If  $sSet \leq ""$  Then  $ActiveCell.Offset(1, i - 1) =$ **sSet Next i Set oFilter = ActiveCell.CurrentRegion oData.AdvancedFilter xlFilterCopy, Range(oFilter.Address), Range("A4") oFilter.EntireColumn.AutoFit**

**End Sub**

**Sub HideRows()**

**Dim col As Integer, r As Long, i As Long, iCount As Long, oSelect As Range**

```
With ActiveCell.CurrentRegion
    r = .Rows.Count
    Set oSelect = Application.InputBox("Select a
value to filter for"
, , Range("G4").Address, , , , , 8)
    oSelect.Select: col = ActiveCell.Column
    For i = 2 To rIf .Cells(i, col) <> ActiveCell Then
         .Cells(i, col).EntireRow.Hidden = True
       Else
         iCount = iCount + 1
       End If
    Next i
    MsgBox iCount & " records"
     If MsgBox("Unhide rows?"
, vbYesNo) = vbYes
Then .EntireRow.Hidden = False
  End With
End Sub
```
# **Chapter 95: Formatting Phone Numbers**

### **What the simulation does**



This macro formats "messy" phone numbers so they look properly formatted. It works even for seriously mutilated numbers (see column E). The macro is based on the format that the USA uses for its phone numbers. You may have to adjust the VBA code to your country's format.

Through *an Application.InputBox*, the users can select the top phone number in a column. The macro will insert a new column to the right of it and produce the formatted version of all the numbers in the preceding column.

### **What you need to know**



The macro *PhoneColumn* does the heavy work, but it does so in the new column by creating formulas that use the custom function *PhoneFormat*. This function does the cobbling together of the numbers by using VBA functions such as *Len*, *Right*, *Mid*, and *IsNumeric.* They all speak for themselves. To determine the number of characters in a string, we use the *Len* function. Perhaps *Mid* needs a bit more information. It has 3 arguments: string, start (the character position in a string), and length (the number of characters to return).

Another new VBA element is the *Select Case* statement. In this macro, it specifies the length of the string we have reached so far in the process.

### **Option Explicit**

```
Function PhoneFormat(Phone As String) As String
  Dim i As Integer, sFormat As String, sCur As
String, sTrunc As String, n As Integer
  sTrunc = Phone
  For i = 1 To Len(sTrunc)If IsNumeric(Mid(sTrunc, i, 1)) Then n = n + 1Next i
  If n > 10 Then sTrunc = Right(sTrunc, Len(sTrunc)
- 1)
  For i = 1 To Len(sTrunc)sCur = Mid(sTrunc, i, 1)
    If IsNumeric(sCur) Then
       Select Case Len(sFormat)
         Case 0: sFormat = "(" & sCur
         Case 3: sFormat = sFormat & sCur & ")-"
         Case 8: sFormat = sFormat & sCur & "-"
         Case Else: sFormat = sFormat & sCur
       End Select
    End If
  Next i
  PhoneFormat = sFormat
End Function
```
**Sub PhoneColumn()**

**Dim r As Long, c As Integer, i As Long, iLast As Long, oSelect As Range**

**Set oSelect = Application.InputBox("Select the top number" , , Range("B2").Address, , , , , 8)**

**oSelect.Select**

```
r = ActiveCell.Row
```

```
c = ActiveCell.Column
```
**iLast = ActiveCell.CurrentRegion.Rows.Count ActiveCell.Offset(0, 1).EntireColumn.Insert**

**Range(Cells(2, c + 1), Cells(iLast, c +**

**1)).NumberFormat = "General"**

**Range(Cells(2, c + 1), Cells(iLast, c +**

**1)).FormulaR1C1 = "=PhoneFormat(RC[-1])" End Sub**

### **Chapter 96: Creating Gradients What the simulation does**



This simulation creates gradients between the four corner cells of range A8:E12. At each run the four corner cells change randomly. All the other cells have to be adjusted so they form a smooth gradient with gradual transitions.

### **What you need to know**



The "trick" to achieve this is using the AVERAGE function, but in such a way that the formula refers to two neighboring cells plus itself—for instance, in cell B8: =AVERAGE(A8:C8). Since the formula in such cells

uses a reference to itself, it causes circular reference. Excel does not allow this, unless you temporarily turn *Iteration* on.

Once the formulas are "settled," the macro replaces them with the values found, so it can turn *Iteration* back off.

If the matrix would have more cells, you may have to increase *MaxIterations* in the VBA code, to make sure each cells reaches a stable value.

**Option Explicit**

**Sub Gradients() Application.Iteration = True Application.MaxIterations = 1000 Application.Calculation = xlCalculationAutomatic Do Range("A8") = Rnd: Range("A8").Formula = Range("A8").Value Range("E8") = Rnd: Range("E8").Formula = Range("E8").Value Range("A12") = Rnd: Range("A12").Formula = Range("A12").Value Range("E12") = Rnd: Range("E12").Formula = Range("E12").Value 'Fill the outer ranges first and then the center Range("B8:D8").Formula = "=AVERAGE(A8:C8)" Range("E9:E11").Formula = "=AVERAGE(E8:E10)" Range("B12:D12").Formula = "=AVERAGE(A12:C12)" Range("A9:A11").Formula = "=AVERAGE(A8:A10)"**

### **Range("B9:D11").Formula = "=AVERAGE(A8:C10)" 'Replace formulas with values Range("A8:E12").Formula = Range("A8:E12").Value Loop Until MsgBox("Repeat?" , vbYesNo) = vbNo Application.Iteration = False End Sub**



# **Chapter 97: Aligning Multiple Charts**

### **What the simulation does**



This sheet has multiple *Areas*—that is, sections separated by empty rows (or columns). The macro loops through the collection of *Areas* and creates charts next to each other of a new sheet.

### **What you need to know**





The file contains

also a *UserForm* with a *ComboBox* on it. The *ComboBox* is populated with information stored on Sheet22 (see picture to the left). With the settings in column C, the user can regulate through the *ComboBox* which type of chart to display. The user can activate the form with the *Sub Types*  $(Ctrl+Sh+T).$ 

**Private Sub UserForm\_Activate() 'code in a UserForm with a ComboBox Dim i As Integer With Sheet22.Range("A1").CurrentRegion**  $For i = 1 To . Rows. Count$ **ComboBox1.AddItem .Cells(i, 1) & "-" & .Cells(i, 2) Next i End With End Sub Private Sub ComboBox1\_Click() Dim oWS As Worksheet, i As Integer On Error Resume Next Set oWS = ActiveSheet For i = 1 To oWS.ChartObjects.Count oWS.ChartObjects(i).Chart.ChartType = Left(ComboBox1.Text, InStr(1, ComboBox1.Text, "-**  $"$ ) - 1) **Next i End Sub**

**Sub CreateCharts() 'this code is in a Module Dim oRange As Range, i As Integer, oChart As**

```
Chart, oWS As Worksheet
  Set oWS = Worksheets.Add(, ActiveSheet)
  Set oRange =
Sheet1.Columns(1).SpecialCells(xlCellTypeConstants).
  For i = 1 To oRange.Areas.Count
    Set oChart = Charts.Add
    With oChart
       .SetSourceData
oRange.Areas(i).CurrentRegion
      .ChartArea.Border.Weight = xlThick :
.ChartType = xlColumnClustered
       : .HasTitle = True : .ChartTitle.Caption
= oRange.Areas(i).Cells(1, 1)
       .Location xlLocationAsObject, oWS.Name
    End With
  Next i
  oWS.Activate
  For i = 1 To oWS.ChartObjects.Count
    With oWS.ChartObjects(i)
       .Width = ActiveWindow.Width * 0.4 :
.Height = ActiveWindow.Height * 0.6
       .Left = ((i - 1) Mod oWS.ChartObjects.Count)
* ActiveWindow.Width * 0.41
       .Top = Int((i - 1) / oWS.ChartObjects.Count) *
150
    End With
  Next i
```
**End Sub**

**Sub Types()**

**UserForm1.Show vbModeless 'see code above End Sub**

## **Chapter 98: Temperature Fluctuations**

### **What the simulation does**



As they say, nothing is as fickle as the weather. We will simulate this for temperature, having it oscillate around a mean of  $65\textdegree$  F and a standard deviation of 10 during a period of 65 years.

As to be expected, there will be some relatively extreme values below the  $5<sup>th</sup>$  percentile mark or above the  $95<sup>th</sup>$  percentile mark by mere randomness. Sometimes we might hit more "peaks" or more extreme "peaks" than usual.

### **What you need to know**



Dramatic swings in temperature can be quite common because of pure randomness. The 5<sup>th</sup> and 95<sup>th</sup> percentile lines in the chart are based on the "hidden" columns C and D. The markers for extremes outside that range are based on hidden columns E and F. The VBA code changes the font color in these four columns to white, and it can protect these columns from manual changes.

The chart plots the series of values in columns B:F. The horizontal axis is based on the first column. Columns E and F plot only the positive and negative peaks; the other cells in those two columns contain the function NA and do not show.

### **Option Explicit**

```
Sub Temps()
  Dim oRange As Range, r As Long
  'to protect the "hidden" columns
  Sheet1.Unprotect
  Columns("C:F").Cells.Font.Color = vbWhite
  Sheet1.Protect , False, , , True 'True allows VBA to
work
  Set oRange = Range("A1").CurrentRegion
  r = oRange.Rows.Count: r = r - 1
  Set oRange = oRange.Offset(1, 0).Resize(r,
oRange.Columns.Count)
  Do
    oRange.Columns(3).Formula =
"=PERCENTILE($B$2:$B$66,$C$1)"
    oRange.Columns(4).Formula =
"=PERCENTILE($B$2:$B$66,$D$1)"
    oRange.Columns(5).Formula =
"=IF(B2>C2,B2,NA())"
    oRange.Columns(6).Formula =
"=IF(B2<D2,B2,NA())"
  Loop Until MsgBox("Repeat?"
, vbYesNo) = vbNo
  If MsgBox("Protect the formulas in columns
```
### **A:E?" , vbYesNo) = vbYes Then Cells.Locked = False Columns("A:F").Locked = True Sheet1.Protect , , , , True, True End If End Sub**



## **Chapter 99: Working with Fiscal Years**

### **What the simulation does**



Excel has great functions to extract the year, month, and day part of a date—but amazingly enough, it has no function to find out to which *quarter* of the year such a date belongs. For data analysis and summary overviews, that is quite a limitation. This problem can be solved, though, with a simple formula of nested functions such as *ROUNDUP(MONTH(any date)/3,0)*.

However, finding the correct quarter becomes much harder when your company does not have a regular fiscal year. That's where a macro comes in handy. On this sheet, an *InputBox* inquires in which month your fiscal year starts and stores that number in an internal variable (and in cell K2). Based on that information, the macro calculates for any particular date to which fiscal year and quarter that date belongs.

The sheet contains two macros: *RegularYear* for a regular year and *FiscalYear* for a fiscal year. However, the 2<sup>nd</sup> macro can also handle a regular year by calling the 1<sup>st</sup> macro, *RegularYear*, when needed.

### **What you need to know**



The table to the right is only for comparison purposes so you can check whether your calculations in the left table are correct. Conditional formatting in the range M1:P24 does the rest:  $=AND(ROW()>=$ \$K\$2,ROW()<\$K\$2+12)

**Option Explicit**

```
Sub RegularYear()
  Dim i As Long, dDate As Date, pQtr As Double,
oStart As Range
  Columns("D:E").ClearContents
  Set oStart = Application.InputBox("Select the top
date"
, , Range("C2").Address, , , , , 8)
  With oStart
    Do While .Offset(i, 0) <> ""
       dDate = .Offset(i, 0)
       .Offset(i, 1) = Year(dDate)
       pQtr = Month(dDate) / 3
       .Offset(i, 2) = IIf(pQtr - Int(pQtr) = 0, pQtr,
Int(pQtr) + 1) 'Instead of RoundUp
       i = i + 1Loop
  End With
End Sub
```
**Sub FiscalYear()**

**Dim i As Long, dDate As Date, iFiscMonth As Integer, iMonth As Integer, oStart As Range Columns("D:E").ClearContents**

```
Set oStart = Application.InputBox("Select the top
date"
, , Range("C2").Address, , , , , 8)
  iFiscMonth = InputBox("In which month does
your fiscal year start?"
, , 10)
  Range("K2") = iFiscMonth
  If iFiscMonth = 1 Then RegularYear: Exit Sub
  With oStart
     Do While .Offset(i, 0) <> ""
       dDate = .Offset(i, 0)
       .Offset(i, 1) = Year(dDate) + IIf(Month(dDate)
>= iFiscMonth, 1, 0)
       iMonth = Month(.Offset(i, 0)) - iFiscMonth +
1
       If iMonth \leq 0 Then iMonth = iMonth +12.Offset(i, 2) = IIf(iMonth / 3 - Int(iMonth / 3)
= 0, iMonth / 3, Int(iMonth / 3) + 1)
       i = i + 1Loop
  End With
End Sub
```
### **Chapter 100: Time Calculations What the simulation does**



In Excel, time is a value that ranges from 0 to 0. 999988425925926, representing the times from 0:00:00 (12:00:00 AM) to 23:59:59 (11:59:59 PM). You can see the value of a particular time under *General Format* or by using  $Ctrl + \sim$  (the tilde is just below the *Esc* key). The advantage of using decimal values for time is that you can then easily add and subtract them. You can even use functions such as SUM, AVERAGE, and so on.

When the difference in time values or their total is more than 24 hours, the decimal time values go beyond 0.9999999. This causes trouble, for time values beyond 0.9999999 get truncated when forced into the *h:mm:ss* format. If the sum is 1.5, for example, Excel shows only its decimal part, 0.5, which is 12:00:00 AM. To solve this problem, you must change the format of this number from *h:mm:ss* to *[h]:mm.ss*. Then a number such as 1.5 will indeed show up as 1.5 (in the proper time format, of course: 36:00:00). Thanks to the *[h]:mm:ss* format, you can calculate with time values beyond the duration of 1 day, which is usually necessary for sum operations.

### **What you need to know**



This is basically all the macro does for summaries below the table, if needed,and also to the right, if so desired. On the next run it will delete

those summaries first.

Some people prefer to use hours with decimals—where, for example, 13**.**50 (with a decimal point) is 13 hours and 30 minutes, as opposed to 13**:**50 (with a colon), which is 13 hours and 50 minutes. To convert these decimals to Excel's time decimals, you need to divide by 24 because Excel works with day units of 24 hours, 60 minutes, and 60 seconds.

**Option Explicit**

```
Sub TimeCalc()
```

```
Dim oSum As Range, oTable As Range, oAvg As
Range, r As Long, c As Long
```
**Set oTable = Range("B2").CurrentRegion r = oTable.Rows.Count: c = oTable.Columns.Count oTable.Rows(r).Offset(2, 0).ClearContents oTable.Rows(r).Offset(3, 0).ClearContents oTable.Columns(c).Offset(0, 2).ClearContents oTable.Columns(c).Offset(0, 3).ClearContents If MsgBox("Summaries at the bottom?" , vbYesNo) = vbYes Then**

 $Cells(r + 2, 1) = "Sum"$ Set  $oSum = Range(Cells(r + 2, 2), Cells(r + 2, c))$  $Cells(r + 3, 1) = "Mean"$ Set  $oAvg = Range(Cells(r + 3, 2), Cells(r + 3, c))$ **oSum.FormulaR1C1 = "=SUM(R[-" & r & "]C:R[-2]C)" oSum.NumberFormat = "[h]:mm:ss"**

**oAvg.FormulaR1C1 = "=AVERAGE(R[-" & r + 1 & "]C:R[-3]C)"**

```
oAvg.NumberFormat = "h:mm:ss"
End If
```

```
If MsgBox("Also summaries to the right?"
,
vbYesNo) = vbYes Then
    Cells(1, c + 2) = "Sum"Set oSum = Range(Cells(2, c + 2), Cells(r, c + 1))2)): oSum.ClearContents
    Cells(1, c + 3) = "Mean"Set oAvg = Range(Cells(2, c + 3), Cells(r, c + 3)):
oAvg.ClearContents
    oSum.FormulaR1C1 = "=SUM(RC[-" & r &
"]:RC[-2])"
    oSum.NumberFormat = "[h]:mm:ss"
    oAvg.FormulaR1C1 = "=AVERAGE((RC[-" & r
+ 1 & "]:RC[-3]))"
    oAvg.NumberFormat = "h:mm:ss"
  End If
End Sub
```
# **IX. APPENDIX**

### **Data Tables**

A *Data Table* is a range of cells that shows how changing one or two variables in your formulas will affect the results of those formulas. A *Data Table* provides a powerful way of calculating multiple results in one operation and a way to view and compare the results of all the different variations together on your worksheet.



To implement a *Data Table*, you select the entire range, including its point of origin with a formula in it—so that is B3:F13 in the example above. Then you go through the following menus: Data | What-If Analysis | Data Table. In the dialog box, set the row input to cell B2 and the column input to cell B1.

Once you click OK, Excel replaces all empty cells (in the shaded area) with an array formula like this:  $\{\text{=TABLE(B2,B1)}\}$ . Or more in general, *{=TABLE(row-input-cell, column-input-cell)}*. Sometimes, one or both of the two arguments are missing. Do not type the braces—Excel creates them automatically when you hit the *Data Table* button. And do not type the formula!

Why use a *Data Table*? There are several reasons. First, it might be easier to implement one than working with locked and unlocked cell references. Second, no part of the array can inadvertently be deleted or changed, because the array acts as one entire unit. Third, a *Data Table* has much more extra potential, as you can see in many of the simulations we use in this book.

However, there is one drawback. Because there may be many operations involved in a *Data Table*, Excel may run into speed problems. There are two ways to get around this speed issue. Method #1 is to stop automatic recalculation—at least for Data Tables. Do the following: File | Options | Options | Formulas | Automatic Except for Data Tables (you can even set all calculations to manual). If you ever need to recalculate a *Data Table*, just use  $Sh + F9$ , and that will recalculate only the particular sheet you are on (whereas *F9* alone would recalculate the entire file).

Method #2 is that, after you run a specific what-if analysis, you copy the *Data Table* section—that is, the area between the top row and the left column—and then paste it as values over itself. Move on to the next *Data Table*, run it, and paste values again. Whenever you need to run a pasted table again, quickly reimplement the *Data Table*.

One more limitation: A Data Table cannot accommodate more than two variables. So they are at best two-dimensional but never three-dimensional. There are ways to get around this limitation as shown in some simulations (e.g. Chapter 69).

In VBA, it is actually very easy to implement a *Data Table* by using a range's *Table* method followed by a space and two arguments, one for the row input and one for the column input.
## **Simulation Controls**

Controls such as spin buttons and scroll bars are great tools for many kinds of what-if analysis. They quickly reset specific hard-coded values and then show you the impact of such operations.

In order to create such controls, you need the *Developer* tab in your menu, which may not be present on your machine. To add it to the ribbon, you do the following, depending on your Excel version. Pre-2010: File | Options | General | Enable the Developer Tab. In 2010 and 2013: File | Options | Customize Ribbon | in the far right list: Developer. From now on, the tab can be found in the menu on top.



On the above sheet, we placed three controls. You do so by clicking on the *Insert* button and then on one of the options in the lower section of the list (Active-X Controls). Draw the control you have chosen on your sheet.

Then click on the *Properties* menu (make sure the control you want to set the properties for is still selected, or select it). Set at least the properties *Min*, *Max*, and *LinkedCell* (that is, the cell where you want the control's value to appear).

Once you are done, do not forget to click the *Design Mode* button OFF, so you can go back to your sheet!!! Be aware, though, that when you

change a control and calculation is not automatic, you need to activate the sheet first before you can hit the "run" keys *Sh F9*.

You probably noticed already that the properties *Min* and *Max* can only hold integers. So if you want to regulate decimals with your control (like in the scroll bar to the far right), you need an intermediate cell. I happened to choose a *LinkedCell* reference located behind the control (e.g. cell I5). In the cell where you want the decimal number visibly displayed, you need to place a formula like =I5/10 (or I5/100, etc.).

Controls like these are fantastic. I used them for several simulations in this book. They are not only fun, but also very informative and revealing. I think you will love them more and more, if you did not already.

## **If Statements**

Either one-liners:



Or multi-liners:



# **End If**

# **Value Type Variables**





# **Ranges vs. Cells**





# **FormulaR1C1**



## **Arrays**





# **Error Handling**

## gnillonsk rorr



This would make a very general error handler: Sub AnySub() On Error GoTo ErrTrap .... Exit Sub ErrTrap: MsgBox "Number: " & Err.Number & vbCr & \_ "Description: " & Err.Description & vbCr & "Source: " & Err.Source, vbCritical, "Call 1-800-123-

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## **About the Author**



Dr. Gerard M. Verschuuren is a human geneticist who also earned a doctorate in the philosophy of science. He studied and worked at universities in Europe and the United States and wrote several biology textbooks in Dutch. During this time, he also used and programmed computer software, including Excel, to simulate scientific problems.

Currently, he is semi-retired and spends most of his time as a writer, speaker, and consultant on the interface of science and computer programming.

His most recent computer-related books are:

- 1. From VBA to VSTO (Holy Macro! Books, 2006).
- 2. Visual Learning Series (MrExcel.com).
- 3. VBScript (CD)
- 4. Excel 2013 for Scientists (CD)
- 5. Excel 2013 for Scientists (book)
- 6. 100 Excel Simulations (book)
- 7. Excel 2013 VBA (CD)
- 8. Excel Video Medley (double DVD)

For more info see: [http://en.wikipedia.org/wiki/Gerard\\_Verschuuren](http://en.wikipedia.org/wiki/Gerard_Verschuuren)

For his YouTube videos on Excel and VBA: http://www.genesispc.com/links.htm#videos

All his books, CDs, and DVD's can be found at http://[www.genesispc.com](http://www.genesispc.com/)



### All by the same author, Dr. Gerard M. Verschuuren



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Part 2: Data Analysis

Chapter 7: Subtotals Chapter 8: Summary Functions Chapter 9: Unique Lists

Chapter 10: Data Validation Chapter 11: Conditional Formatting Chapter 12: Filtering Tools Chapter 13: Lookups Chapter 14: Working with Trends Chapter 15: Fixing Numbers Chapter 16: Copying Formulas Chapter 17: Multi-cell Arrays Chapter 18: Single-cell Arrays Chapter 19: Date Manipulation Chapter 20: Time Manipulation Part 2 Exercises

#### Part 3: Plotting Data

Chapter 22: A Chart's Data Source Chapter 23: Combining Chart Types Chapter 24: Graph Locations Chapter 25: Templates and Defaults Chapter 26: Axis Scales Chapter 27: More Axes Chapter 28: Error Bars Chapter 29: More Bars Chapter 30: Line Markers Chapter 31: Interpolation Chapter 32: Graph Formulas Part 3 Exercises

Part 4: Regression and Curve Fitting Chapter 34: Nonlinear Regression Chapter 35: Curve Fitting Chapter 36: Sigmoid Curves Chapter 37: Predictability Chapter 38: Correlation Chapter 39: Multiple Regression Chapter 40: Reiterations + Matrixes Chapter 41: Solving Equations Chapter 42: What-If Controls Chapter 43: Syntax of Functions Chapter 44: Worksheet Functions Part 4 Exercises

Part 5: Statistical Analysis

Chapter 46: Types of Distributions Chapter 47: Simulating Distributions Chapter 48: Sampling Techniques Chapter 49: Test Conditions Chapter 50: Estimating Means Chapter 51: Estimating Proportions Chapter 52: Significant Means Chapter 53: Significant Proportions Chapter 54: Significant Frequencies Chapter 55: Chi-Squared Testing Chapter 56: Analysis of Variance Part 5 Exercises



### **100 Excel Simulations: very similar to the ones in this book but all done with formulas (no VBA)**



Part 1: Basic Essentials Object Oriented Recording Macros Branch Statements Interaction Variables (Value Type) Variables (Object Type) Collections Loop Statements

Variables as Arguments Pivot Tables and Charts

Part 2: Formulas and Arrays Dates and Calendars The Current-Region WorksheetFunction Property Formula Property FormulaR1C1 Custom Functions Array Functions 1D- and 2D-Arrays Customized Arrays Variant Arrays

Part 3: Buttons and Forms

Importing and Exporting Buttons, Bars, Menus Application Events User Forms Data Entry + Mail Merge Custom Objects (Classes) Class Collections Error Handling Distributing VBAcode VBAMonitoring VBA