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Haskell

2010
GHC 9.x

Mini Reference

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A Hitchhiker's Guide to
The Haskell Functional Programming Language

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Haskell Mini Reference:

A Quick Guide to the Haskell 2010 Programming Language

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Preface

If we measure "market shares" of all programming languages in some way and plot the data as a pie chart, the functional programming languages, all of them combined, would not even show up as a wedge-shaped slice on the pie chart.

Despite their general importance, and practical usefulness, functional programming is still considered a niche in the software industry. There can be many reasons for this, but one of the main reasons is lack of good educational materials. There are also a lot of misinformation out there regarding functional programming. Many software developers consider functional programming "difficult", which can be done only by the "elitist" programmers. That cannot be further from the truth.

Functional programming is different from imperative programming. But, not necessarily more difficult. Unfamiliarity breeds

Haskell is one of the most widely used functional programming languages. Haskell has been around for over 30 years, and it has influenced the language designs of numerous (modern) programming languages, including many popular imperative languages such as

Python, JavaScript, C#, Julia, and Rust to name a few.

Haskell is a pure functional programming language. This means that we primarily, and almost exclusively, use the mathematical principle of function applications and function compositions as the primary means of computation. This also means that more traditional imperative programming styles using side effects cannot be generally used while programming in Haskell (with a few important exceptions).

When programmers with the imperative programming background start learning functional programming languages like Haskell, they generally face two main challenges. First, they will need to learn pure functional programming, which requires a rather different mindset. This can be the hard part for some people who have been trained in imperative programming for many years. Second, languages like Haskell use somewhat different syntax from most of the main stream languages. In fact, functional programming languages all tend to use more terse syntax, for example, and this trips over many beginning Haskell programmers. However, this is the easy part.

Books like this can help you learn Haskell language syntax so that you can focus more on learning high-level functional programming styles. As a matter of fact, this mini reference will not teach you how best to program in a functional style, but rather it will only teach you the essentials of the Haskell programming language. If you are looking for a tutorial on functional programming, this book may not be the right one

for you. If you are a complete beginner, then you will not find this book very useful.

This book is specifically written for the people

Who have some exposure to functional programming and would like to learn Haskell,

Who are learning functional programming in Haskell and making a rather slow progress due to its somewhat unfamiliar syntax, or

Who are experienced in procedural programming and want to get a quick taste of the Haskell language.

For this intended target audience, this mini reference will provide an excellent overview of the Haskell functional programming language.

This book is largely based on the official "Haskell 2010 Language Report", but it is not an authoritative language reference. We recommend the readers refer to the original Report for more precise and more detailed information whenever there is any ambiguity in the descriptions in the book.

Dear Readers:

Please read this before you purchase, or start reading and investing your time on, this book.

This book is a language reference, written in an informal style. It is one of the books in a series which cover different programming languages that are widely used. These books are not meant to teach you how to program in those languages in a tutorial style, however.

Going through this kind of language reference-style books once in a while, at various stages of your learning, can boost your programming skills dramatically. But, you will only learn so much based on what you already know. We learn incrementally. Do not try to boil the ocean at your first reading unless you are a truly experienced developer.

These mini references are intended to be read quickly, or even just browsed, in a few hours or a few days. If you feel like you are struggling with every paragraph, on the other hand, then this book is clearly not a right one for you. We suggest you look for an alternative book that is more suitable to you. If you have already purchased this book, you can return it if it's still within the return time window.

Otherwise, here's a quick suggestion. First of all, you do not have to understand or remember Just quickly go through the book from beginning to end, and see which parts you are more familiar with and which parts you are not. Then, come back to this book later, say, after practicing programming for a little while, and read it again. Do you find the book a bit easier to read?

You can repeat these steps once in a while. We all tend to forget things, and a quick refresher is always a good idea. You will learn, or re-learn, something "new" every time.

Good luck!

1. Introduction

The Haskell programming language is based on lambda calculus at its core. In fact, all syntactic structures in Haskell are formally defined through translations of those structures into the lambda calculus-based core part, known as the Haskell kernel.

However, you do not need to be familiar with lambda calculus to use Haskell. Haskell is a high-level general purpose programming language that supports, and encourages, pure functional style programming. If you are new to functional programming, then Haskell is the best language to learn functional programming with.

Despite some common misconceptions, functional programming styles are widely used in modern programming. For example, many developers are now used to programming styles using higher order functions like map, filter, and reduce. Pattern matching has been adopted by virtually all modern languages. Immutability is considered a holy grail even in imperative programming nowadays, especially in the multi-core concurrent programming environments.

It may still require some time and practice to transition to pure

functional programming, but as indicated in the Preface, we do not believe that is the main reason why functional programming languages like Haskell are not as much widely used.

It is most likely the unfamiliar syntax that is what keeps many programmers from trying out functional programming languages. Therefore, we hope that books like this one that focuses on the language grammar can help developers get into functional programming more easily and more willingly.

Other than that, the case for (pure) functional programming is overwhelming, and we will not make any effort to convert you in this book.

1.1. Example Haskell Program

Merge sort is one of the most functional algorithms. Here's a simple implementation of merge sort in Haskell.

Listing 1. MergeSort.hs

```
module      ①
```

```
divide :: Ord a => -> ② divide xs = splitAt xs + xs
```

```
merge :: Ord a => -> -> ③ merge [] s2 = ④ merge s1 []  
= s1 merge ⑤
```

```
| x > y = y : merge s1 ys
```

```
| otherwise = x : merge xs s2
```

```
sort :: Ord a => -> ⑥ sort [] = [] sort = sort list =
```

let = divide ⑦

in merge

①

This line declares a module MergeSort and exports a function Module imports and exports are explained in the [Modules](#) chapter.

②

This line denotes a type signature for the function whose implementation follows in the next line. Notice the general syntax, name :: separated by double colons splitAt is a "built-in" function, included in the Haskell Standard Prelude. Types and functions are two of the most important concepts in Haskell programming, and they are explained throughout this book.

③

Likewise, a type declaration of the function,

④

The and functions are implemented using [pattern](#) which is described in detail in the later part of the book. Pattern matching was first introduced by Haskell, and it is now becoming a core part of virtually every modern

programming language, thanks to its intuitive syntax and expressive power.

⑤

Recursion is at the heart of functional programming. One of the unique features of Haskell is that, lexically, Haskell programs can be written in layout-sensitive or layout-insensitive formats. For instance, the expression written in three lines in this example can be written in one line as well. The layout rule is described in the [Lexical Structure](#) chapter, in the very beginning of the book.

⑥

The sort function also uses pattern matching and recursion. Notice the common pattern in the way that functions are defined over multiple patterns (and, over multiple lines) in Haskell.

⑦

Unlike some popular beliefs, even pure functional programming uses "variables" (albeit The let in expression is explained in the main part of the book, in particular, in the [Let and Where](#) chapter. Note that this let in expression captures the essence of the merge sort algorithm.

Here's a sample program using this sort function:

Listing 2. Main.hs

```
module Main where ①

import MergeSort (sort) ②

main :: IO () ③
main = do ④
    print $ sort [7, 5, 8, 6, 4, 9] ⑤
```

①

Every Haskell program needs a Main module, which includes a value named `This` is similar to the way C-style languages work, in which the "main" function is the entry point to a program.

②

Importing the sort function from the MergeSort module. Notice the lack of semicolons throughout this code example. Again, this is explained in the context of [layout](#)

③

The type of main is `IO ()` which is an instance of the Monad class. Types and classes (or, typeclasses) are explained throughout this reference. The class is briefly described in the [Monads](#) chapter, primarily for completeness. Note that, only through monads, we can include (non-pure) actions in pure functional programs.

④

In the monadic context, the [do expression](#) can be used for "sequential programming". Do expressions often include multiple statements, e.g.,

expressions and declarations. The expression in this particular line will output [4,5,6,7,8,9] to standard output, or the terminal.

If you do not fully understand this program at this point, then read on. This book will teach you how to read Haskell programs, at least in terms of all essential syntax.

1.2. Functional Programming

Pure functional programming is about computing (desired) values through applications of functions. (In this book, and in functional programming in general, a function means a pure function, that is, a mathematical function.) You get an input, a value, and you produce an output, another value, through pure computations. There are no imperative statements involved like "do this and do that".

Although there is no general consensus as to what exactly is functional programming (FP), FP is often characterized by a few tenets, if you will:

In FP, functions are the main building blocks of programs.

FP only deals with values, and values are by definition immutable.

FP does not cause side effects (that is, unless explicitly intended).

In addition, Haskell has a few important characteristics that are not necessarily considered an intrinsic part of FP. For example,

Haskell has a strong static type system, with support for parametric polymorphism.

Haskell supports universal type inference, and hence type declarations are (almost) optional.

Haskell supports lazy evaluation of expressions by default, which can lead to code optimization.

Haskell supports user-defined operators, which is much more powerful than the "predefined operator overloading" mechanism found in other programming languages.

Haskell supports powerful pattern matching, which plays an essential role in virtually every aspect of Haskell programming.

In Haskell, all functions take one value and return one value, through what is known as currying.

In Haskell, every function is a value. And, every value is a function.

Haskell isolates pure functions and non-pure actions using Monads (which originated from category theory).

As a high-level programming language, Haskell runtimes support automatic memory management, e.g., garbage collection.

Haskell programs can be either dynamically interpreted, or they can be compiled to executables.

Haskell has such a strong static type system that the Haskell compiler removes all type information when building an executable. That is, there is no need for runtime type information for Haskell programs after they have been verified by the static type checker. Furthermore, despite the pervasive misconceptions that FP languages are "slow", the leading Haskell compiler can produce highly optimized code which are comparable to those generated by other "fast" imperative languages.

1.3. Book Organization

We start the book with a quick introduction to the [Haskell software development](#) in particular, using the Cabal - GHC toolchain. This is included primarily for completeness, especially for absolute beginners, and it can be skipped if you have some experience with Haskell programming.

In fact, this book assumes that the reader has some exposure to Haskell, or other similar functional programming languages.

In the next chapter, we briefly go through the [lexical structure](#) of Haskell programs, again for completeness. This book, by its very nature, emphasizes breadth more than depth. This chapter can also be skipped, maybe except for the [layout rules](#) section, unless you are completely new to Haskell. The rest of the book is organized more or less in a top down fashion.

A Haskell program comprises one or more Modules are generally used to manage namespaces and organize large programs. Names can be shared among different modules through Haskell's import-export mechanism. All Haskell programs include a special module which includes a value named main with the type This is the entry point to any Haskell program.

A Haskell module consists of a collection of declarations for entities like ordinary values, datatypes, and type classes, and for fixity information. Some declarations can only be used at the module-, or top-, level, and they are described in the [top-level declarations](#) chapter. Some other kinds of declarations, on the other hand, can be included both at the top-level and at some nested context. They are described in the [nested declarations](#) chapter.

We also go through some basics of Haskell's type system in these two chapters, including data types, newtype types, and type synonyms.

As with other programming languages, Haskell includes a number of [primitive, or "builtin"](#). We go through some of them, such as booleans, numbers, characters, and strings in this chapter, and we further discuss user-defined data types and type classes later in the book.

Haskell is a pure functional programming language, and hence it does not have constructs comparable to the "statements" in other imperative programming languages, whose main purpose is to generate side effects. At the level below the modules and declarations are as described in the next several chapters. An expression denotes a value and has a static type. Expressions are the bread and butter of Haskell functional programming.

It may seem somewhat ironic, because many developers consider functional programming languages like Haskell "complex", but the Haskell's language grammar is much simpler than those of other widely used programming languages. In fact, the Haskell language itself includes only a few different kinds of expressions (again, no side effect causing statements), and the rest of the language constructs (e.g., operators) are included in the standard library. Some of them are part of "the Standard Prelude", and they are no different from the "built-in" language syntax for all intents and purposes.

As is the case with virtually all functional programming languages, functions are the most important construct in Haskell. In the [Functions](#) chapter, we review how to define a function, how to invoke a function, and how to compose two or more functions in Haskell. We also introduce lambda functions in this chapter.

Other than the primitive types like Bool and numbers, [lists](#) are the most important types in Haskell, as in many functional programming languages. Functional programming often involves manipulating lists. [Tuples](#) are also important compound data types that deserve a careful study if you are new to Haskell. Tuples provide a light-weight syntax for user-defined data types, which are discussed later in the book.

All expressions in Haskell have static types. Haskell can deduce the broadest possible type for any expression, which is called its "principal type". Otherwise, that is, if Haskell cannot deduce the principal type, then it is not a valid expression, i.e., not a valid Haskell code. The

[expression type signature](#) syntax can be used to specify a type narrower than the principal type. Or, it can sometimes be used to make an otherwise-invalid expression valid by explicitly specifying the type.

As with any high-level programming language, Haskell supports [conditional](#) with the familiar if - then - else syntax. Unlike in many other languages, however, both then and else clauses are required in Haskell.

Functional programming languages also use "variables". But they have different meanings, and they play different roles, in functional programming languages like Haskell. In particular, variables in Haskell do not imply "storage locations" in memory as in imperative programming languages. (Pure) functional programming languages only deal with "values". Variables are just names for values. In the next chapter, [Let and](#) we go through the basic syntax of the let expressions. We also discuss the where syntax in this chapter, which itself is not an expression but can be used in a somewhat similar fashion to e.g., to define variables.

If we have to pick one particular feature that is the most important in Haskell, it would be the pattern matching. In Haskell, it is almost the foundation of all other expressions. Virtually everything is built on top of pattern matching. The [case expressions](#) play the fundamental role in this regards. Other pattern matching syntax is ultimately translated to case expressions. A case expression can include one or more alternative patterns, and each pattern can include zero or more Boolean guards.

In the following chapter, we go through each of the pattern types supported by Haskell. This is a somewhat artificial classification, and in practice, we mostly use some combinations of these patterns.

In Haskell, there is little distinction between functions and operators. Operators are just a special kind of functions (e.g., which take two arguments). In the chapter, [Core](#) we describe a few of the "built-in" functions and operators from the Prelude.

In the next chapter, [List](#) we go through other "built-in" functions that are used to manipulate lists. There are quite a few, and they are all important, to varying degrees. We only briefly cover each of these functions, but it is essential to understand and "internalize" all these functions in order to be able to use Haskell effectively. One thing to note is that Haskell comes with other standard libraries beyond the Prelude, but we do not cover those in this book.

Haskell supports a rather powerful polymorphic type system. After having gone through all important expressions, we now go back to a few important kinds of declarations, namely, the data type and class declarations.

Needless to say, types are important in modern programming. This is especially so in languages like Haskell which provide strong type-safety

checks at build time. It is pretty much impossible to have type-related errors at run time. It does not mean that if you can build it, it runs without errors, but it is pretty close. Haskell makes it rather easy to create and use custom types through the [data type declaration](#) syntax. A data type is defined by declaring one or more constructors, with positional fields. Haskell also supports the record syntax for data constructors, e.g., using labeled fields. The record syntax is now widely adopted by many other programming languages.

Haskell's polymorphic type system is based on [type](#). We briefly discuss the class declarations, instance declarations, and the deriving syntax in the following chapter. The Standard Prelude includes a few predefined classes, such as `Int` and other numeric classes like `Integer`. We briefly go through some of these classes in the next chapter, [Standard](#)

Whether justifiable or not, [Functors](#) and (especially) [Monads](#) are generally considered the most difficult topics in Haskell. This (short) book will not be able to convince you otherwise if you are in that camp. But, nonetheless, we briefly cover each of these builtin classes. Learning is about recognizing patterns. If you have some experience in programming, then you will realize that Functors and Monads are just simple abstractions over some familiar programming patterns. If not, no worries. You do not have to understand precisely what these terms mean to be able to program in Haskell.

In the monadic context, one can use sort of "imperative-style"

programming, which a majority of programmers are more used to, even in Haskell. This is briefly explained in the next chapter, [do](#)

The most important beneficiary of the Monad class is the I/O related actions. In fact, Haskell, as a pure functional programming language, did not initially have support for I/O for many years. Now, through [Input/Output](#) can be easily incorporated into Haskell programs. The IO type is one of the most important instances of

In the next, and final, chapter, [IO Functions](#) we go through some of the I/O related functions defined in the Prelude. These are core functions to be able to do basic IO in any Haskell programs.

It should be noted that, as indicated earlier, we do not cover any of the Haskell Standard libraries in this book, in the interest of space and the reader's time. This book is a mini language reference.

2. Haskell Software Development

The Haskell programming language was originally created over 35 years ago. But there have been only two official releases in terms of the language specifications. The Haskell language definition was first publicly released in 1998, which is known as Haskell The second and currently most up-to-date spec was released in 2010, which is officially called the Haskell 2010 Language

At this point, there does not appear to be an ownership of the language by any particular organizations. That does not mean Haskell is dead or abandoned. Some day, there might be formed another Haskell Committee, and they will produce the next version of the language, if necessary. Meanwhile, the GHC team (originally, of the University of Glasgow) has the de-facto stewardship of Haskell. They create and distribute the most widely-used Haskell compiler and interpreter, called `ghc` and respectively. And, their build tools support an extensive set of "language extensions", which are essentially additions to the language beyond the Haskell 2010 Report.

Although this book's main focus is the Haskell language itself, we will briefly discuss in this chapter the particular toolings provided by the GHC team, to the benefit of the people who are new to Haskell software

development.

2.1. Development Tools

The most important tool in programming is clearly the compiler (or, the interpreter). But, the modern software development is aided by various tools. Haskell is no exception. We briefly go through some of the GHC-related development tools in this section, without attempting to be complete or exhaustive.

2.1.1. GHCup

GHCup is an optional tool that allows easy management of other Haskell build and package management tools. You can download it from the [GHCup Installation](#). Although it is not required, it is often the best and easiest way to manage Haskell tools such as and

For example, you can easily manage these tools using the tui command:

```
$ ghcup tui
```

(If you have used RustUp for Rust development, for instance, these two tools are comparable to each other. In fact, there are many similar tools across different programming languages.)

2.1.2. Cabal

Cabal is one of the most essential tools for professional Haskell software development. It is a project and package management tool, and it is also a high-level build tool (which uses the `ghc` compiler underneath). You can scaffold a simple Haskell project using the `init` command. For instance,

```
$ cabal init -i
```

You can build a Cabal project using `cabal` or you can build and run using `cabal run` during development. For example,

```
$ cabal run --verbose=0
```

①

The verbose flag can be used to change the verbosity of the build output messages.

You can also install any Haskell packages (available on Hackage) using `cabal`. `cabal --help` will print out some common usages of the `cabal`

command.

2.1.3. Stack

Stack is a (newer) alternative to That is, you can manage and build a Haskell project using Stack instead of Some people prefer one tool over the other, but it is really a matter of preference.

It should be noted that Stack is also integrated into the Haskell Cabal infrastructure. The relationship between Stack and Cabal is comparable to that of Gradle vs Maven in Java, for instance.

2.1.4. HLS

or "Haskell Language Server", is used to add Haskell language support to IDEs or other programs that understand the language server protocols. VS Code, along with the third-party provided extensions, provides good dev support for a wide range of programming languages (e.g., syntax highlighting, intellisense, static code analysis during development, etc.). If you install then you can use VS Code, for example, for Haskell development,

2.1.5. GHC

GHC stands for "Glasgow Haskell Compiler". As stated, it is the de-facto standard compiler for Haskell. If you develop production-quality software in Haskell, you will most likely have to use either directly or indirectly.

In practice, the `ghc` command is rarely used directly. Most developers use the aforementioned high-level (project-oriented) build tools like Cabal or

2.1.6. GHCi

If you are new to Haskell programming, or to functional programming in general, REPL is one of the most important tools during software development. It is rather hard to theorize precisely why REPL plays a lot more important roles in functional programming than in imperative programming, but it is not uncommon to see Haskell programmers always keep the REPL terminal open during development.

The `ghci` command, the REPL that comes with the GHC toolchain, does not compile the Haskell program like `ghc`. Rather it interprets the given expressions, one at a time, in the interactive mode. (The `runghc` command also interprets a given Haskell program, but in the non-interactive mode.) You can start a Haskell REPL by simply invoking the command,

```
$ ghci
GHCi, version 9.4.4: https://www.haskell.org/ghc/ :? for help
ghci> ①
```

①

The default GHCi prompt, waiting for the next command.

You can see a list of all available commands using the `:h` command. For example, `:info`, or `:i`, displays information about the provided names, and `:type`, or `:t`, shows the type of a given expression.

```
ghci> :i map
map :: (a -> b) -> [a] -> [b]    -- Defined in 'GHC.Base'
ghci> :t "Hello World"
"Hello World" :: String
ghci> :t 42
42 :: Num a => a ①
```

①

Numeric literals are polymorphic in Haskell. We explain what this notation means later in the book.

2.1.7. Haskell source code

As with most programming languages, Haskell programs are generally written in files as text. Haskell programs can be coded in two different forms, a normal program style and a "literate" style. The Haskell source code file written in the regular style is generally saved in a file with the .hs extension. This represents a normal code, as is commonly done in any other programming languages.

On the other hand, in the literate programming style, Haskell code should be prefixed with (Or, alternatively, code blocks can be enclosed within LaTeX style tags.) All other text is considered a comment in the literate style code. Literate source code is generally saved in the files with the extension

2.2. Language Extensions

As mentioned, the GHC toolchain provides an extensive set of language extensions. You can selectively turn on or off each of these extensions, e.g., using the `ghc` command line options or using the compiler LANGUAGE pragmas (which we do not discuss in this book). Note that, in Glasgow Haskell, the baseline for the language definition is Haskell 98, and not Haskell 2010. That is, you will need to enable all necessary language extensions (or, "features") if you plan to use Haskell 2010.

Luckily, GHC also provides a small number of meta-extension options which include other options. For example, there are currently three predefined values, e.g., as of GHC 9.4, `Haskell98` (e.g., no extensions enabled), and

We will always be using `Haskell2010` with `ghc` in this book unless otherwise specifically noted. When there is any uncertainty or conflict, the Haskell 2010 Language Report should be the authoritative reference. As for what language extensions are available and how to use them, we recommend the readers refer to the GHC User's Guide.

3. Lexical Structure

Haskell uses the Unicode character set. A Haskell program can only include graphic characters and whitespaces. A comment is lexically considered a whitespace.

3.1. Comments

3.1.1. Line comments

An ordinary line comment begins with a sequence of two consecutive dashes (e.g. `--`) and extends to the end of the line, including the newline. (Note that, in Haskell, the double dashes can also be part of lexically legal operator symbols, e.g.,

```
-- This is comment.  
--- This is also comment.
```

3.1.2. Nested comments

A nested multiline comment begins with `{-` and ends with `-}`. Nested comments may be nested to any depth. Any occurrence of the character sequence `{-` within the nested comment starts a new nested comment, terminated by `-}`. Within a nested comment, each `{-` is matched by a corresponding occurrence of `-}`.

```
{--  
{-  
I am a comment inside another comment.  
-}  
--}
```

3.2. Identifiers

An identifier consists of a letter followed by zero or more letters (including underscores, digits, and single quotes). One or more single quotes are often used at the end of an identifier to denote alternative versions of the given entity with the same identifier but without the single quote suffix. Identifiers are case sensitive.

Haskell identifiers are lexically distinguished into two namespaces:

Variable identifiers - The identifiers that begin with a lowercase letter, which denote variables or functions, and

Constructor identifiers - The identifiers that begin with an uppercase letter, which denote types or constructors.

Underscore `_` is treated as a lowercase letter, and it can occur wherever a lowercase letter is syntactically allowed. The identifier, by itself, is a reserved identifier, which is used as the [wildcard in Haskell](#). Haskell generally offers warnings for declared but unused identifiers. However, these warnings are suppressed against the identifiers that start with underscores, by convention. This, for example, allows programmers to use names like `_foo` or `_bar` as a placeholder (that they expect to be

unused).

3.3. Reserved Words

The following 20 identifiers are reserved in Haskell:

case	class	data	deriving
do	else	if	import
in	infix	infixl	infixr
instance	let	of	module
newtype	then	type	where

3.4. Operators

Operator symbols consist of one or more symbol characters, and they are classified into two distinct namespaces.

An operator symbol with two or more characters starting with a colon : is a constructor.

An operator symbol starting with any other character is an ordinary identifier.

All operators are infix by default, and they can be used in a

3.4.1. Reserved operator symbols

```
..      :      ::     =      |  
<-     ->     @      ~      =>
```

3.5. Layout Rules

Haskell uses curly braces and semicolons for the purposes of grouping, etc., just like many other programming languages. Haskell, however, also supports layout-based style of coding without requiring braces and semicolons in many places. These layout-sensitive and layout-insensitive styles of coding can be freely mixed within one program. Although the layout rules include many details, it is based on rather straightforward indentation rules, and in practice, curly braces and semicolons are rarely used in Haskell programs.

3.5.1. Braces and semicolons

Statements written in the layout-based style can be converted to layout-insensitive style by adding braces and semicolons in places determined by the layout rules.

In general, semicolons demarcate the end of an expression, and curly braces represent scope. For example,

```
cube x = c where { c = x * x * x; }
```

Note that an explicit open brace must be matched by an explicit close brace. Within these explicit braces, no layout processing, as described next, is performed.

3.5.2. Layout processing

The braces and semicolons are inserted as follows.

When an open brace is omitted after the keyword or a new layout starts:

First, the omitted open brace is inserted at the indentation of the next token, and then

For each subsequent line,

If it contains only whitespace or is indented more, then the previous item is continued.

If it is indented by the same amount, then a semicolon is inserted and a new item begins, and

If it is indented less, then a close brace is inserted and the current layout list ends.

When the indentation of the next token after a or of is less than or equal to the current indentation level, then

Instead of starting a layout, an empty item {} is inserted, and

Layout processing occurs for the current level.

(Note: If you are a beginner, you do not have to memorize these rules. Haskell's layout rules are rather flexible, and it will all come naturally.)

4. Modules

A module defines a collection of entities such as values, and in an environment created by a set of imports. A module, in turn, can make some of these entities available to other modules by exporting them. Modules are used for namespace control, and they are not first class values.

A Haskell program comprises one Main module and possibly zero or more other modules. The Main module exports a value named `main` which must be an expression of type `IO T` for some type `T`. The value of the whole program is the value of

4.1. Module Names

A module name is a sequence of one or more separated by dots. Each identifier must begin with a capital letter.

Although it is not part of the language definition, module names can be thought of as being arranged in a hierarchy in which appending a new component (with a dot) creates a child of the original module name.

Modules in standard libraries and other widely used modules tend to use a standardized set of "top-level" module names such as `IO` and `System`, and other related modules are organized "under" these top-level module names such as `IO.Handle`. It should be emphasized, however, that this is purely a naming convention, and Haskell does not support "submodules" or other relationships among the modules.

4.2. Module Structure

Generally speaking, a module and a source code file in Haskell has a one-to-one correspondence. A Haskell module consists of two parts.

A module begins with a header:

The keyword

The module name,

A list of entities to be exported (enclosed in parentheses), and

The keyword and the header is followed by

A module body:

A possibly-empty list of import declarations that specify the modules to be imported into the current module, and

A possibly-empty list of [top-level](#)

In case of the Main module, the module declaration header can be omitted. In such a case, the header is assumed to be module Main(main)

4.3. Export Lists

An export list identifies the entities to be exported by a module declaration such as functions, types, and constructors.

If an export list is not provided, then all values, types, and classes defined in the module are automatically exported, and they will be available to anyone importing the module. Note that the entities imported from other modules are not exported in this case.

```
module MyModule where
```

Limiting the names exported is done by adding a parenthesized list of names after the module name:

```
module MyModule (MyType1, MyClassA, myFuncX) where
```

Note that all [instance declarations](#) are automatically exported with [associated](#) and they cannot be explicitly specified in the export list.

If a module imports another module, it can also export that module,

using the module prefix:

```
module MyModule (module Data.Set, module Data.Char) where  
  
import Data.Set  
import Data.Char
```

4.4. Import Declarations

An import declaration brings into scope the entities exported by another module. The import declaration specifies the name of a module, and it may optionally include the specific entities to be imported from that module. Imported names serve as top level declarations in the current module.

For each entity imported, both the qualified and unqualified names of the entity is brought into scope. If the import declaration uses the qualified keyword, however, only the qualified names of the entities are brought into scope.

An as clause may be used with both qualified and unqualified import statements to provide local aliases.

4.4.1. Importing all

If no specific entities are specified after the imported module name, then all the entities exported by that module are imported, including functions, data types and constructors, classes, and other re-exported modules. For instance, using the following module M as an example,

```
module M(X(..), y) where
  data X = X
  y = 1
```

The following import declaration imports both X and

```
import M
```

These names can be used either as qualified, e.g., M.X and or unqualified, e.g., X and

For a qualified import, however,

```
import qualified M
```

Only the qualified names are available in the importing module, e.g., M.X and M.y in this example. Or, we can use an as alias,

```
import M as M2
```

Or,

```
import qualified M as M2
```

In these two cases, the names M2.X and M2.y are brought into scope, in addition to X and y in the case of unqualified import.

Note that it is legal for more than one module in scope to use the same alias provided that all names can still be resolved unambiguously. For example,

```
module Main where
  import qualified M as M2
  import qualified N as M2
```

This is valid as long as the module N does not export names X and

4.4.2. Importing some or none

The imported entities can be specified explicitly by listing them in parentheses. The list may be empty, in which case only the [instances](#) are imported, if any. When the `(..)` form of import is used for a type or class, the `(..)` refers to all of the constructors, methods, or field names exported from the module.

Using the same example module

```
import M(X(..))           ①
import M as M2(y)        ②
import qualified M(X(..)) ③
import qualified M as M2(X(..), y) ④
```

①

The names `M.X` and `X` are imported.

②

The names `M2.y` and `y` are imported.

③

The name `M.X` is imported.

④

The names `M2.X` and `M2.y` are imported.

The following import declaration, on the other hand, imports no names from the module

```
import M()
```

4.4.3. Importing all but some

As a variation of the method for importing all exported names, one can explicitly exclude some names by using the form `import moduleM hiding(import1, ..., This import declaration specifies that all entities exported by the named module should be imported except for those specifically named in the list.`

For example,

```
import M hiding ()           ①  
import M hiding (X)         ②  
import qualified M hiding () ③  
import qualified M hiding (y) ④  
import qualified M as M2 hiding(X) ⑤
```

①

This brings the names and `M.y` into scope.

②

This imports the names `y` and

③

This imports the names `M.X` and

④

This imports the name

⑤

This imports the name

5. Top-Level Declarations

A Haskell module can include

Zero, one, or more top-level declarations,

[type synonym](#)

[newtype](#)

[data type](#)

[class](#)

[instance](#)

[default](#) and

[Other declarations](#) that can be included in both top-level and nested scopes (e.g., within a [let](#) expression), which comprise

[Type](#)

[Fixity](#)

[Function](#) and

[Pattern](#)

These declarations can also be classified into three groups:

[User-defined data](#) e.g., and data declarations,

[Type classes and](#) e.g., and default declarations, and

[The rest nested](#) e.g., type signatures, fixities, and value bindings for both functions and patterns.

Haskell's builtin types, such as integers and floating-point numbers, and other primitive types are described in the [Basic Types](#) chapter.

5.1. Types and Classes

Haskell uses a polymorphic type system augmented with [type](#) Idiomatic haskell programming styles are often based on manipulating parametrized types (aka, generic types).

5.2. Haskell Type System

Haskell's type system attributes a type to each expression during compilation. The type of an expression depends on an environment that determines the types of the variables in the expression. It also depends on a [class environment](#) if types are [instances of](#). In general, a type is defined over a [context](#) for a set of type variables, typically denoted by (one letter) lowercase alphabets. For example,

```
Eq a => a -> a
```

This denotes a function which takes a value of type `a` and returns a value of the same type `a` -> The type constraint `Eq a` states that this function type can only be defined on the types which are instances of [type class](#). The most general type that can be assigned to a particular expression (e.g., in a given environment) is called its principal. The Haskell type system can infer the principal types of all valid expressions. Therefore, explicit [type signatures for expressions](#) are usually not necessary.

5.3. Typeclasses

A [class declaration](#) introduces a new type class and a set of overloaded operations, called class. An instance type of that class must support those operations. An [instance declaration](#) declares a new type of a given type class, and it (generally) includes the implementations of the [class](#)

5.4. Contexts and Class Assertions

A context consists of zero or more class assertions, with a general form $(C_1 u_1, \dots, C_n u_n)$ where $C_i u_i$ is a class assertion. C_i represents a type class identifier, and u_i can be either a type variable, or the application of type variable to one or more types. (e.g., $\text{Eq } a$ in the above example.) When there is only one type assertion, the outer parentheses can be omitted. A class identifier begins with an uppercase letter whereas a type variable begins with a lowercase letter.

In general, we write $cx \Rightarrow t$ to indicate the constraint that the type t is restricted by the context cx . When the context is empty, we just write t without

5.5. Type Syntax

Type values are built from type constructors. The names of type constructors start with uppercase letters just like [data](#). But, unlike data constructors, infix type constructors are not allowed, other than Type expressions have the following four main forms:

Type Variables

Type variables (or, "generic type parameters", as they are called in some other programming languages) are written as identifiers beginning with a lowercase letter, as just indicated.

Type Constructors

Here are some examples of type constructors. (Note that they are generally called "generic types" in other languages.)

The built-in `Int` and `Bool` are type constants. (That is, they are not "generic".)

[Maybe](#) and [IO](#) are unary type constructors.

[Either](#) is a binary type constructor.

The `T ...` or newtype `T ...` introduce the type constructor

Haskell provides special syntax for certain built-in type constructors:

The [unit type constant](#) is written as `()` and it has one value

The binary function type constructor is written as `(->)` (as a prefix). A function type `(->) t1 t2` can also be written, using the infix notation, as `t1 -> t2`. Function type arrows are right-associative just like in expressions. For instance, `Int -> Char -> Bool` is equivalent to `Int -> (Char -> Bool)`.

The [list type constructor](#) is written as `[]`. A list type `[] t` can also be written as `t []`. It denotes the type of lists with the element type `t`.

The [tuple type constructors](#) (with two or more components) are written as `(, ...)`. A tuple type `(, ...) t1 ... tk` can also use the special syntax `(t1, ..., tk)`. It denotes the type of `k`-tuples with its component types `t1` through `tk`.

Type Applications

A type application `t1 t2` is a type expression of types `t1` and `t2`.

Parenthesized Types

A parenthesized type of a form `(t)` is identical to the type `t`.

Notice that Haskell supports consistent syntax for expressions and their corresponding types. For example, if t_1 and t_2 are the types of expressions e_1 and e_2 respectively, then a function $e_1 \rightarrow e_2$ has the function type $t_1 \rightarrow t_2$, a tuple (e_1, e_2) has the tuple type (t_1, t_2) , and a list $[e_1]$ has the list type $[t_1]$ respectively.

5.6. User-Defined Types

There are three primary constructs in Haskell through which a new type or type alias can be introduced:

The data declaration for creating a new algebraic datatype,

The newtype declaration for creating a new type based on an existing type, and

The type declaration for creating a type synonym for another type.

5.6.1. The data declarations

A new algebraic datatype can be declared with the `data` keyword. along with the [record](#) are described later in the book.

Here's a simple example:

```
data Cat = Cat Int Bool
```

①

①

The `Cat` on the left hand side is a type constructor (with no type variables), whereas the `Cat` on the right hand side is a data constructor. A data type can be defined with one or more constructors. When a data type has only one constructor, it is conventional to use the same name for the type itself and its (only) data constructor. The `Cat` constructor, in this example, includes two fields of `Int` and `Bool` types.

5.6.2. The newtype declarations

A new type can be introduced whose representation is the same as an existing type using the `newtype` keyword:

```
newtype cx => T u1 ... uk = N t
```

This declaration creates a new type `T u1 ... uk` based on, but distinct from, the type `N` `newtype` does not change the underlying representation of an object.

For example,

```
newtype Age = Age Int
newtype Weight = Weight Float
```

A newtype declaration may use the [record syntax](#) with one For example,

```
newtype Age = Age { unAge :: Int }
```


The declaration brings into scope both a constructor and a de-
constructor:

```
Age    :: Int -> Age  
unAge  :: Age -> Int
```

5.6.3. The type declarations

A type synonym declaration introduces a new type that is equivalent to an old type.

```
type T u1 ... uk = t
```

This type declaration introduces a new type constructor, For example,

```
type LastName = String  
type Perhaps = Maybe Int  
type Both a = Either a a
```

6. Nested Declarations

Nested declarations may be used in any declaration list, e.g., either at the top-level of a module or within a where or let construct.

6.1. Type Signatures

A type signature declaration specifies types for variables, e.g., patterns and functions. A type signature has the following general form, for one or more variables $v_1 \dots$

```
v1, ..., vn :: cx => t
```

cx refers to a [context](#) and t represents a [type variable](#) or [type](#). This is equivalent to

```
v1 :: cx => t  
...  
vn :: cx => t
```

Although Haskell can deduce the principal type of any variable, it is conventional to include the type signature declarations for top-level variables, especially functions, in a program. In many cases, the type you want to use for a variable may not be the broadest principal type (which is generally polymorphic in Haskell).

Note that, although it is syntactically not required, the type signature

declaration of a variable (almost always) immediately precedes the binding declaration of the variable.

A variable cannot be declared with more than one type signature even if the signatures are identical.

6.2. Fixity Declarations

A fixity declaration gives the fixity (or, "associativity") and binding precedence of one or more A fixity declaration may appear anywhere that a type signature appears and, like a type signature, it declares a property of a particular target operator.

Also like a type signature, a fixity declaration can only occur in the same sequence of declarations as the declaration of the operator itself, and no more than one fixity declaration may be given for any operator. There are three kinds of fixity:

Non-associativity -

Left-associativity - and

Right-associativity -

There are ten precedence levels, 0 to from binding least tightly to binding most tightly. If the level is omitted, 9 is assumed. Any operator without an explicit fixity declaration is assumed to be infixl E.g.,

```
infixl 6 `plus`  
a `plus` b = a + b
```

6.3. Function Bindings

A function binding binds a variable to a function value. A function binding declaration for variable f has the following general form with n clauses, $n \geq 1$

```
f p11 ... p1k match1
...
f pn1 ... pnk matchn
```

where each p_{ij} is a [pattern](#) each $match_i$ is of the general form:

```
| gsi1 = ei1
...
| gsii = eii
  where { declsi }
```

The expressions, gsi_1 through are called the guards, and they are evaluated to the Boolean values. Pattern matching is further discussed throughout this book, especially in the [case expressions](#) and [patterns](#) chapters.

In case when $match_i$ has a single guard that is merely it can be simply written as follows:


```
= ei where { declsi }
```

Note that

All clauses defining a function must be contiguous, and

The number of patterns in each clause must be the same.

For example,

```
fun :: Int -> Int -> String ①  
fun 0 0 = "Origin" ②  
fun x 0 ③  
  | x > 0 = "Positive x-axis"  
  | x < 0 = "Negative x-axis"  
fun 0 y ④  
  | y > 0 = "Positive y-axis"  
  | y < 0 = "Negative y-axis"  
fun _ _ = "Not so special" ⑤
```

①

The [general type signature declaration syntax](#) is discussed earlier in this chapter. We further discuss what this particular signature means for [functions](#) later in the book. As indicated, it is a universal convention that the type signature for a top-level function binding is placed immediately before the binding declaration.

②

This clause is equivalent to `fun 0 0 | True =`

③

This clause includes a pattern and a match with two guards.

④

Ditto. After the function name, `0 y` is a pattern, and the rest is a match.

⑤

The underscore symbol `_` is a [wildcard](#). The two juxtaposed patterns, in a function binding declaration as in this example, effectively represent a [tuple pattern](#) (e.g., for the two function arguments), as we further discuss later, in the context of [case](#)

6.4. Pattern Bindings

A pattern binding declaration binds variables to values. The general form of a pattern binding is `p where a match is the same structure as for function bindings.`

```
p | gs1 = e1  
  | gs2 = e2  
  ...  
  | gsm = em  
  where { decls }
```

The pattern `p` is matched "lazily" as an [irrefutable](#) as if there were an implicit `~` in front of it.

In case when the guard is simply the pattern binding has the simple form:

```
p = e
```

For example,

```
x :: Int
```

```
x = 3 ②  
  
a, b :: Int  
(a, b) | x > 0 = (3, 4) ③  
       | x < 0 = (-3, -4)  
       | otherwise = (0, 0)
```

①

A [type signature declaration](#) for the following pattern binding. Note that `Int` is the type of the value of the expression `3` in this example. We discuss what is [an "expression"](#) in Haskell throughout the book.

②

A simple pattern binding. Note that, in other more traditional programming languages this kind of syntax may be called a variable declaration and/or variable assignment, etc. In Haskell, the expression on the left-hand side is a [pattern](#) (which is clearly more general and more flexible than just using "names" in other languages). This particular pattern binding declaration is equivalent to `x | True =`

③

A slightly more general pattern binding example. The value [otherwise](#) is a synonym for

7. Basic Types

The Haskell Prelude contains predefined classes, types, and functions that are implicitly imported into every Haskell program.

The following types are defined in the Prelude:

The boolean type,

Numeric types, and etc.,

Char and

and

IO and IOError Types.

In addition, Haskell defines the unit () datatype, which represents a void

value, and an implicit type "Bottom" which is included in every type.

7.1. Booleans

The boolean type `Bool` is an

```
data Bool = False | True
  deriving (Read, Show, Eq, Ord, Enum, Bounded)
```

7.1.1. Boolean functions

The basic boolean functions are `&&` (and), `||` (or), and `otherwise` is defined as `True` to make guarded expressions more readable.

```
(&&) :: Bool -> Bool -> Bool
(||) :: Bool -> Bool -> Bool
not  :: Bool -> Bool
otherwise :: Bool
```

For example,

```
ghci> [True && True, True && False, False && True, False && False]
[True,False,False,False]
ghci> [True || True, True || False, False || True, False || False]
[True,True,True,False]
ghci> [not True, not False]
[False,True]
ghci> otherwise
True
```


7.2. Characters

Haskell's character type `Char` is an [enumeration](#) whose values represent Unicode characters. Character literals, e.g., `'a'` and `'A'` are nullary constructors in the datatype

Type `Char` is an instance of the classes `Enum` and `Ord`. The `toEnum` and `fromEnum` functions, from the `Enum` class, map characters to and from the `Int` type, respectively. For example,

```
ghci> toEnum 65 :: Char
'A'
ghci> fromEnum 'a' :: Int
97
```

7.3. Strings

String in Haskell is an alias for a list of chars. That is,

```
type String = [Char]
```

For example,

```
ghci> h = "hello world"
ghci> import Data.Char
ghci> map toUpper h
"HELLO WORLD"
```

A string literal may include a "gap", that is, a pair of backslashes enclosing one or more whitespace characters, including newlines. Gaps are ignored, which allows writing "multi line" strings in Haskell. For example,

```
ghci> :{
ghci| truth = "It's not      enough" ①
ghci|           to speak,
ghci|           but to speak true."
ghci| :}
ghci> putStrLn truth ③
```

①

GHCI accepts multi-line commands with this syntax, using a pair of opening and closing symbols, `{` and

②

Note that there are three backslash characters. The first two match and form a gap. The third one pairs with the one at the beginning of the next line.

③

This will output `It's not enough to speak, but to speak true.`

7.4. Numbers

The Prelude defines a few basic numeric types:

Fixed sized integers

Arbitrary precision integers

Single precision floating and

Double precision floating

Other numeric types such as rationals and complex numbers are defined in libraries. The [class Num](#) of numeric types is a subclass of since all numbers may be compared for equality. Its subclass Real library is also a subclass of since the order comparison operations apply to all but complex numbers.

7.4.1. Numeric operators

The following [operators](#) for arithmetic computations are defined in the Prelude:

```
:: Integral => a -> b -> a :: Integral => a -> b -> a :: Floating a => a -> a  
-> a
```

```
:: Num a => a -> a -> a :: Fractional a => a -> a -> a quot :: Integral a =>  
a -> a -> a :: Integral a => a -> a -> a :: Integral a => a -> a -> a ::  
Integral a => a -> a -> a
```

```
:: Num a => a -> a -> a :: Num a => a -> a -> a
```

and `(**)` are exponent operators. Note that ``mod`` are usually used as [infix](#)

7.4.2. Numeric functions

In addition, the following functions are also defined in the Prelude for numeric types:

```
subtract    :: (Num a) => a -> a -> a
even, odd   :: (Integral a) => a -> Bool
gcd         :: (Integral a) => a -> a -> a
lcm        :: (Integral a) => a -> a -> a
fromIntegral :: (Integral a, Num b) => a -> b
realToFrac  :: (Real a, Fractional b) => a -> b
```

What these functions do should be rather self-evident even if you haven't used Haskell before. `gcd` and `lcm` stand for greatest common divisor and least common multiple, respectively. Note that the distinction between operators and functions is rather subtle in Haskell. This is discussed later in the [Expressions](#) chapter.

7.5. The Unit Datatype

The unit type `()` is an enumeration with one nullary constructor. Type `()` is an instance of `Enum` and `Eq`.

```
ghci> [(()) == (), () /= ()]
[True, False]
ghci> [minBound :: (), maxBound :: ()]
[(()), ()]
ghci> fromEnum () :: Int
0
ghci> toEnum 0 :: ()
()
```

7.6. Maybe

The Maybe datatype, defined in the Prelude, consists of two constructors Nothing and Just

```
data Maybe a = Nothing | Just a
  deriving (Eq, Ord, Read, Show)
```

The Maybe type derives from and In addition, Maybe is an instance of classes and

The Prelude also includes maybe function, which takes a value a function and a value of Maybe type and returns the first value n if the Maybe value is Nothing or f x if the Maybe value is Just

```
maybe :: b -> (a -> b) -> Maybe a -> b
```

For example,

```
ghci> maybe 0 (+ 10) Nothing
0
ghci> maybe 0 (+ 10) (Just 2)
12
```


7.7. Either

The Either datatype consists of two constructors Left and Right and it derives Eq, Ord, Read, Show from them.

```
data Either a b = Left a | Right b
  deriving (Eq, Ord, Read, Show)
```

The either function takes two functions and a value of type Either a b and it invokes the first function or the second function depending on whether the given value is the Left or Right variant, respectively.

```
either :: (a -> c) -> (b -> c) -> Either a b -> c
either f g (Left x) = f x
either f g (Right y) = g y
```

For example,

```
ghci> either (* 2) (+ 10) (Left 3)
6
ghci> either (* 2) (+ 10) (Right 5)
15
```

7.8. Ordering

```
data Ordering = LT | EQ | GT
  deriving (Eq, Ord, Enum, Bounded, Read, Show);
```

The Ordering datatype is used to represent "greater than", "less than", and "equal to" relationships. For example,

```
ghci> :{
ghci| cmp :: Int -> Int -> Ordering
ghci| cmp x y
ghci|   | x > y = GT
ghci|   | x < y = LT
ghci|   | otherwise = EQ
ghci| :}
ghci> [cmp 1 3, cmp 3 1, cmp 3 3]
[LT,GT,EQ]
```

7.9. Bottom

The pseudo-type "Bottom" `_|_` is a subtype of all types in Haskell. It is an empty type. That is, it does not have a value of its own kind. The bottom refers to a computation which does not return a value in Haskell, e.g., due to some kind of errors, or because the computation never terminates (and, hence does not return a value). The [undefined value](#) can be used in situations where a value of bottom is needed.

7.10. The IO Type

The IO type serves as a tag for operations (actions) that interact with the outside world. IO is a [unary type](#) and it is an [abstract No data constructors](#) are visible to the user. IO is an [instance](#) of the [Functor](#) and [Monad](#) classes. We discuss the [basic I/O](#) and [I/O-related functions](#) at the end of the book.

7.11. The IOError Type

IOError is also an [abstract](#) representing errors raised by [I/O](#). It is an [instance](#) of the [Show](#) and [Eq](#) classes. Values of this type are constructed by various [I/O](#) including the [userError function](#) defined in the Prelude.

8. Expressions

Haskell is based on lambda calculus. But, as a high-level programming language, it provides syntax for expressions and what not. In the following few chapters, we describe the syntax and informal semantics of Haskell expressions.

8.1. Variables

Haskell, as a pure functional programming language, has no concept of "updating". That is, a value does not contain any mutable state.

Variables are bound to values via the [pattern binding](#). The same variable can be bound to different values, even within the same scope. The new binding "shadows" the earlier bindings.

8.2. Literals

In Haskell, numeric literals are polymorphic.

An integer literal is a syntactic shorthand for applying `fromInteger` to the given value of type

A floating point literal is a shorthand notation of an application of `fromRational` to the given value of type

8.3. Operators

Haskell provides special syntax for "operators". An operator is a function that can be applied using infix notation, or partially applied using a An operator is either an operator symbol, e.g., or is an ordinary identifier in back quotes, e.g., That is, `x `op` y` is semantically equivalent to `op x` In reverse, an operator symbol can be converted to an ordinary identifier by enclosing it in parentheses.

Haskell's "builtin" operators (e.g., from the Prelude) have the following [fixity declarations](#) (operator precedence and associativity):

```
infixr 9  .                               ①
infixr 8  ^, ^^, **
infixl 7  *, /, `quot`, `rem`, `div`, `mod`
infixl 6  +, -
infix  4  ==, /=, <, <=, >=, >
-- infixr 5  :                               ②
infixr 3  &&
infixr 2  ||
infixl 1  >>, >>=
infixr 1  ==<<
infixr 0  $, $!, `seq`
```

①

This is a [function composition](#) In Haskell, the [function application](#) syntax (which is not an operator) has the highest precedence (it's

literally off the chart), and it is left-associative. The next in line is the function composition, which is right-associative (as indicated by

②

The [cons operator](#) : is also a builtin syntax, and not a declared operator. But, if a fixity declaration were given, it would be infixr 5 The [fixity declaration](#) syntax (e.g., for user-defined operators) is explained later in the book.

A lot of beginning Haskell programmers find Haskell difficult. They generally attribute this difficulty to FP. That is, however, most likely not the case. The initial difficulty that beginners face is the syntax, not the functional For instance, these fixity rules are, although trivial in a sense, one of the most difficult to learn, or to get used to. In imperative programming, this is not that significant, in which we rarely use long expressions. In functional programming, on the other hand, we deal with (only) expressions. Sometimes, long expressions. Despite this, or possibly because of this, the use of parentheses are generally discouraged in Haskell when they are not necessary. Therefore, you will have to know these fixity rules by heart to be able to read (and, write) Haskell code.

8.4. Errors

Errors during expression evaluation, denoted by `⊥` are indistinguishable by a Haskell program from non-termination. Since Haskell is a non-strict language, all Haskell types include `⊥`. That is, a value of any type may be bound to a computation that, when demanded, results in an error. When evaluated, errors cause immediate program termination and cannot be caught by the user.

8.5. The error and undefined Functions

8.5.1. The error function

error stops execution and displays an error message.

```
error :: String -> a
```

8.5.2. The undefined value

When undefined is used, the error message is created by the compiler.

```
undefined :: a  
undefined = error "Prelude.undefined"
```

9. Functions

A function is an abstract type, and they do not have constructors. A function value is created by declaring its name, zero or more parameters, and an equal sign followed by an expression, which is the definition of the function. All function names must start with a lowercase letter or For example,

```
incrBy1 :: Int -> Int ①  
incrBy1 x = x + 1     ②
```

①

A [type](#) immediately preceding the [function](#)

②

This notation suggests that if you [apply the function incrBy1 to](#) its value will be $x +$

9.1. Function Applications

Function application is written as, `e1 Application` associates left. That is, `x y z` is equivalent to `(x y)` for instance. This syntax is somewhat unusual in that, in mathematics, and in fact in the vast majority of programming languages, function application uses the parentheses notation. However, the Haskell syntax, based on lambda calculus, is the most efficient notation for function application, which is at the heart of everything else in Haskell.

For example,

```
f1 :: Int -> Int -> Int -> Bool
f1 x y z = (x > y) && (y > z) ①

main = do ②
  print $ f1 5 4 3 ③
  print $ f1 3 3 1 ④
```

①

As described in the [Nested Declarations](#) chapter, a [function binding](#) uses patterns. In this example, the triple `x y z` after the function name is an (implicit) [tuple pattern](#) comprising three [variable](#). This is an [irrefutable](#) meaning that any valid application will match this clause, and we do not need, and cannot have, any other clauses below this line.

②

As indicated the value `main` has a polymorphic type [IO](#). In all examples in this book, which is also generally the case in practice, the type of `main` is almost always `IO`. Hence, we will generally omit the type signature for `main` in this book. The [do notation](#) is explained near the end of the book, in the context of the I/O. But, in effect, `do` allows us to use "imperative style" programming. In this example, the `do` expression includes two `print` expressions, which are processed sequentially one after the other. Note that we almost always use the [layout-sensitive coding](#). That is, the curly braces enclosing these two `print` expressions in this example are omitted by using the indentation rules.

③

An example of function application, `f1 5 4`. Note the similarity between the function binding pattern and the function application syntax. This application evaluates to `in this example`. `print` is one of the [builtin I/O functions](#) that we use throughout this book without first defining them. It prints the given value to the terminal. The lazy infix application operator `$` is explained later in the [Core Functions](#) chapter. Since function applications are left-associative, `print f1 5 4 3` would have had a different meaning (and, in fact, syntactically invalid). We could have done `print (f1 5 4)` but the syntax with fewer parentheses is generally preferred in Haskell.

④

`f1 3 3 1` evaluates to `As we will discuss the f1 function can be either`

viewed as taking three arguments (and returning a value), or it can be viewed as taking one argument (and returning a function). $f1\ 3\ 3$ $(f1\ 3)\ 3$ and $((f1\ 3)\ 3)\ 1$ are all syntactically equivalent, and they are also semantically equivalent through

9.2. Operator Applications

Application of a binary operator `op` on `e1` and `e2`, e.g., `(op) e1 e2` can be written as infix application, `e1 op e2`. Likewise, application of a binary function, e.g., `f e1 e2` can be also written with an infix form, `e1 `f` e2`. Note that, lexically, [operators](#) belong to two categories, operator symbols and ordinary identifiers.

Here are a couple of example functions to demonstrate the infix-based function application syntax:

```
(+*+) :: Int -> Int -> Int
x +*+ y = x + 2 * y           ①
mold :: Int -> Int -> Int
x `mold` y = x * (y + 2)     ②
```

①

Alternatively, `(+*+) x y = x + 2 * y`. Note that Haskell allows defining any arbitrary operators, in particular, using operator symbols. But, as the saying goes, with the great power comes the great

②

Or, `mold x y = x * (y +`

Then, we can use them as follows, for instance:

```
main = do ①  
  print $ 5 ++ 10 ②  
  print $ (++) 10 5  
  print $ mold 1 2  
  print $ 2 `mold` 1
```

①

As indicated, the main function signature `main :: IO ()` is always omitted in this book.

②

These four print function applications will output and to the terminal.

9.3. Lambda Abstractions

Functions can also be declared anonymously. For example, an expression, `\x -> x *` defines a function which takes one argument and returns its squared value. Anonymous functions, also called lambdas or lambda expressions, are useful for simple functions that need not be separately declared first.

As with (regular) functions, a lambda is just a value in Haskell, which has a function type. For example,

```
squareAll :: [Int] -> [Int]
squareAll = map (a -> a * a) ①
biggerThan :: [Int] -> ([Int] -> [Int]) ②
biggerThan n = xs -> filter (> n) xs ③
```

①

The [map function](#) takes two arguments. In this example, only one (e.g., a lambda function) is given. This is called the partial application. It is useful for [currying](#) and for example.

②

Note that the part in the parentheses in this type signature is the type of the lambda function on the right hand side of the function binding in the

next line. The parentheses in this example is redundant, as we discuss next.

③

This is for illustration only. Lambdas are typically declared at the point of use, and they are rarely given names. Note that, by convention, the variables that end with s are E.g., zss could refer to a list of lists (because it ends with two s). The builtin [filter function](#) is discussed later. (> n) is a

A general lambda abstraction can be written as

```
p1 ... pn -> e
```

where the p_i are Note that the backslash character in the lambda syntax is supposed to represent the Greek Lambda character. An example lambda function with two arguments:

```
main = do
  let lamb = x y -> 2 * x + y      ①
  print $ lamb 5 10              ②
```

①

Again, for illustration only. This [let binding](#) with a lambda function is the same as a function binding, `lamb x y = 2 * x +` Note that, unlike in the case of regular functions, a lambda function cannot have more than

one pattern clause.

②

This will print out 20 to the terminal.

9.4. Curried Applications

As indicated, function applications are left-associative in Haskell, and a function that takes n arguments, e.g., $f\ e_1\ e_2\ \dots$ is equivalent to a function that takes $n-1$ arguments, e.g., $g\ e_2\ \dots$ if $f\ e_1 ==$ The expression $f\ e_1$ is called partial

Hence, f can be viewed as a function that takes one argument and returns a function that takes $n-1$ arguments ... Likewise, function application of g that takes $n-1$ arguments, $g\ e_2\ \dots$ is equivalent to $h\ e_3\ \dots\ e_n$ if $g\ e_2 ==$ Therefore, again the function g can be viewed as a function that takes one argument and returns another function that takes $n-2$ arguments ... We can continue this process down to the level where the last function takes one argument and returns a simple value (e.g., a function takes zero arguments).

(In pure functional programming languages like Haskell, a function that takes zero arguments must return a constant value. There are no other options, unlike in other impure languages, as you can easily convince yourself. Hence, there is a one-to-one correspondence between a simple value and a nullary function that returns that value. In fact, they are equivalent in Haskell.)

Converting a function that takes n arguments, $n \geq 1$ to a functional form that takes one argument and returns one value, i.e., a function, is called "currying". In Haskell, there is little difference between these two forms, and in fact we do not need "conversion". Syntactically, Haskell does not really distinguish these two interpretations. Therefore, we consider all functions in Haskell take one argument and return one value. This is manifested, for example, in the function type notations. All functions in Haskell are curried functions.

9.4.1. An informal illustration

As an example, let's consider the following three functions, and which have different arities, e.g., 1, 2, and 3, respectively.

```
f1 :: Int -> Int
f1 c = 5 + 3 * c

f2 :: Int -> Int -> Int
f2 b c = 1 + 2 * b + 3 * c

f3 :: Int -> Int -> Int -> Int
f3 a b c = a + 2 * b + 3 * c
```

As indicated, the [function application](#) is left-associative, whereas the arrows in the function [type signatures](#) associate right in Haskell. (This illustration will show you why that is chosen to be the case.)

The type signature of f3 is, therefore, equivalent to $f3 :: Int \rightarrow (Int \rightarrow Int \rightarrow Int)$. In this (curried) interpretation, the f3 function takes one argument of type Int and returns one value of type Int -> Int -> which happens to be the type of the function

The type of f2 is $f2 :: Int \rightarrow (Int \rightarrow Int)$ which indicates that f2 takes one value of Int and returns one value of Int -> which happens to be the type signature of The f1 function also takes one value (of type Int) and returns

one value (of type

We have deliberately chosen the implementations of these three functions. Now, let's trace back. The f3 function takes three arguments and returns one value, in the conventional (non-curried) view:

```
f3 :: Int -> Int -> Int -> Int ①  
f3 a b c = a + 2 * b + 3 * c
```

①

Haskell could have chosen different notations for multi-argument functions (e.g., something like $(Int, Int, Int) \rightarrow$ but they didn't. The illustration in this section will convince you why that was not necessary.

This is, however, equivalent to

```
f3 :: Int -> (Int -> Int -> Int)  
(f3 a) b c = a + 2 * b + 3 * c
```

That is, the partial application $f3\ a$ is a function that takes two Int arguments and returns an Int value. $f3\ a$ happens to be the same as $f2$ when a happens to be Likewise,

```
f2 :: Int -> (Int -> Int)  
(f2 b) c = 1 + 2 * b + 3 * c
```

The partial application `f2 b` is a function that takes an `Int` value and returns an `Int` value. `f2 b` happens to be the same as `f1` when `b == 2` (again, in this deliberately constructed example). That is,

```
f1 :: Int -> Int
f1 c = 5 + 3 * c
```

Hence, there is no difference between which takes two arguments `b` and `c` and returns one `Int` value and (`f2` which returns a function that takes one argument `c` and in turn returns an `Int` value. Likewise, there is no difference between which takes three arguments and `c` and returns one `Int` value and (`f3` which returns a function that takes two arguments `b` and `c` and returns an `Int` value.

Note also that the left-associativity of function applications and the right-associativity of arrows in the function types dovetail well with each other. (Notice the respective positions of the (optional) parentheses we've added in these examples.)

9.5. Sections

Sections are a syntactic shorthand for partial application of binary operators. For example, using the multiplication `*` operator,

```
triple = (*) 3 ①  
main = do  
  print $ triple 10 ②
```

①

`triple` is a function that takes one argument since the other argument (of the binary has been [partially applied](#) with a value. Note that this pattern binding is essentially equivalent to a function binding with one clause, `triple x = ((*) 3) x` (which is in turn equivalent to `triple x = 3 * x`). Its type signature is `triple :: Int -> Int -> Int`. As one can easily see, the syntactic difference between [pattern bindings](#) and [function bindings](#) are somewhat superficial.

②

This will print

Now, using `triple` instead of `(*) 3` has some syntactic convenience since we do not have to use many parentheses, e.g., `triple 10` vs `((*) 3) 10`. Section

provides this syntactic convenience without having to create a new binding. For example, this triple function can be written as $(\lambda x y z. x (y z))$ (Note the order.)

Another, possibly more important, advantage of sections is that we can supply the argument either on the left or right hand side, unlike in the case of general [partial](#) in which arguments are consumed from left to right. That is, $(op\ e1)$ and $(e1\ op)$ are generally two different sections. (Multiplication happens to be commutative, and hence $(e\ *)$ and $(*\ e)$ are effectively the same function.)

Formally, given a binary operator op and an expression e a right section is written as

```
e op 1
```

①

This is equivalent to the normal partial application form, $(op\ e)$ (Note the difference between the infix and prefix notations.)

Likewise, a left section for op and e is written as

```
op e 1
```

①

This form has no corresponding partial application form.

The right section $(e \text{ op})$ is syntactically valid if and only if $(e \text{ op } x)$ parses in the same way as $((e) \text{ op } x)$. Likewise, the left section $(\text{op } e)$ is syntactically valid if and only if $(x \text{ op } e)$ parses in the same way as $(x \text{ op } (e)$

9.6. Function Composition

Function composition plays an essential role as [function application](#) in Haskell. The builtin function composition operator `.` composes two given functions.

```
(.) :: (b -> c) -> (a -> b) -> (a -> c)
```

Composing a function $h \rightarrow$ with $g \rightarrow$ i.e., $g \cdot$ yields a function from a to $c \rightarrow$ (Note the order.)

$(g \cdot h) x$ is defined to be $g (h x)$. That is, if we set $f = g \cdot$, then $f x = g (h x)$. Note that a function (partial) application $g h$ would have associated left. That is, for a given argument the function application would have been $(g h) x$ or $g h x$ (which is syntactically invalid in this example). On the other hand, $g \cdot h$ applied to x would yield a different value, $g (h x)$. For example,

```
fnOne :: Int -> Int
fnOne x = x + 1
fnTwo :: Int -> Int
fnTwo x = 2 * x
fnCombo :: Int -> Int
fnCombo = fnTwo . fnOne

main = do
  print $ (fnTwo . fnOne) 3
```

```
print $ fnCombo 3
```

②

①

This will print

②

The same. Note that $\text{fnCombo } x = 2 * (x +$ The power of function composition often comes from the fact that we can manipulate, and compute, functions without applying them first to any specific values.

10. Lists

The list literal, `[e1, ..., ek]`, represents a list of k expressions, e_1, \dots, e_k . The empty list is denoted `[]`.

In Haskell, the list data constructor is a special operator `:` (or, "cons"). Lists are an instance of classes, and [Standard operations on lists](#) defined in the Prelude are included later in the book.

10.1. List Constructors

Lists are an algebraic datatype with two constructors, albeit with special syntax. The first constructor is the null list, written `[]` ("nil"), and the second is `:` ("cons"). For example,

```
main = do
  let a = [] :: [Int]           ①
      print a
      let b = 1 : ([] :: [Int]) ②
          print b
          let c = 'a' : ['d', 'e', 'f'] ③
              print c
              let d = 'g' : c          ④
                  print d
```

①

A nil constructor for `[Int]` list. `a` is an empty list of type `[Int]`. The `print` function in the next line will print

②

A cons constructor with two arguments, `1` and an empty `[Int]` list. `b` is

③

A cons constructor with `'a'` and a `[Char]` list, `['d', 'e', 'f']`. `c` is `['a', 'd', 'e', 'f']`.

④

Another cons constructor example. d is

Note that, for example, [1, 2, 3, 4] is the same as 1 : 2 : 3 : 4 : which is the same as 1 : (2 : (3 : (4 : (The [builtin cons operator](#) is right-associative.) In general, a list literal is a shorthand for the constructor expressions with each element subsequently added to the head.

```
main = do
  print $ 'L' : 'i' : 's' : 't' : [] ①
```

①

This will print

10.2. Enumerations

Haskell supports a special syntax for creating a list with enumerable elements. This is called the "arithmetic sequences" (or, "ranges" or "enumerations", etc.). Syntactically, it can take one of the following four forms:

```
[ exp1 .. ]  
[ exp1, exp2 .. ]  
[ exp1 .. exp3 ]  
[ exp1, exp2 .. exp3 ]
```

That is, `exp2` and `exp3` are optional, while it requires `[exp1 ..`. The expressions, and should be of type which is an instance of class `Any` of these arithmetic sequences denotes a list of type `They` are defined as follows:

`[exp1 ..]` == `enumFrom exp1`

`[exp1, exp2 ..]` == `enumFromThen exp1 exp2`

`[exp1 .. exp3]` == `enumFromTo exp1 exp3`

`[exp1, exp2 .. exp3] == enumFromThenTo exp1 exp2 exp3`

When `exp3` is omitted, it is assumed to be the biggest element for the given Enum type. Otherwise, the semantics of arithmetic sequences are entirely dependent on the type. In cases of numeric types, `exp1` is the first element, and `exp2 - exp1` represents the "step". For example,

```
main = do
  print [5 .. 10]           ①
  print [2, 4 .. 11]       ②
  print $ take 5 [1 .. ]   ③
  print $ take 5 [2.0, 5.0 .. ] ④
```

①

This will print `[5,6,7,8,9,10]`. Note that the last element is inclusive.

②

This will print `[2,4,6,8,10]`.

③

This will print `[1,2,3,4,5]`. Note that `[1 ..]` is an infinite list, with the Integer element type.

④

This will print `[2.0,3.0,4.0,5.0,6.0]`.

Another example, using Char elements,

```
main = do
  print ['d' .. 'h' ]           ①
  print ['d', 'f' .. 'k' ]     ②
  print $ take 10 ['w' .. ]    ③
  print $ take 10 ['t', 'v' .. ] ④
```

①

This will print

②

This will print

③

This will print Note that Char type is bounded. That is, ['w' ..] is not an infinite list.

④

This will print

10.3. List Comprehensions

List comprehensions are now widely supported by many different programming languages, including Scala and Python.

A list comprehension in Haskell has the following general syntax:

```
[ exp | q1, ..., qi, ..., qn ]
```

Here n is equal to, or bigger than, and each qualifier q_i can be one of the following three forms:

Generators of the form $\text{pat} \leftarrow \text{exp}$ where pat and exp are patterns and expressions of types t and respectively,

Boolean expressions known as to filter preceding generators, and

Local let bindings that are to be used in the generated expression exp or subsequent boolean guards and generators.

A list comprehension evaluates the target expression exp in the

successive environments, from left to right, which are created by evaluating the generators in the qualifier list.

Note that, in the list comprehension, pattern matching in a generator is simply used for filtering. That is, if a match fails then that element of the list is just excluded from the resulting list.

Here are some examples:

```
main = do
  let c1 = [x * x | x <- [1 ..]]      ①
  print (take 5 c1 :: [Integer])    ②
```

①

An infinite list of squared integer values. This list comprehension includes one generator, `x <- [1 ..]` which uses the [enumeration](#)

②

This will output `[1,4,9,16,25]` to the terminal.

```
divisors :: Int -> [Int]
divisors n = [d | d <- [1 .. n],
               n `mod` d == 0]      ①

main = do
  print (divisors 10, divisors 12)  ②
```

①

A Boolean guard. This guard is used as a filter for the "divisors" of the given Int argument.

②

This line will print

```
main = do
  let c2 =
    [ (a, b)
    | a <- [1 .. 5] :: [Int]
    , b <- [1 .. 5] :: [Int]
    , let s = a + b           ①
    , s >= 3                 ②
    , s <= 4                 ③
    ]
  print c2                   ④
```

①

A local let binding, whose value is used in the subsequent guards.

②

A Boolean guard.

③

Another guard. These two guards could have been combined as one guard `s >= 3 && s <= 4` in this example.

④

The output:

11. Tuples

Tuples are algebraic data types with special syntax, (e_1, \dots, e_n) . A tuple size must be equal to, or greater than, but there is no preset upper bound, other than practical limitations. A compliant Haskell implementation is required to support tuples up to size

All tuples are instances of `Eq` and that is, as long as all their component types are.

For example,

```
apply :: (t -> a, t -> b) -> t -> (a, b)
apply (f1, f2) list = (f1 list, f2 list)

main :: IO ()
main = do
  print (True, 'A', "Haskell") ①
  print $ apply (head, tail) [1, 2, 3] ②
```

①

`(True, 'A', "Haskell")` is a 3-element tuple of a `Bool` and a `Char` and a `String`

②

(head, tail) is a 2-element tuple of functions. Note the definition of apply which takes a pair of functions as its first argument.

11.1. Tuple Constructors

The constructor for an n-tuple is written as `(...)` with n-1 commas, e.g., by omitting the expressions surrounding the commas in an n-tuple. Hence, for instance, `(,,) a b c` constructs a tuple `(a, b,`

Likewise, the [tuple type constructor](#) has a similar syntax, as described earlier in the book. For instance, `(,,) Bool Char Int` denotes the same type as `(Bool, Char,`

As an example,

```
main = do
  let x = (,,) 'a' True 'z' ①
  print x ②
```

①

Variable x has a type `(Char, Bool, or (,,) Char Bool`

②

This will print

11.2. Tuple Functions

The following functions are defined in the Prelude for pairs (2-tuples):

```
fst    :: (a,b) -> a
snd    :: (a,b) -> b
curry  :: ((a, b) -> c) -> a -> b -> c
uncurry :: (a -> b -> c) -> (a, b) -> c
```

11.2.1. The fst and snd functions

The `fst` function takes a pair and it returns its first element, e.g., `fst (x,y)` returns

The `snd` function takes a pair and it returns its second element, e.g., `snd (x,y)` returns

For example,

```
main = do
  let pair = ("Hello", 42 :: Int)
  print $ fst pair           ①
  print $ snd pair          ②
```

①

The output: "Hello"

②

The output: 42

11.2.2. The uncurry and curry functions

The uncurry function takes a (curried) function that accepts two arguments and converts it to a function which takes a single argument of a pair type. That is, `uncurry f pair` is defined to be `f (fst pair) (snd pair)` (Note that, since [function applications](#) are left-associative, `uncurry f pair` is the same as `(uncurry f) pair`)

The curry function converts an uncurried function that takes a pair into a (regular) curried function. That is, `curry ucf x` or `(curry ucf) x` is defined to be `ucf (x,`

For instance,

```
addFn :: Int -> Int -> Int           ①
addFn a b = a + 2 * b

uncurriedAddFn :: (Int, Int) -> Int  ②
uncurriedAddFn = uncurry addFn

pairFn :: (Int, Int) -> Int          ③
pairFn (a, b) = 2 * a - b

curriedPairFn :: Int -> Int -> Int   ④
curriedPairFn = curry pairFn
```

①

A "regular" function.

②

An uncurried version of

③

A function that takes a pair.

④

A curried version of

Here are a few simple examples of using these functions:

```
main = do
  print $ addFn 1 2           ①
  print $ uncurriedAddFn (1, 2) ②
  print $ pairFn (1, 2)      ③
  print $ curriedPairFn 1 2  ④
```

①

The output: 5

②

The same output: 5

③

The output: 0

④

The same output: 0

11.3. The Unit and Parenthesized Expressions

The unit expression `()` has type whose only member is `()` (other than the bottom `()` can be thought of as the "nullary tuple" (with zero elements). (That is, the unit notation using the tuple-like syntax is not a coincidence.)

Haskell does not support one-element tuple types unlike in some other programming languages. The form `(exp)` is simply a parenthesized expression, and it is equivalent to `exp`. From the viewpoint of algebraic data types, a single element tuple type is no different from the element type itself. That is, a (hypothetical) type `(t)` must be the same type as `t` and a single element tuple cannot be a distinct type in Haskell.

12. Expression Type Signatures

Expression type signatures have the following two forms:

```
exp :: t
exp :: cx => t
```

where `exp` is an expression and `t` is a type. The context `cx` is optional, as in normal [type signature](#)

Expression type signatures may be used

To explicitly type an expression, or

To resolve ambiguous typings due to

As with normal type signatures,

The declared type may be more specific than the principal type derivable from but

It is illegal to give a type that is more general than, or not comparable to, the principal type.

For example,

```
addTwoNums :: Num a => a -> a -> a ①
addTwoNums x y = x + y

main = do
  print $ addTwoNums (1 :: Int) 2 ②
  print $ addTwoNums (1.0 :: Float) 2.0 ③
  -- addTwoNums (1 :: Int)(2 :: Integer) ④
```

①

A [type signature](#) for the `addTwoNums` function. Note that it uses the most general type which supports addition `+` for the operands and return values. This is also the function's principal type.

②

The integer `1` is polymorphic, but we explicitly declare it as `Int` using the expression type signature syntax. Note that, in this example, `2` is also of the `Int` type (without requiring another explicit expression type signature).

③

Likewise, `1.0` and `2.0` are both of the `Float` type.

④

This will cause a compile error since the type annotation is not consistent with the type signature of the `addTwoNums` function.

Here's another example, in which ambiguity arises as to what type Haskell is supposed to use for an expression whose type is not explicitly specified in the type signature declaration. This is the so-called "show . read" problem.

```
readAndShow :: String -> String
-- readAndShow x = show (read x)           ①
readAndShow x = show (read x :: Int)      ②

main = do
  print $ readAndShow "300"              ③
  print $ readAndShow "abc"              ④
```

①

Haskell cannot compile this function because it does not know the type of `read`. We must limit the type through an annotation.

②

We use an explicit expression type signature to indicate that the type of `read x` is `Int`. Note that because of the precedence rules, `read x :: Int` is the same as `(read x) :: Int`. The [function application](#) binds most tightly in Haskell.

③

This will print

④

This will return an error, type: Prelude.read: no

13. Let and Where

13.1. The let - in Expression

A let expression introduces a nested and possibly mutually-recursive list of declarations, with the following general form:

```
let { d1 ; ... ; dn } in exp
```

Here, `exp` is an expression. The value of `exp` is the value of the overall let expression.

Each declaration `di` is translated into an equation of the form `pi = ei` where `pi` and `ei` are [patterns](#) and expressions, respectively. The let declarations are lexically-scoped.

For example, in its simplest form,

```
multiples :: Int -> [Int]
multiples x =
  let mult n = n * x           ①
      in map mult [1 .. 10]    ②

main = do
  print $ multiples 10        ③
```

①

This let expression binds `mult n` to an expression `n *`

②

This "local function" `mult` is used in the expression of the `in` part. The [map function](#) is a list function defined in the Prelude, and it is described later in the [list functions](#) chapter.

③

This will print

13.1.1. Deconstruction

As another example, a pattern on the left hand side of a declaration in a `let` expression can be used to destructure the expression on the right hand side of the declaration.

For instance, the following function would extract the first two characters from a string whose length is at least 2:

```
firstTwoChars :: String -> [Char]
firstTwoChars str =
  let (a:b:_) = str ①
      in "First two chars: " ++ [a, ',', b]

main = do
  print $ firstTwoChars "hello world" ②
```

①

`str` needs to have at least 2 characters for this pattern to work.

②

This will print "First two chars:

13.2. Where Clauses

Similar to where can be used to declare bindings in [function declarations](#) and [case](#). For example,

```
summation :: Int -> Int
summation m = aux m 0
  where ①
    aux n acc ②
      | n <= 0 = acc
      | otherwise = aux (n - 1) (n + acc)

main = do
  print $ summation 10 ③
```

①

A "local function" aux is declared in the where clause. Note that the aux function is "tail recursive".

②

acc is an

③

This will print

Unlike let bindings, the scope of the where bindings can extend over

several guarded equations. For instance,

```
piecewise :: Float -> Float -> Float
piecewise x y
  | y > z = z           ①
  | y < z = -z          ②
  | otherwise = 0
  where                ③
    z = x * x

main = do
  print $ piecewise 3 16  ④
  print $ piecewise 4 16  ⑤
  print $ piecewise 5 16  ⑥
```

①

z is defined in the where clause below.

②

The same z is used in a different guarded equation. Note that this cannot be done with a let expression, which only scopes over the expression which it encloses.

③

Note that where is part of the syntax of function declarations and case expressions, and they do not for separate expressions like let expressions.

④

This will print

⑤

This will print

⑥

This will print

14. Conditional Expressions

A conditional expression has the form `if e1 then e2 else e3`. It first evaluates the Boolean expression `e1` and if its value is `True` or `False` then it returns the value of `e2` or `e3` respectively. Note that the type of `e2` and `e3` must be the same, which is also the type of the overall `if` expression.

For example,

```
summation :: Int -> Int
summation n =
  if n <= 0           ①
  then 0
  else n + summation (n - 1)

main = do
  print $ summation 10 ②
```

①

An `if - then - else` expression. Notice the layout. The `then` and `else` clauses have the same indentations.

②

This will print

This summation function is equivalent to the following definition, using the [Boolean](#)

```
summation' :: Int -> Int
summation' n
  | n <= 0 = 0
  | otherwise = n + summation' (n - 1)
```

15. Case Expressions

A case expression has the following general form:

```
case e of { p1 match1 ; ... ; pn matchn }
```

Each alternative $p_i \text{ match}_i$ consists of a pattern p_i and its match, Each match in turn consists of a sequence of pairs of guards g_{sij} and bodies e_{ij} (expressions), followed by optional where bindings,

```
| gs11 -> ei1  
...  
| gsimi -> eim  
  where declsi
```

When there is only one guard that always evaluates to e.g., $\text{pat} \mid \text{True} \rightarrow$ then it can be omitted for an alternative short hand form, $\text{pat} \rightarrow$

A case expression must have at least one alternative, and all bodies must have the same principal type, which is the type of the whole case expression.

A case expression is evaluated by pattern matching the expression e against the individual alternatives, from top to bottom. If e matches the pattern of an alternative, then the guarded expressions for that alternative are tried sequentially from top to bottom. If the guard succeeds, then the corresponding body is evaluated. If all guards fail, then this guarded expression fails and the next guarded expression is tried. If none of the guarded expressions for a given alternative succeed, then matching continues with the next alternative. If no alternative succeeds, then the value of the case expression is

The [conditional](#) `if e1 then e2 else` for example, can be written as follows, using the case expression:

```
case e1 of
  True  -> e2
  False -> e3
```

The [function declaration](#) using patterns is a shorthand syntax for using a case expression. That is, for instance,

```
f p11 ... p1k = e1
...
f pn1 ... pnk = en
```

This function definition for f is equivalent to the following:

```
f x1 x2 ... xk =  
  case (x1, x2, ..., xk) of ①  
    (p11, ..., p1k) -> e1 ②  
    ...  
    (pn1, ..., pnk) -> en
```

①

The matching expression is a [tuple](#) when $k \geq 1$ consisting of the function arguments, in the given order. Otherwise it's a [single](#)

②

The pattern on the left-hand side is a [tuple](#)

Here are a couple of examples:

```
not' :: Bool -> Bool ①  
not' x = case x of  
  True -> False ②  
  False -> True ③
```

①

The [not function](#) is defined in the Prelude, and hence we use a different name for illustration.

②

If a given argument evaluates to the not' function returns The value True in this example is called a [literal](#)

③

Otherwise, that is, when `x ==` it returns

This `not'` function is equivalent to the following:

```
not' :: Bool -> Bool
not' True = False
not' False = True
```

The above two definitions of the `not` function are semantically equivalent. Likewise, the following two definitions of the `isZero` function are equivalent to each other.

```
isZero :: Int -> Bool
isZero :: Int -> Bool
isZero x = case x of
  0 -> True           ①
  _ -> False         ②
```

①

If the value of `x` is then the `isZero` functions returns

②

Otherwise, it returns The underscore `_` is a [wildcard](#) and it matches any `Int` value in this example.

```
isZero' :: Int -> Bool
isZero' 0 = True
isZero' _ = False
```

Pattern matching is described in more detail in the [next](#)

16. Patterns

The [case expressions](#) are used with patterns, as described in the previous chapter. Patterns can also appear in [lambda function pattern list](#) and [do](#) which are all ultimately translated into case expressions.

16.1. Pattern Matching

Patterns are matched against values. Attempting to match a pattern can result in one of the following three results:

It may succeed, returning a binding for each variable in the pattern,

It may fail, or

It may diverge (i.e. return

Pattern matching proceeds from left to right, and outside to inside. We describe each of the valid patterns in Haskell in the following sections.

16.2. Wildcard Patterns

The wildcard pattern `_` is an [irrefutable](#) and it matches any value. It is similar to a [variable](#) but there is no binding. Hence, the `_` patterns are useful when some part of a pattern is not referenced on the right-hand-side. For example,

```
wildcardPatterns :: String -> Char
wildcardPatterns x =
  case x of
    "" -> ' '
    _ -> '!'
```

①

The wildcard pattern `_` matches any non-null string in this example.

16.3. Literal Patterns

A numeric, or String literal pattern p matches against a value v if $v == p$. In case of numeric literals,

An integer literal pattern can only be matched against a value in the class `Int` and

A floating literal pattern can only be matched against a value in the class `Double`

For example,

```
literalPatterns :: Int -> Int
literalPatterns x =
  case x of
    33 -> 30           ①
   -44 -> -50        ②
    _  -> 0
```

①

$x = 33$ matches this literal pattern. The value of the [case expression](#) is

②

$x = -44$ matches this negative number literal pattern. The case

expression returns -50 in this case.

16.4. Constructor Patterns

Haskell supports a few different forms of constructor patterns. The ["record pattern"](#) is described in the next section. A constructor pattern is a [nested](#) and the arity of a constructor must match the number of sub-patterns associated with it.

The pattern `F {}` matches any value built with constructor `F` whether or not `F` was declared with record syntax.

When the constructor is defined by matching the pattern `con pat1 ... patn` depends on the value:

If the value is of the form `con v1 ...` sub-patterns are matched from left to right against the components of the data value.

If all matches succeed, the overall match succeeds.

Otherwise, the first to fail or diverge causes the overall match to fail or diverge, respectively.

If the value is of the form `con' v1 ... vm` with `con` and `con'` two different constructors, then the match fails.

If the value is then the match diverges.

For example,

```
data Boring = Empty | Vacant

nullaryPatterns :: Boring -> Bool
nullaryPatterns x =
  case x of
    Empty -> True           ①
    _ -> False             ②

main = do
  print $ nullaryPatterns Empty  ③
  print $ nullaryPatterns Vacant ④
```

①

A nullary constructor pattern.

②

The wildcard pattern. In this particular example, it only matches the other nullary constructor `Vacant` of the `Boring` type. Hence, `_ -> False` is equivalent to `Vacant ->`

③

This will print `True` to the terminal.

④

This will print

```
consPatterns :: Either Int String -> Int
consPatterns x =
  case x of
    Left 1 -> 100           ①
    Right "Five" -> 500    ②
    _ -> 0

main = do
  print $ consPatterns $ Left 1      ③
  print $ consPatterns $ Right "Ten" ④
```

①

A constructor pattern. The [Either type](#) is defined with two data constructors, Left and

②

Another constructor pattern.

③

This will print

④

The argument Right "Ten" matches neither constructor pattern in this example, and hence it matches the wildcard pattern and the function returns

When the constructor is defined by the pattern con pat matches against a value as follows:

If the value is of the form `con` then `pat` is matched against

If the value is then `pat` is matched against

For example,

```
newtype Truth = Truth Bool ①

newtypePatterns :: Truth -> Int
newtypePatterns x =
  case x of
    Truth True -> 1000000 ②
    _ -> 0

main = do
  print $ newtypePatterns $ Truth True ③
  print $ newtypePatterns $ Truth False ④
```

①

A newtype `Truth` is created with Note that the `Bool` type has two nullary constructors, `True` and

②

A constructor pattern.

③

This will print

④

This will print

Binary data constructors can also use the infix syntax. For instance,

```
data Sum = Sum Int Int ①

infixPatterns :: Sum -> Int
infixPatterns x =
  case x of
    1 `Sum` 2 -> 3 ②
    _ -> 0

main = do
  print $ infixPatterns (Sum 1 2) ③
  print $ infixPatterns $ 1 `Sum` 2 ④
  print $ infixPatterns (Sum 2 2) ⑤
```

①

The type Sum has a single data constructor which takes two Int arguments.

②

An infix constructor pattern. This pattern 1 `Sum` 2 is equivalent to the normal constructor pattern Sum 1

③

This will print

④

Same as above. This will output 3 to the terminal.

⑤

This will print

16.5. Labeled Patterns

In the ordinary constructor patterns, pattern matching occurs based on the position of arguments in the value being matched. When matching against a constructor using [labeled](#) the fields are matched based on their names, and in the order they are listed in the pattern. Otherwise, these two constructor patterns work more or less the same way. Fields not named by the pattern are ignored. That is, they are matched against

```
data Color =  
  Color { red, gray, blue :: Int } ①  
  
labeledPatterns :: Color -> String  
labeledPatterns x =  
  case x of  
    Color {red = 0} -> "Not so red" ②  
    Color {blue = 255} -> "Full of blue" ③  
    _ -> ""  
  
main = do  
  print $ labeledPatterns  
    Color {red = 0, gray = 0, blue = 255} ④  
  print $ labeledPatterns  
    Color {red = 1, gray = 0, blue = 255} ⑤  
  print $ labeledPatterns  
    Color {red = 1, gray = 1, blue = 254} ⑥
```

①

A constructor with labeled fields. The [record syntax](#) is explained later in the book.

②

A labeled field constructor pattern. This pattern matches as long as the value of the field "red" is 0 regardless of values of other fields.

③

Another labeled pattern. This pattern matches as long as the value "blue" is

④

Since patterns are tested from top to bottom, this will match the first pattern `Color {red = 0}` in the case expression.

⑤

This will match the second labeled pattern, `Color {blue =`

⑥

This will match the wildcard pattern, which is an [irrefutable](#)

16.6. Variable Patterns

Pattern matching also allows values to be assigned to variables. For example, matching a pattern `var` against a value `v` always succeeds and binds `var` to `v`. This is called the variable pattern. It is similar to the [wildcard pattern](#) in that both are [irrefutable](#) that is, they will match any value.

For example,

```
variablePatterns :: Char -> String
variablePatterns x =
  case x of
    '0' -> "None found" ①
    c   -> "Found: " ++ [c] ②

main = do
  print $ variablePatterns 'a' ③
  print $ variablePatterns 'z' ④
```

①

A [character literal](#)

②

A variable pattern. This pattern will match any `x` other than the null character, in this example.

③

This will print "Found:"

④

This will print "Found:"

16.7. As-Patterns

Patterns of the form `var@apat` are called as-patterns, and allow one to use `var` as a name for the value being matched by. That is, matching an as-pattern `var@apat` against a value `v` is the result of matching `apat` against `v` and, if the match is successful, binding `var` to the result of matching `apat` against `v`. If the match of `apat` against `v` fails or diverges, then so does the overall match of the as-pattern. For example,

```
asPatterns :: String -> (Char, Int)
asPatterns x =
  case x of
    "" -> ('0', 0)
    w@(c:_) -> (c, length w) ①

main = do
  print $ asPatterns "Hello, world" ②
  print $ asPatterns "Bonjour le monde" ③
```

①

An as-pattern. The [pattern \(c:_\)](#) matches a string with at least one character, in this example, and it binds `c` to the first character of the matched string. The string itself is bound to a variable `w` through this as-pattern.

②

This will print `c` and `w` are bound to `'H'` and `"Hello, world"`, respectively.

③

This will print

16.8. Tuple Patterns

A tuple pattern provides a convenient syntax over what is essentially a [constructor Wildcard patterns](#) are often used to ignore certain elements in pattern matching. As [nested](#) other (sub-)patterns are also commonly used in the element positions of the tuple patterns. For example,

```
tuplePatterns :: (Int, Char, Bool) -> Int
tuplePatterns x =
  case x of
    (1, _, _) -> 1
    (_, c, True) -> fromEnum c
    _ -> 0

main = do
  print $ tuplePatterns (1, 'a', False) ①
  print $ tuplePatterns (2, 'A', True) ②
  print $ tuplePatterns (3, 'a', False) ③
```

①

The value (1, 'a', False) will match the first pattern, and this expression will print 1 to the terminal through [IO](#)

②

This will print The ASCII code of the English uppercase letter 'A' happens to be 65. fromEnum is a method of the [Enum](#)

③

This will print

16.9. List Patterns

Haskell also provides some convenient pattern syntax for matching lists, which essentially amounts to some variations of the [constructor](#) similar to how the [tuple patterns](#) work.

In particular, you can match with the `nil` constructor, or an empty list, or you can match with the `cons` constructor, where `x` represents a single element, or the "head", and `xs` refers to the rest of the list, or the "tail" list, which can be empty. The patterns like `(x:xs)` or etc. can only match lists with at least one element. (Note that [parentheses \(\)](#) are not part of the list patterns.) Alternatively, one can also use the complete `cons` pattern by repeatedly applying the `cons` operator on each of the elements in a list, e.g., or its syntactically sugared version, which will match a list with three elements.

Or, one can even use syntax somewhere between the two. For example, a pattern `(x:y:zs)` will match a list with at least two elements, with `zs` matching a list with zero or more elements after removing the first two elements in a value. For example,

```
listPatterns :: [Int] -> String
listPatterns x =
  case x of
    [] -> "Empty" ①
```

```

[c] -> "Uno: " ++ [toEnum c :: Char] ②
[c, d] -> "Dos: " ++ show (c, d) ③
(c:_) -> "Mas: " ++ show c ++ " etc" ④

main = do
  print $ listPatterns [] ⑤
  print $ listPatterns [100] ⑥
  print $ listPatterns [200, 250] ⑦
  print $ listPatterns [40, 50, 60, 70] ⑧

```

①

The empty list pattern [] matches an empty list.

②

The list pattern [c] will match any single element list. Note that the sub-pattern c included in this list pattern is a variable pattern, which is irrefutable.

③

The list pattern [c, d] will match any two-element list.

④

The pattern (c:_) will match any list with at least 1 element. In this example, however, it will match a list with 3 or more elements since the previous patterns match all lists with fewer than 3 elements.

⑤

This will print

⑥

This will print "Uno: The ASCII code of 'd' happens to be 100. toEnum is also a method of the [Enum](#)

⑦

This will print "Dos:

⑧

This will print "Mas: 40

Here are a few more examples of pattern matching in declaring some commonly used functions in Haskell programming, As stated, lists are one of the most important data structures in Haskell programming, and likewise, the list patterns are one of the most widely used patterns. Note that all three functions are defined recursively.

```
elem' :: (Eq a) => a -> [a] -> Bool ①  
elem' _ [] = False  
elem' e (x:xs) = (e == x) || elem' e xs ②
```

①

The elem' function takes two values of type a and a list type and it returns True if the first value is an element of the second value/list. Otherwise, it returns False. Note that the context specifies that a must be an instance of the [Eq](#)

②

Although we mostly use [case expressions](#) to demonstrate various patterns in this chapter, Haskell allows a special syntax for function declaration with pattern matching, [as indicated](#). This kind of function pattern binding syntax is more widely used, especially for simple functions. This particular function declaration is, for instance, equivalent to the following:

```
elem' :: (Eq a) => a -> [a] -> Bool
elem' ex list =
  case (ex, list) of
    (_, []) -> False
    (e, x:xs) -> (e == x) || elem' e xs ①
```

①

Note that, in the first example, the list pattern `x:xs` is enclosed in parentheses. This is because function application has a higher precedence than the cons constructor `:` in the pattern. In general, list patterns are often combined with [parenthesis patterns](#) because the [cons operator](#) has a generally rather low fixity. In this particular example, however, the parentheses are not needed since it is an element of a [tuple](#).

The following function, uses the `elem` function (e.g., from the Prelude), and removes all duplicates in a given list.

```
dedupe :: (Eq a) => [a] -> [a] ①
dedupe [] = [] ②
dedupe (x:xs) ③
  | x `elem` xs = dedupe xs
  | otherwise = x : dedupe xs
```

①

The `elem` function requires the type `a` to be an instance of the `Eq` class. Hence, `dedupe` has the same requirement.

②

We handle an empty list here.

③

Then, we can assume that all lists have at least one element at this point. This pattern includes two guards. The implementation is straightforward.

The following function, takes a list of elements of an [Ord type](#) and it returns `True` if all elements in the given list is sorted in the ascending order. Otherwise, it returns

```
isAsc :: (Ord a) => [a] -> Bool
isAsc [] = True
isAsc [_] = True
isAsc (x:y:xs) =
  (x <= y) && isAsc (y : xs)
```

①

When a list includes no elements, should it be considered sorted?

②

What about a list with one element?

③

At this point, we can assume that the list we are matching has at least two elements, and hence $x:y:xs$ is a valid pattern. (Note that xs can still be an empty list.)

④

The implementation is straightforward.

16.10. Parenthesized Patterns

Pattern matching can extend to nested values, e.g., as we have seen some examples so far, and as we will discuss further at the end of this section. Parenthesized patterns are used for grouping purposes. For example,

```
data Me = Me (Maybe Int) (Maybe String) ①

parenPatterns :: Me -> Int
parenPatterns x =
  case x of
    Me (Just n) (Just s) -> n + length s ②
    Me (Just n) _ -> n ③
    _ -> 0

main = do
  print $ parenPatterns $
    Me (Just 1) (Just "hi") ④
  print $ parenPatterns $
    Me Nothing (Just "hi")
  print $ parenPatterns $
    Me (Just 1) Nothing
  print $ parenPatterns $
    Me Nothing Nothing
```

①

A [data type](#) with one constructor, which consists of two fields.

②

Constructor patterns can be In this case, the overall pattern is a

[constructor](#) Both of its arguments are parenthesized patterns, each of which contains a constructor pattern.

③

Similarly, a constructor pattern with two sub-patterns, a parenthesized pattern over another constructor pattern and the [wildcard](#)

④

These four print expressions will output and 0 to the terminal.

16.11. Nested Patterns

Patterns can be nested. In particular, constructor patterns, list patterns, and tuple patterns, along with parenthesized patterns, can include other sub-patterns, some of which can in turn include other sub-patterns, and so on. Here are some more examples of nested patterns.

```
addTuples :: (Num a, Num b) =>
  (a, b) -> (a, b) -> (a, b) ①
addTuples (x1, y1) (x2, y2) = ②
  (x1 + x2, y1 + y2)
```

①

The `addTuples` function take two pairs and return their sum.

②

As indicated, this pattern is the same as a tuple of two tuples, with each tuple containing two variable patterns.

```
main = do
  print $ addTuples (1.0, 3) (2.0, 0) ①
```

①

This will print

```
data Point a b = Origin | Point a b ①
  deriving(Show)

addPoints :: (Num a, Num b) =>
  Point a b -> Point a b -> Point a b
addPoints Origin Origin = Origin ②
addPoints Origin (Point x2 y2) =
  Point x2 y2
addPoints (Point x1 y1) Origin =
  Point x1 y1
addPoints (Point x1 y1) (Point x2 y2) =
  Point (x1 + x2) (y1 + y2)
```

①

A datatype with two constructors.

②

All patterns in this function binding are tuples of two constructors, one of which comprises two variable patterns.

```
main = do
  print $ addPoints Origin Origin ①
  print $ addPoints Origin (Point 3 4.0) ②
```

①

This will print

②

This will print Point 3

```

addLists :: (Num a, Num b) =>
  [(a, b)] -> [(a, b)] -> [(a, b)] ①
addLists [] [] = []
addLists [] ((x2, y2):ws) = ②
  (x2, y2):ws
addLists ((x1, y1):zs) [] =
  (x1, y1):zs
addLists ((x1, y1):zs) ((x2, y2):ws) =
  (x1 + x2, y1 + y2) : addLists zs ws

```

①

This `addLists` function takes two lists of pairs and returns a list of pairs by adding their corresponding elements.

②

All four of these patterns are implicitly top-level tuple patterns (when converted to a case expression). In this particular case, the second element pattern is a list pattern enclosed in parentheses. The inner parentheses are part of the tuple pattern.

```

main = do
  print $ addLists [(1, 2)] [(2, 4), (6, 8)] ①

```

①

This will print `[(3,6),(6,8)]` to the terminal.

16.12. Irrefutable Patterns

The following patterns are irrefutable:

A variable pattern,

A wildcard pattern,

A [lazy](#) in the form of `where apat ia another pattern`, which is described further at the end of the section,

An as-pattern of the form `var@apat` where `apat` is irrefutable, and

`N apat` where `N` is a constructor defined by `newtype` and `apat` is irrefutable.

All other patterns are refutable. Matching an irrefutable pattern is non-strict. That is, the pattern matches even if the value to be matched is `Matching a refutable pattern is, on the other hand, strict. That is, if the value to be matched is then the match diverges.`

16.13. Lazy Patterns

A lazy pattern has the form where apat is another pattern, which may or may not be irrefutable.

Matching the pattern $\sim\text{apat}$ against a value v always succeeds. But, no actual matching evaluation is done on a $\sim\text{apat}$ pattern until one of the variables in apat is used. At that point the entire pattern is matched against the value, and the free variables in apat are bound to the appropriate values if matching apat against v would otherwise succeed. If the match fails or diverges, so does the overall computation.

17. Core Functions

The Haskell Standard Prelude includes a number of "builtin" functions.

17.1. The id Function

```
id :: a -> a
```

The builtin identity function `id` for a given value `x` returns the same value

```
main = do
  print $ id "Hello, Haskell!" ①
```

①

This will print "Hello,

17.2. The const Function

```
const :: a -> b -> a
```

The builtin constant function `const` takes two arguments, and it returns the value of the first argument, ignoring the second argument.

```
main = do
  print $ const 'a' 'b'           ①
  print $ const 42 "Irrelevant"  ②
```

①

This will print

②

This will print

17.3. The flip Function

```
flip :: (a -> b -> c) -> b -> a -> c
```

The builtin flip function takes a function of two arguments as an argument, and it return another function which works like the given function, but taking the two arguments in the reverse order. That is, flip $f\ x\ y = f\ y\ x$

```
fnPower :: Int -> Int -> Int
fnPower a b = a ^ b
fnPowerFlipped :: Int -> Int -> Int
fnPowerFlipped = flip fnPower

main = do
  print $ fnPower 2 3           ①
  print $ fnPowerFlipped 2 3   ②
```

①

This will print

②

This will print

17.4. The seq Function

```
seq :: a -> b -> b
```

The builtin `seq` function takes two arguments, and it makes both arguments to be evaluated. Its return value is the value of the second argument unless the first argument is in such a case it returns

```
_|_ `seq` b = |_|_  
a `seq` b = b
```

17.5. The Lazy Infix Application Operator

```
( $\$$ ) :: (a -> b) -> a -> b
```

The lazy infix application operator $\$$ takes a function and returns the same function. That is, $(\mathcal{S}) f ==$ or $f \mathcal{S} x == f$. The \mathcal{S} operator is right-associative, and it is primarily used in continuation-passing style. For example, the following two print expressions are the same:

```
main = do
  print (sum (map (* 2) [1, 2, 3])) ①
  print  $\$$  sum  $\$$  map (* 2) [1, 2, 3] ②
```

①

This will print

②

The same These two expressions are semantically equivalent.

17.6. The Eager Infix Application Operator

The eager infix application operator `$!` takes a function and returns a `seq` function with the same function as its second argument. That is, `($!) f == seq _ or f $! x == x `seq` f`. The `$!` operator is right-associative, like `seq`. Using the same example above,

```
main = do
  print $! sum $! map (* 2) [1, 2, 3] ①
```

①

This will print `10`. The only difference between `$` and `$!` is their strictness. That is, `$` preserves the default laziness whereas `$!` uses the `seq` function to force eager evaluation of arguments.

17.7. The until Function

until p f yields the result of applying f until p holds.

```
until :: (a -> Bool) -> (a -> a) -> a -> a
```

For example,

```
main = do
  print $ until (> 10) (* 2) 1
```

①

This will print

17.8. The asTypeOf Function

asTypeOf is a type-restricted version of Its typing forces its first argument to have the same type as the second.

```
asTypeOf :: a -> a -> a
```

For example,

```
main = do  
  print $ asTypeOf 3 (5 :: Int) ①
```

①

The type of the literal 3 is

18. List Functions

The Prelude defines the following list-related functions:

```
null, !!, length, ++, concat, reverse  
head, tail, last, init  
take, drop, splitAt, takeWhile, dropWhile, span, break  
map, concatMap, filter, any, all  
foldl, foldl1, scanl, scanl1, foldr, foldr1, scanr, scanr1  
iterate, repeat, replicate, cycle  
zip, zip3, zipWith, zipWith3, unzip, unzip3  
lines, words, unlines, unwords  
and, or, elem, notElem, lookup, maximum, minimum, sum, product
```


18.1. Basic List Functions

This section describes and

18.1.1. The null function

```
null :: [a] -> Bool
```

The list null function returns True if a given list is empty. Otherwise, it returns False. For example,

```
main = do
  print $ null ([] :: [Char])      ①
  print $ null ['a', 'b', 'c']    ②
```

①

It prints

②

It prints

18.1.2. The index !! operator

```
(!!) :: [a] -> Int -> a
```

The index operator !! takes a list and a non-negative index of type Int and it returns the value at the given index. When the index is outside the valid index range for the given list, it throws an error. For example,

```
main = do
  print $ ['a', 'b', 'c'] !! 1      ①
  -- print $ ['a', 'b', 'c'] !! (-1) ②
  -- print $ ['a', 'b', 'c'] !! 4   ③
```

①

This outputs List indexes are

②

It raises an error. Prelude.!!: negative

③

It raises an error. Prelude.!!: index too

18.1.3. The length function

```
length :: [a] -> Int
```

The list length function returns the length of a given list as an `Int`. This function does not terminate when the given list is not finite.

```
main = do
  print $ length []           ①
  print $ length ['a' .. 'z']
  -- print $ length [1 .. ]  ②
```

①

It prints

②

This function call does not return.

18.1.4. The append ++ operator

```
(++) :: [a] -> [a] -> [a]
```

The list append operator ++ concatenates two given lists.

```
main = do
  print $ ([] :: [Char]) ++ ['a', 'b'] ①
  print $ ['a', 'b'] ++ ['e', 'f', 'g'] ②
```

①

The resulting list is the same as ['a',

②

The resulting list is the same as ['a', 'b', 'e', 'f',

18.1.5. The concat function

```
concat :: [[a]] -> [a]
```

The list concat function takes a list of lists, and it returns the concatenation of all elements of the list.

```
main = do
  print (concat [[1],
                [5, 6, 7],
                [11]] :: [Int]) ①
  print $ concat ["Hello",
                 ", ", "Dr. Haskell",
                 " and ", "Mr. Highly Functional!"] ②
```

①

This prints out

②

Since String is this prints out "Hello, Dr. Haskell and Mr. Highly

18.1.6. The reverse function

```
reverse :: [a] -> [a]
```

The list reverse function returns the elements of a given list in reverse order. The argument list should be finite.

```
main = do
  print (reverse [1, 2, 3] :: [Int]) ①
  -- print $ reverse [1 ..]         ②
```

①

This prints out

②

This will not terminate.

18.2. Head and Tail Functions

This section describes the `head` and `init` functions.

18.2.1. The head function

```
head :: [a] -> a
```

The list head function takes a non-empty list and returns the first element of the list.

```
main = do
  print $ head ['a', 'b', 'c']      ①
  -- print $ head ([] :: [Char])  ②
```

①

It prints

②

It raises an error, Prelude.head: empty

18.2.2. The tail function

```
tail :: [a] -> [a]
```

The list tail function takes a non-empty list and returns a list of the remaining elements of the given list after the first element, which can be an empty list.

```
main = do
  print $ tail ([1, 2, 3] :: [Int]) ①
  -- print $ tail ([] :: [Int])    ②
```

①

It prints

②

It raises an error, Prelude.tail: empty

18.2.3. The last function

```
last :: [a] -> a
```

The list last function takes a non-empty and finite list and returns the last element of the list.

```
main = do
  print $ last ['a', 'b', 'c']           ①
  -- print $ last ([] :: [Char])       ②
```

①

It prints

②

It raises an error Prelude.last: empty

18.2.4. The init function

```
init :: [a] -> [a]
```

The list `init` function takes a non-empty and finite list and returns a list of the remaining elements of the given list before the last element.

```
main = do
  print $ init ([1, 2, 3] :: [Int])    ①
  -- print $ init ([] :: [Int])      ②
```

①

It prints

②

It raises an error, `Prelude.init: empty`

18.3. Take and Drop Functions

This section describes the and break functions.

18.3.1. The take function

```
take :: Int -> [a] -> [a]
```

The list take function takes an Int n and a list and it returns the prefix of xs of length n. It returns xs itself if n > length xs.

```
main = do
  print (take 2 [1, 2, 3, 4] :: [Int]) ①
  print (take 5 [1, 2, 3] :: [Int])   ②
```

①

It prints

②

It prints

18.3.2. The drop function

```
drop :: Int -> [a] -> [a]
```

The list drop function takes an int n and a list and it returns the suffix of xs after the first n elements. Or, it return an empty list [] if n >= length

```
main = do
  print (drop 2 [1, 2, 3, 4] :: [Int]) ①
  print (drop 5 [1, 2, 3] :: [Int])   ②
```

①

It prints

②

It prints

18.3.3. The splitAt function

```
splitAt :: Int -> [a] -> ([a],[a])
```

The splitAt n xs function is defined as (take n xs, drop n

```
main = do
  print $ splitAt 0 ([1, 2, 3] :: [Int]) ①
  print $ splitAt 2 ([1, 2, 3] :: [Int]) ②
  print $ splitAt 4 ([1, 2, 3] :: [Int]) ③
```

①

It prints

②

It prints

③

It prints

18.3.4. The takeWhile function

```
takeWhile :: (a -> Bool) -> [a] -> [a]
```

The takeWhile function, applied to a predicate p and a list returns the longest (possibly empty) prefix of xs of elements that satisfy

18.3.5. The dropWhile function

```
dropWhile :: (a -> Bool) -> [a] -> [a]
```

The list `dropWhile` function, applied to a predicate `p` and a list returns the remaining suffix after the longest (possibly empty) prefix of `xs` of elements that satisfy

18.3.6. The span function

```
span :: (a -> Bool) -> [a] -> ([a],[a])
```

The `span p xs` function is equivalent to `(takeWhile p xs, dropWhile p xs)`.
For example,

```
main = do
  print $ takeWhile (<= 2) [1, 2, 3, 1] ①
  print $ dropWhile (<= 2) [1, 2, 3, 1] ②
  print $ span (<= 2) [1, 2, 3, 1]      ③
```

①

It prints

②

It prints

③

It prints

18.3.7. The break function

```
break :: (a -> Bool) -> [a] -> ([a],[a])
```

The break p function is the same as span (not .

```
main = do
  print $ break (>= 2) [1, 2, 3, 1] ①
```

①

It prints

18.4. Map and Filter Functions

This section describes the `map` and `filter` functions.

18.4.1. The map function

```
map :: (a -> b) -> [a] -> [b]
```

The list map function takes a function f and a list and it returns a list obtained by applying f to each element of That is, $\text{map } f [x_1, x_2, \dots, x_n]$ evaluates to $[f x_1, f x_2, \dots, f$

For example,

```
mapDouble :: [Int] -> [Int]
mapDouble = map (* 2) ①
```

①

A [partial application](#) of map to The mapDouble function takes a list of Int and it returns another list by doubling all elements in the given list.

```
main = do
  print $ mapDouble [] ①
  print $ mapDouble [1, 2, 3] ②
```

①

It prints

②

It prints

18.4.2. The concatMap function

```
concatMap :: (a -> [b]) -> [a] -> [b]
```

The list `concatMap` function is defined to be a composition of `map` and `concat` functions, e.g., `concat`. That is, `concatMap` first applies `map` to a function of type `a -> [b]` and a list of type `[a]` and then it (or, flattens) the resulting list of type `[[b]]` to get the final list of type `[b]`. For example,

```
initial :: [String] -> [Char]
initial = concatMap (take 1) ①
```

①

The `initial` function takes an argument of a list of list of and it returns a list comprising the first `Char` of each element list.

```
main = do
  print $ initial ["John", "F", "Kennedy"] ①
  print $ initial ["Martin", "Luther", "King"] ②
```

①

It prints

②

It prints

18.4.3. The filter function

```
filter :: (a -> Bool) -> [a] -> [a]
```

The list filter function takes a predicate and a list, and it returns a list including only elements that satisfy the predicate. That is, `filter p xs` is the same as `[x | x <- xs, p x` using a [list](#). For example,

```
evenInts :: [Int] -> [Int]
evenInts = filter even

main = do
  print $ evenInts [1, 2, 12, 13, 14] ①
```

①

This prints

18.4.4. The any function

```
any :: (a -> Bool) -> [a] -> Bool
```

The list any function takes a predicate and a list, and it returns True if any element in the given list satisfies the predicate. It returns False otherwise. That is, any p is equivalent to or . map

For instance,

```
anyOdd :: [Int] -> Bool  
anyOdd = any odd ①
```

①

The anyOdd xs function is equivalent to or (map odd

```
main = do  
  print $ anyOdd [10, 11, 12] ①  
  print $ anyOdd [12, 14, 16] ②
```

①

It prints

②

It prints

18.4.5. The all function

```
all :: (a -> Bool) -> [a] -> Bool
```

The list all function takes a predicate and a list, similar to the any function, and it returns True if all elements in the given list satisfy the predicate. Otherwise, it returns False. That is, all p is equivalent to and . map Or, all p xs is equivalent to and (map p

For example,

```
allOdds :: [Int] -> Bool  
allOdds = all odd ①
```

①

The allOdds xs function is equivalent to and (map odd

```
main = do  
  print $ allOdds [10, 11, 12] ①  
  print $ allOdds [11, 13, 15] ②  
  print $ all (> 5) [6, 8, 10, 20] ③
```

①

It prints

②

It prints

③

It prints

18.5. Fold and Scan Functions

This section describes the `fold` and `scanr1` functions.

18.5.1. The foldl function

```
foldl :: (a -> b -> a) -> a -> [b] -> a
```

The list foldl function takes a binary operator, a starting value (typically, the left-identity of the operator), and a list, and it reduces the list using the binary operator, from left to right. That is, `foldl f z [x1, x2, ..., xn]` is equivalent to `(...(z `f` x1) `f` x2) ... `f`` For example,

```
main = do
  print $ foldl (++) ""
    ["To", "Be", "Or", "Not"] ①
  print $ foldl (+) 0
    ([1, 2, 3, 4, 5] :: [Int]) ②
```

①

The output: "ToBeOrNot"

②

The output: 15

18.5.2. The foldl1 function

```
foldl1 :: (a -> a -> a) -> [a] -> a
```

The list `foldl1` function is a variant of `fold1` that has no starting value argument. It throws an error when it is applied to an empty list. For example,

```
main = do
  print $ foldl1 (++)
    ["To", "Be", "Or", "Not"] ①
  print $ foldl1 (+)
    ([1, 2, 3, 4, 5] :: [Int]) ②
```

①

The output: "ToBeOrNot"

②

The output: 15

18.5.3. The scanl function

```
scanl :: (a -> b -> a) -> a -> [b] -> [a]
```

The list scanl function is similar to but returns a list of successive reduced values from the left. That is, `scanl f z [x1, x2, ...]` is equivalent to `[z, z `f` x1, (z `f` x1) `f` x2, ...]`. Note that `foldl f z xs` is the same as `last (scanl f z xs)`.

```
main = do
  print $ scanl (++) ""
    ["To", "Be", "Or", "Not"] ①
  print $ scanl (+) 0
    ([1, 2, 3, 4, 5] :: [Int]) ②
```

①

The output: `["", "To", "ToBe", "ToBeOr", "ToBeOrNot"]`

②

The output: `[0,1,3,6,10,15]`

18.5.4. The scanl1 function

```
scanl1 :: (a -> a -> a) -> [a] -> [a]
```

The list scanl1 function is similar to but again without the starting element. scanl1 f [x1, x2, ...] is equivalent to [x1, x1 `f` x2,

```
main = do
  print $ scanl1 (++)
    ["To", "Be", "Or", "Not"]      ①
  print $ scanl1 (+)
    ([1, 2, 3, 4, 5] :: [Int])    ②
```

①

The output: ["To","ToBe","ToBeOr","ToBeOrNot"]

②

The output: [1,3,6,10,15]

18.5.5. The foldr function

```
foldr :: (a -> b -> b) -> b -> [a] -> b
```

The foldr function takes a binary operator, a starting value (typically the right-identity of the operator), and a list, and it reduces the list using the binary operator, from right to left. `foldr f z [..., xn1, xn]` is equivalent to `(... `f` (xn1 `f` (xn `f``

For example,

```
main = do
  print $ foldr (++) ""
    ["To", "Be", "Or", "Not"]      ①
  print $ foldr (+) 0
    ([1, 2, 3, 4, 5] :: [Int])    ②
```

①

The output: "ToBeOrNot"

②

The output: 15

18.5.6. The foldr1 function

```
foldr1 :: (a -> a -> a) -> [a] -> a
```

The list `foldr1` function is a variant of `foldr` that has no starting value argument. It raises an error when it is applied to an empty list.

```
main = do
  print $ foldr1 (++)
    ["To", "Be", "Or", "Not"] ①
  print $ foldr1 (+)
    ([1, 2, 3, 4, 5] :: [Int]) ②
```

①

The output: "ToBeOrNot"

②

The output: 15

18.5.7. The scanr function

```
scanr :: (a -> b -> b) -> b -> [a] -> [b]
```

The list scanr function is similar to but it returns a list of successive reduced values from the right. That is, `scanr f z [..., xn1, xn]` is equivalent to `[..., xn1 `f` (z `f` xn), z `f` xn]`. Note that `foldr f z xs` is the same as `head (scanr f z For example,`

```
main = do
  print $ scanr (++) ""
    ["To", "Be", "Or", "Not"]      ①
  print $ scanr (+) 0
    ([1, 2, 3, 4, 5] :: [Int])    ②
```

①

The output: ["ToBeOrNot","BeOrNot","OrNot","Not",""]

②

The output: [15,14,12,9,5,0]

18.5.8. The scanr1 function

```
scanr1 :: (a -> a -> a) -> [a] -> [a]
```

The list `scanr1` function is similar to `scanr` but again without the starting element. `scanr1 f [..., xn2, xn1, xn]` is equivalent to `[..., xn2 `f` (xn1 `f` xn), xn1 `f` xn,`

```
main = do
  print $ scanr1 (++)
    ["To", "Be", "Or", "Not"] ①
  print $ scanr1 (+)
    ([1, 2, 3, 4, 5] :: [Int]) ②
```

①

The output: ["ToBeOrNot","BeOrNot","OrNot","Not"]

②

The output: [15,14,12,9,5]

This book can be rather "dense", depending on your background. It covers a lot of topics, but possibly not with enough depth. For example, the folding functions discussed in this section are very important tools in

Haskell, and it will require some deliberate studies if you haven't used this kind of functional programming style before. Although we claim that Haskell is a much simpler language, syntactically, than other widely-used programming languages, learning still takes time. The readers are encouraged to go through each of the above examples, step by step, so that you understand how "left folding" vs "right folding" work, etc.

18.6. Iterate and Repeat Functions

This section describes the `iterate` and `repeat` functions.

18.6.1. The iterate function

```
iterate :: (a -> a) -> a -> [a]
```

The list iterate function is recursively defined as $\text{iterate } f \ x = x : \text{iterate } f \ (f \ x)$ (f which is an infinite list of repeated applications of f to e.g., $[x, f \ x, f \ (f \ x)]$). For example,

```
main = do
  print $ take 5 $ iterate (* 2) 2
```

①

The output: [2,4,8,16,32]

18.6.2. The repeat function

```
repeat :: a -> [a]
```

The list repeat function returns an infinite list by indefinitely repeating a given argument. That is, $\text{repeat } x = \text{xs}$ where $\text{xs} =$ For example,

```
main = do  
  print $ take 5 $ repeat 21
```

①

The output: [21,21,21,21,21]

18.6.3. The replicate function

```
replicate :: Int -> a -> [a]
```

The list replicate function is defined to be replicate n x = take n (repeat x)

For example,

```
main = do  
  print $ replicate 5 42
```

①

The output: [42,42,42,42,42]

18.6.4. The cycle function

```
cycle :: [a] -> [a]
```

The list cycle function takes a list and returns the infinite repetition of the given list. It returns an error when the list is empty. It returns the same list when the list is an infinite list. For example,

```
main = do  
  print $ take 10 $ cycle [1, 2, 3] ①
```

①

The output: [1,2,3,1,2,3,1,2,3,1]

18.7. Zip and Unzip Functions

This section describes the `zip` and `unzip3` functions from the Prelude, which deal with lists of pairs (2-tuples) and triplets (3-tuples).

18.7.1. The zip function

```
zip :: [a] -> [b] -> [(a,b)]
```

The list zip function takes two lists and returns a list of pairs, each pair comprising the corresponding elements from two lists. If one input list is shorter than the other, then excess elements of the longer list are discarded.

```
main = do
  print $ zip [1, 2, 3] ['a', 'b']
```

①

The output: [(1,'a'),(2,'b')]

18.7.2. The zip3 function

```
zip3 :: [a] -> [b] -> [c] -> [(a,b,c)]
```

The list `zip3` function takes three lists and returns a list of triplets, by taking one element from each list. The length of the resulting list is the same as that of the shortest input list.

```
main = do
  print $ zip3 [1, 2] ['a', 'b'] ["hi"] ①
```

①

The output: [(1,'a',"hi")]

18.7.3. The zipWith function

```
zipWith :: (a->b->c) -> [a]->[b]->[c]
```

The list `zipWith` function takes a binary function and two lists, and it returns a new list by applying the given function to the corresponding elements in the two input lists.

```
main = do  
  print $ zipWith (+) [1, 2, 3] [3, 6] ①
```

①

The output: [4,8]

18.7.4. The zipWith3 function

```
zipWith3 :: (a->b->c->d) -> [a]->[b]->[c]->[d]
```

The list `zipWith3` function takes a ternary function and three lists, and it returns a new list by combining the corresponding elements in the three input lists with the given function.

```
sum3 :: Int -> Int -> Int -> Int
sum3 x y z = x + y + z ①

main = do
  print $ zipWith3 sum3 [1, 2] [2] [3] ②
```

①

We define a simple ternary function for illustration. The most general type for this kind of function would be `sum3 :: Num a => a -> a -> a ->`

②

The output: `[6]`

18.7.5. The unzip function

```
unzip :: [(a,b)] -> ([a],[b])
```

The list unzip function takes a list of pairs and returns a pair of lists.

```
main = do  
  print $ unzip [(1, 2), (3, 4), (5, 6)] ①
```

①

The output: ([1,3,5],[2,4,6])

18.7.6. The unzip3 function

```
unzip3 :: [(a,b,c)] -> ([a],[b],[c])
```

The list unzip3 function takes a list of triplets and returns a triplet of three lists.

```
main = do  
  print $ unzip3 [(1, 2, 3), (4, 5, 6)] ①
```

①

The output: ([1,4],[2,5],[3,6])

18.8. Special Class Functions

Some list functions are defined over particular types or classes.

18.8.1. The Bool list functions

The `and` and `or` functions deal with Bool lists.

```
and, or :: [Bool] -> Bool
```

The `and` function returns the conjunction of all elements in a given Boolean list. Likewise, the `or` function returns the disjunction of all elements in a Boolean list. For example,

```
main = do
  print $ and []                ①
  print $ and [True, False, False]
  print $ and $ replicate 10 True
  print $ and (False : repeat True)
  print $ and (False : repeat False)
  print $ and (True : repeat False)
  -- print $ and (True : repeat True)  ②
```

①

The outputs are, from the top, and Note that `and []` returns

②

This will hang.

```
main = do
  print $ or [] ①
  print $ or [True, True, False]
  print $ or $ replicate 10 False
  print $ or (True : repeat False)
  print $ or (True : repeat True)
  print $ or (False : repeat True)
  -- print $ or (False : repeat False) ②
```

①

The outputs are, from the top, and Note that or [] returns

②

This will hang.

18.8.2. The Eq list functions

The `elem` and `lookup` functions deal with lists whose elements belong to the [Eq](#)

```
elem, notElem :: (Eq a) => a -> [a] -> Bool
```

The `elem` function takes a value and a list and it returns `True` if the value is an element of the given list. Otherwise, it returns `False`. The `notElem` function is a negation of `elem`. For example,

```
main = do
  print $ elem 3 [1, 2, 3, 4]      ①
  print $ elem 6 [1, 2, 3, 4]      ②
  print $ notElem 3 [1, 2, 3, 4]  ③
  print $ notElem 6 [1, 2, 3, 4]  ④
```

①

The output: `True`

②

The output: `False`

③

The output: False

④

The output: True

The lookup function

```
lookup :: (Eq a) => a -> [(a,b)] -> Maybe b
```

The lookup function takes a value and an association list (e.g., a list of pairs), and if there exists a pair in the list whose first element is the same as the given value, then it returns the second element v of the found pair, as Just. If there are found multiple pairs with the same given value in the list, the first pair is used. If no such pair is found, then it returns For example,

```
main = do
  let dict = [(1, 'a'), (2, 'b'), (5, 'e'), (2, 'v')]
  print $ lookup 1 dict           ①
  print $ lookup 4 dict           ②
  print $ lookup 2 dict           ③
```

①

The output: Just 'a'

②

The output: Nothing

③

The output: Just Note that there are two pairs with its first element equal to

18.8.3. The Ord list functions

The maximum and minimum functions operate on non-empty and finite lists whose element types belong to the [Ord](#)

```
maximum, minimum :: (Ord a) => [a] -> a
```

The maximum and minimum functions return the maximum value or minimum value from a given list, respectively. For example,

```
main = do
  print $ maximum [10, -5, 40, 20] ①
  print $ minimum [10, -5, 40, 20] ②
```

①

The output: 40

②

The output: -5

18.8.4. The Num list functions

The sum and product functions operate on lists whose element types belong to the [Num](#)

```
sum, product :: (Num a) => [a] -> a
```

The sum function computes the sum of a finite list of numbers. The product function computes the product of a finite list of numbers. For example,

```
main = do
  print $ sum [1, 2, 3, 4, 5]      ①
  print $ product [1, 2, 3, 4, 5] ②
```

①

The output: 15

②

The output: 120

18.8.5. The string lines and words functions

The `lines` and `unlines` functions deal with `String` and

```
lines  :: String -> [String]
unlines :: [String] -> String
```

The `lines` function splits a given string into a list of strings using newline characters as separators. The `unlines` function does the reverse. It joins a given list of strings into one string, which comprises multiple lines with terminating newlines. For example,

```
main = do
  let verse =
      "April is the cruellest month, breedingn
      Lilacs out of the dead land, mixingn
      Memory and desire, stirringn
      Dull roots with spring rain." ①
  print $ lines verse ②
```

①

Note the "multiline string" literal syntax.

②

The output: ["April is the cruellest month, breeding", "Lilacs out of the

dead land, mixing", "Memory and desire, stirring", "Dull roots with spring rain."]

```
main = do
  let stanzas =
      [ "Frisch weht der Wind"
      , "Der Heimat zu"
      , "Mein Irisch Kind,"
      , "Wo weilest du?"
      ]
  print $ unlines stanzas ①
```

①

The output: "Frisch weht der Wind\nDer Heimat zu\nMein Irisch Kind,\nWo weilest du?\n"

The words and unwords functions

```
words  :: String -> [String]
unwords :: [String] -> String
```

The words function splits a given string into a list of strings, similar to but it uses white spaces as separators. The unwords function joins a given list of strings into one string with separating spaces. For example,

```
main = do
  let toBe = "To be or not to be."
  print $ words toBe ①
  let question = ["That", "is", "the", "question"]
  print $ unwords question ②
```

①

The output: ["To", "be", "or", "not", "to", "be."]

②

The output: "That is the question"

19. Data Types

19.1. Datatypes

We discuss a few different ways to [declare new types or type synonyms](#) in Haskell in an earlier part of the book. We describe the top-level data declaration syntax in some more detail in this chapter.

An algebraic datatype can be declared with the `data` keyword. It has the following general syntax:

```
data cx => T u1 ... uk =  
  K1 t11 ... t1k1  
  | ...  
  | Kn tn1 ... tnkn
```

This declaration introduces a new data type `T` with one or more data constructors `...`, `Kn` (or, just "constructors"). In this notation, `cx` denotes `a` and `u1 ... uk` represent type parameters. The type of each constructor `Ki` is (roughly) `ti1 -> ... -> tiki -> (T u1 ... uk)` within a proper context. For example,

```
data Num a => Result a  
  = Tie  
  | Win a  
  | Loss a a
```

This declaration introduces a new data type `Result` with three constructors, and The type of `Tie` is `Result a` for an implicit type variable whereas the types of `Win` and `Loss` are `(Num a) => a -> Result a` and `(Num a) => a -> a -> Result` respectively, for any type `a` that is an instance of the [Num](#)

The data declaration can optionally include a deriving clause, which is discussed in the next chapter, in the context of [derived](#)

19.1.1. Field access

A data constructor of arity k creates an object with k components, in the specified order. These components are normally accessed positionally, e.g, using [pattern](#)

For instance, using the above Result datatype,

```
scored :: Result Int -> Int
scored (Loss s _) = s
scored _ = error "Not a loss"
```

This scored function returns the first field of the Loss data constructor. For example,

```
main = do
  let result = Loss (2 :: Int) (1 :: Int)
  print $ scored result
```

Alternative to this positional access method, one can assign field labels to the components of a data object. This is called a "record". A labeled field of a record can be referenced by its label, independently of its position within the constructor. The [record syntax](#) is described next.

19.2. Record Syntax

A datatype declaration may optionally assign labels to the fields of a constructor, using the record syntax, `C { ...`. These field labels can be used to construct, select, and update fields. For example,

```
data Contact = Contact { name, phone :: String, address :: Int, zipCode :: String }
```

These labels are referred to as selector or accessor functions because they are used to access the named fields. They must start with a lowercase letter or underscore (because they are functions), and they cannot have the same name as another function in scope.

This particular data declaration is more or less equivalent to the following without using field labels.

```
data Contact = Contact String String Int String
```

19.2.1. Field selection

Field labels create selector functions, which are top level bindings in a module.

A selector can extract the corresponding field from an object. More specifically, a field label f introduces a selector function defined as:

```
f x = case x of
  C1 p11 ... p1k -> e1
  ...
  Cn pn1 ... pnk -> en
```

where

$C_1 \dots C_n$ are the constructors of the given datatype that contains a field labeled with

p_{ij} is y or $_$ depending on whether f labels the component of and

e_i is y or undefined depending on whether some field in C_i has a label of f or not, respectively.

For example, in the following datatype declaration,

```
data Data
  = Cons1 { f1 :: String, f2 :: Int }
  | Cons2 { f2 :: Int, f3 :: Bool }
  | Cons3 Int Int
```

The `f1` and `f3` labels are field selectors, (implicitly) defined as follows:

```
f1 :: Data -> String
f1 x = case x of
  Cons1 y _ -> y
```

```
f2 :: Data -> Int
f2 x = case x of
  Cons1 _ y -> y
  Cons2 y _ -> y
```

```
f3 :: Data -> Bool
f3 x = case x of
  Cons2 _ y -> y
```

Note that, as shown in this example,

Record and non-record syntax constructors can be mixed in a single data declaration, and

The same field labels can be used across multiple data constructors as long as they have the same types.

19.2.2. Record construction

A record constructor may be used to construct a value by specifying their components by name rather than by position, using the curly braces syntax. Unlike the braces used in declaration lists, however, the { and } characters must be explicitly included, and they cannot be omitted using the [layout](#)

For instance, using the same Data type,

```
main = do
  let d1 = Cons1 {f1 = "Hell", f2 = 333} ①
      d2 = Cons2 {f2 = 666, f3 = False}
      d3 = Cons3 333 666
  print (d1, d2, d3) ②
```

①

Note that the field order is not significant in the record syntax. That is, `Cons1 {f1 = "Hell", f2 = 333}` is equivalent to `Cons1 {f2 = 333, f1 =`

②

The Data type needs to be an instance of Show in order to be able to call `print`. See the section on

Note that the field selectors can be used just like any other top-level functions, as described above. Using the same example,

```
main = do
  let d1 = Cons1 {f1 = "Hello", f2 = 333}
  print $ f1 d1
  print $ f2 d1
```

①

This will print

②

This will print

19.2.3. Updating records

Values of a record syntax constructor of a datatype can be "non-destructively updated". That is, one can create a new value based on the field values of an existing value belonging to the same record syntax constructor, by selectively updating only some (or, all) of the fields. For example,

```
main = do
  let d2 = Cons2 {f2 = 666, f3 = False}
      d2' = d2 {f2 = 999}
  print d2'
```

①

①

d2' has a value {f2 = 999, f3 =

19.3. Abstract Datatypes

The visibility of a datatype's constructors (outside of the module in which the datatype is defined) is controlled by the form of the datatype's name in the [export](#) as we explain in the [Modules](#) chapter. This effectively allows creating abstract datatypes (ADTs) that cannot be directly constructed (outside the given module). For example, here's a simple queue data type, defined in a module named

Listing 3. Queue.hs

```
module Queue
  ( add
  , remove
  , empty
  ) where ①

data QueueType a
  = NullQueue
  | Queue a (QueueType a)
  deriving (Show)

add :: a -> QueueType a -> QueueType a
add = Queue

remove :: QueueType a -> (Maybe a, QueueType a)
remove NullQueue = (Nothing, NullQueue)
remove (Queue v NullQueue) = (Just v, NullQueue)
remove (Queue v q) = (fst qq, Queue v (snd qq))
  where
    qq = remove q

empty :: QueueType a
empty = NullQueue
```

①

Notice the conventional formatting. There is no difference between this and the module declaration written in one line.

In this example, we declare a datatype `QueueType` with two constructors, and define three functions, and Note that we export neither the type `QueueType` nor its constructors, `NullQueue` and Hence, a value of `QueueType` cannot be directly constructed outside this module. But, values of `QueueType` can still be used using the exported functions. For instance,

Listing 4. Main.hs

```
main = do
  let q1 = Queue.add (5 :: Int) $ Queue.add (3 :: Int) Queue.empty
      print q1
      let (v, _) = Queue.remove q1
          print v
```

①

This will print Queue 5 (Queue 3

②

This will print Just

20. Classes

The or typeclass, in Haskell is comparable to constructs like interfaces, traits, or protocols in other programming languages.

A class in Haskell is essentially a collection of types, just like a type is a collection of values. A class specifies a set of functions, or "behaviors". A type that belongs to a certain class needs to implement (either explicitly or implicitly) all functions of the

Alternatively, another way to look at the class in Haskell is from the viewpoint of "function overloading". A function can be defined with parameters from certain collection of types, and not just specific types. As long as the parameter set belongs to this "collection", they may be valid types for the given function.

Haskell accomplishes overloading through [class](#) and [instance](#) declarations.

20.1. Class Declarations

A class declaration introduces a new class and the operations on it, called the class Here's a general syntax:

```
class cx => C u where cdecls
```

This declaration introduces a new class with name C and a single type variable The context cx specifies the superclasses of if any.

The where clause (e.g., the where cdecls part above), different from the [where](#) is optional, but if provided, it can contain any of the following three declarations.

20.1.1. New class methods

The class declaration introduces new class methods, in the top-level namespace. The class methods of a class declaration are those with an explicit type signature $v_i :: c_{xi} \Rightarrow t_i$ in `cdecls`. E.g.,

```
class cx => C u where
  v1 :: cx1 => t1
  ...
  vn :: cxn => tn
```

For instance, we can define a class that provides "literate values" for numeric types as follows:

```
class Num a => Value a where
  value :: a -> String
```

①

A class method for the example class `Note` that this is syntactically more or less the same as the type signature declaration for a function binding. In fact, this introduces a function name, at the top-level scope.

20.1.2. Default class methods

The where clause may contain a default class method implementation for any of the class methods. The default class method for `vi` is used if no binding is given in a particular [instance](#). For example,

```
class Num a => Value a where
  value :: a -> String      ①
  value x = "High"         ②
```

①

An example class method, as above.

②

A default class method for the class method. Syntactically, orders are significant, but it is typical to put a default class method immediately below the corresponding class method, just like we (always) put the function binding below its type signature declaration.

20.1.3. Fixity declaration

The class declaration where clause may also contain a [fixity declaration](#) for any of the class methods. Since class methods declare top-level values, the fixity declaration for a class method may alternatively appear at top level, outside the class declaration.

20.2. Instance Declarations

An instance declaration which makes the type T to be an instance of class C is called a C - T instance. For example, for a class C declared as `class cx => C u where { cbody }` the general form of the corresponding instance declaration for type T is,

```
instance cx' => C (T u1 ... uk) where { d }
```

The type $(T u1 \dots uk)$ must take the form of a type constructor T applied to simple type variables \dots . When the type constructor is nullary, the parentheses may be omitted. The declarations d may contain bindings only for the class methods of

For instance, using the `Value` class example from the previous section,

```
instance Num => Value Int where  
  -- value :: a -> String           ①  
  value x = "High"                 ②
```

①

The class method `value` for the `Value` class. You cannot redeclare it in

an instance declaration, but sometimes it is useful to see its signature while implementing it in a particular instance. You can put it in a comment, as in this example, or you can use a GHC language extension.

②

An example function binding for the class method,

The instance body declarations may not contain any type signatures or fixity declarations, since these have already been given in the class declaration. The GHC language extension `InstanceSigs` may be used if you want to explicitly include the method's type signature (the class method) in an instance declaration.

If no binding is given for a class method, then the class method of this instance is bound to `undefined` unless the corresponding default class method exists in the class declaration.

20.3. Deriving

As indicated earlier, data and newtype declarations can include an optional deriving clause. If it is included with one or more classes, then derived instance declarations are automatically generated for the datatype for each of the specified classes.

Derived instances can be declared for the `Eq` and `Read` classes in the `Prelude`, and possibly for other classes in the standard library.

21. Standard Classes

The following type classes are defined by the Haskell Prelude:

and

Other numeric classes such as etc.

The [Functor](#) and [Monad](#) classes are explained later in the book, in separate chapters. The `Applicative` for `Applicative` for short, from the GHC language extension, is also widely used, but we do not include it in this book.

21.1. The Eq Class

The Eq class defines equality and inequality methods:

```
class Eq a where
  (==), (/=) :: a -> a -> Bool
```

All basic datatypes except for functions and IO are instances of this class.

Instances of Eq can be [derived](#) for any user-defined datatype whose constituents are also instances of

For example,

```
data Fruit = Apple | Orange
instance Eq Fruit where
  -- (==) :: Fruit -> Fruit -> Bool
  Apple == Apple = True           ①
  Orange == Orange = True
  _ == _ = False
```

①

Note that we provide a binding for but not for in this example. The class

Eq includes default class methods for both (==) and using the negation of each other. That is, if a binding is provided for one in an instance, then we can rely on the default class method for the other.

Or, using

```
data Fruit = Apple | Orange
  deriving(Eq)
```

21.2. The Ord Class

The Ord class is used for totally ordered datatypes:

```
class (Eq a) => Ord a where
  compare      :: a -> a -> Ordering
  (<), (<=), (>=), (>) :: a -> a -> Bool
  max, min     :: a -> a -> a
```

All basic datatypes except for functions, and are instances of this class.

Instances of Ord can be derived for any user-defined datatype whose constituent types are in

For example,

```
data Sound = Do | Re

instance Eq Sound where ①
  -- (==) :: Sound -> Sound -> Bool
  Do == Do = True
  Re == Re = True
  _ == _ = False

instance Ord Sound where ②
  -- compare :: Sound -> Sound -> Ordering
  compare Do Do = EQ
  compare Re Re = EQ
  compare Do _ = LT
```



```
compare _ Re = LT  
compare Re _ = GT  
compare _ Do = GT
```

①

Note that, since Eq is a superclass of Sound needs to be an instance of Eq before it can be an instance of

②

We rely on the default class methods for other methods of

21.3. The Enum Class

Class Enum defines operations on sequentially ordered types:

```
class Enum a where
  succ, pred    :: a -> a
  toEnum       :: Int -> a
  fromEnum     :: a -> Int
  enumFrom     :: a -> [a]
  enumFromThen :: a -> a -> [a]
  enumFromTo   :: a -> a -> [a]
  enumFromThenTo :: a -> a -> a -> [a]
```

For example,

```
data Ternary = T0 | T1 | T2
  deriving (Show)
```

```
instance Enum Ternary where
  -- toEnum :: Int -> Ternary
  toEnum x = case x of
    0 -> T0
    1 -> T1
    _ -> T2

  -- fromEnum :: Ternary -> Int
  fromEnum t = case t of
    T0 -> 0
    T1 -> 1
    T2 -> 2
```

21.4. The Bounded Class

The Bounded class is used to name the upper limit and lower limit of the values of a type:

```
class Bounded a where  
  minBound, maxBound :: a
```

The types and all tuples are instances of

The Bounded class may be derived for any enumeration type.

Bounded may also be derived for single-constructor datatypes whose constituent types are in

For example,

```
data Drink = Tall | Grande | Venti  
  
instance Bounded Drink where  
  -- minBound :: Drink  
  minBound = Tall  
  
  -- maxBound :: Drink  
  maxBound = Venti
```

21.5. The Show Class

The Show class is used to convert values to strings:

```
type ShowS = String -> String ①

class Show a where
  showsPrec :: Int -> a -> ShowS
  show      :: a -> String
  showList :: [a] -> ShowS
```

①

Declared in the Prelude. Note that ShowS is a function type, which takes a string and returns a string.

All Prelude types, except the function types and the IO type, are instances of Show. For example,

```
data Weather = Sunny | Rainy

instance Show Weather where
  -- show :: Weather -> String
  show Sunny = "Sunny"
  show Rainy = "Rainy"
```

Or, by

```
data Weather = Sunny | Rainy
  deriving(Show)
```

21.6. The Read Class

The Read class is used to convert values from strings:

```
type ReadS a = String -> [(a, String)] ①

class Read a where
  readsPrec :: Int -> ReadS a
  readList  :: ReadS [a]
```

①

A convenience type, defined in the Prelude.

All Prelude types, except function types and are instances of For example,

```
instance Read Weather where
  -- readsPrec :: Int -> ReadS Weather

  readsPrec _ r =
    if r == "Sunny"
    then [(Sunny, "")]
    else [(Rainy, "")]
```

Or, using

```
data weather = Sunny | Rainy
  deriving(Read)
```

21.7. The Num Class

The Num class is defined as follows:

```
class (Eq a, Show a) => Num a where
  (+), (-), (*)    :: a -> a -> a
  negate          :: a -> a
  abs, signum     :: a -> a
  fromInteger     :: Integer -> a
```

For example, using the following simple datatype,

```
data Binary = Zero | One
  deriving (Show, Eq)
```

We can make Binary an instance of

```
instance Num Binary where
  -- abs :: Binary -> Binary
  abs a = a
  -- signum :: Binary -> Binary
  signum a = a
  -- fromInteger :: Integer -> Binary
  fromInteger n = if n <= 0 then Zero else One
  -- negate :: Binary -> Binary
  negate a = a
  -- (+) :: Binary -> Binary -> Binary
  Zero + Zero = Zero
  _ + _ = One
```



```
-- (*) :: Binary -> Binary -> Binary
One * One = One
_ * _ = Zero
```

22. Functors

A Functor represents a parametric type that can be mapped over. In fact, the list is an archetypical example of parametric types that support mapping. For example,

```
main = do
  let x = [1, 2, 3] :: [Int]
      y = map (* 3) x
      print y
```

Note that, in this example, a value `[1, 2, 3]` of `[Int]` (a list of has been mapped to another value `[3, 6, 9]` of the same type, using the [map function](#) :: `(a -> b) -> [a] ->` The Functor class is essentially a generalization of the types like lists. In addition to lists, IO and Maybe in the Prelude are in this class.

22.1. The Functor Class

The types belonging to the Functor typeclass need to support a mapping function, defined as follows:

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

①

If this notation is not very clear to you, $f\ a$ represents a parametrized type f with a type variable e.g., similar to `Maybe` etc. The most commonly used parametrized type in Haskell, namely, the list, has a special syntax, This is merely a syntactic sugar for `[]` which has the form f Note the similarity between the list's `map` function and `fmap` function. In fact, as indicated, a list is an instance of `Functor` with `fmap` defined to be the good ol' `map` function.

In addition, instances of `Functor` should satisfy the following laws:

```
fmap id = id
fmap (f . g) = fmap f . fmap g
```

22.2. Functor Instances

22.2.1. The Maybe functor

Here's the standard implementation of fmap for

```
instance Functor Maybe where
  -- fmap :: (a -> b) -> Maybe a -> Maybe b
  fmap f Nothing = Nothing
  fmap f (Just x) = Just (f x)
```

One can easily verify that this implementation satisfies the Functor laws. For instance, both `fmap $ id Nothing` and `id Nothing` yield `Nothing` and `fmap $ id $ Just x` and `id $ Just x` yield `Just x`. Hence `fmap id = id` for this fmap function. The second law `fmap (f . g) = fmap f . fmap g` can be likewise easily verified.

Some more examples:

```
main = do
  let m1 = Nothing :: Maybe Int
      print $ fmap (+ 42) m1           ①
      m2 = Just 624 :: Maybe Int
      print $ fmap (+ 42) m2         ②
```

①

This will print

②

This will print Just

23. Monads

The Monad class represents parametric types that support certain operations, in particular, binding and return operations,

```
class Monad m where
  (>>=) :: m a -> (a -> m b) -> m b ①
  return :: a -> m a ②
```

①

Again, `m a` refers to a parameterized type `m` with a type parameter `A` type which is an instance of needs to implement these methods for an arbitrary type variable

②

Notice the `return` function. Haskell does not have the `return` statement which is found in virtually all imperative programming languages. The `return` class method of a `Monad` type `m` takes a value of type `a` and returns a value of type `m`

The binding operation `>>=` is a generalization of [concatMap](#) (or, "flat map") defined over a list parametric type,

```
concatMap :: (a -> [b]) -> [a] -> [b] ①
```

①

Again notice the similarity between `>>=` and the list's `concatMap` function (despite the flip of the two arguments).

For instance,

```
main = do
  let x = [1, 2, 3] :: [Int]
      y = concatMap (e -> [e, 2 * e]) x
  print y ①
```

①

This will output

Informally speaking, the `Monad` class is a generalization of parametric types like lists which support the "mapping and then flattening" operation. In the Prelude, in addition to lists, `Maybe` and `IO` are instances of

23.1. The Monad Class

The Monad typeclass defines the basic operations over a monad:

```
class Monad m where
  (>>=) :: m a -> (a -> m b) -> m b ①
  (>>)  :: m a -> m b -> m b
  return :: a -> m a
  fail   :: String -> m a
  m >> k = m >>= _ -> k ②
  fail s = error s
```

①

These top four lines are [class](#)

②

The bottom two lines are [default class](#). Hence, (>>) and fail need not be implemented in instance declarations.

Furthermore, instances of Monad should satisfy the following laws:

```
return a >>= k = k a
m >>= return = m
m >>= (x -> k x >>= h) = (m >>= k) >>= h
```

Instances of both Monad and Functor should additionally satisfy the following law (in addition to the Functor laws):

```
fmap f xs = xs >>= return . f
```

23.2. Monad Instances

23.2.1. The Maybe monad

Here's the standard implementations of the and fail functions for

```
instance Monad Maybe where
  (Just x) >>= k = k x
  Nothing  >>= k = Nothing
  return   = Just
  fail s   = Nothing
```

One can easily verify that these implementations satisfy the Monads laws. We will leave it as an exercise to the readers.

Here's an example use of the bind `>>=` operator with the Maybe monad:

```
main = do
  let m1 = Nothing :: Maybe Int
      print $ m1 >>= Just           ①
      m2 = Just 666 :: Maybe Int
      print $ m2 >>= Just           ②
```

①

This will print Note that although `m1` is `Nothing`, `m1 >>= Just` does not fail. It merely returns

②

This will print Just

24. Do Expressions

A do expression provides a more conventional, more imperative programming-style, syntax in a monadic context. Syntactically, a do expression has the following general form:

```
do { STATEMENTS }
```

where STATEMENTS can be one or more of any of the following:

An expression,

A monadic assignment of the form, pattern <-

A let declaration (without and

An empty statement

The last statement in STATEMENTS must be an expression, which becomes the value of the overall do expression. Variables bound by let

have fully polymorphic types while those defined by `<-` are lambda bound and thus they are monomorphic.

Empty statements are ignored. Otherwise, the do expressions are evaluated as follows:

`do { exp }` is the same as

`do { exp; stmts }` is evaluated to `exp >> do { stmts }`

`do { pat <- exp; stmts }` is evaluated to `let ok pat = do { stmts }; ok _ = fail ... in exp >>=`

`do { let decls; stmts }` is equivalent to `let decls in do { stmts }`

We have been using do expressions throughout this book. We will see some more examples in the [last chapter on](#)

25. Basic Input/Output

The I/O system in Haskell is purely and yet it has all of the expressive power found in imperative programming languages. Haskell uses a Monad to integrate I/O operations, or actions, into a purely functional context.

25.1. I/O Operations

The IO type is an instance of the [Monad](#). The two monadic binding functions are used to compose a series of I/O operations:

```
(>>)  :: IO a -> IO b -> IO b
(>>=) :: IO a -> (a -> IO b) -> IO b
```

The `>>` operator is used when the result of the first operation is uninteresting, for example when it is

The `>>=` operation passes the result of the first operation as an argument to the second operation.

Furthermore, the `return` function is used to define the result of an I/O operation.

25.2. Exceptions

An I/O operation may raise an exception, a value of type `IOError` instead of returning a result. One can use the Prelude `userError` function to create an `IOError` which is discussed next.

The readers are encouraged to consult the official Report or other references if you would like to learn more on the IO Monad and exception handling. In the next and final chapter, we discuss some of the I/O functions in the Standard Prelude and how to use them.

26. I/O Functions

The Prelude includes the following IO-related functions:

```
ioError, userError, catch  
putChar, putStr, putStrLn, print  
getChar, getLine, getContents, interact, readIO, readLn  
readFile, writeFile, appendFile
```

26.1. Error Functions

26.1.1. The userError function

```
userError :: String -> IOError
```

The IO userError function returns an IOError value with a given string as an error message. For instance

```
demoError :: String -> IOError
demoError msg =
  userError $ "User Error: " ++ msg
```

26.1.2. The `ioError` function

```
ioError :: IOError -> IO a
```

The IO `ioError` function is used to raise an `IOError` in the IO monad. For example,

```
main = do  
  ioError $ demoError "Urghh"
```

26.1.3. The catch function

```
catch :: IO a -> (IOError -> IO a) -> IO a
```

The IO catch function takes an IO action and a handler function, and if the IO action returns an IOError it raises the error in the IO monad.

26.2. Output Functions

26.2.1. The putChar function

```
putChar :: Char -> IO ()
```

The IO putChar function writes a given Char to the standard output device.

```
main = do  
  putChar 'H'; putChar 'e'; putChar 'l'  
  putChar 'l'; putChar 'o'; putChar 'n'
```

26.2.2. The putStr function

```
putStr :: String -> IO ()
```

The IO putStr function takes a string argument and it writes it to the standard output device.

26.2.3. The putStrLn function

```
putStrLn :: String -> IO ()
```

The IO putStrLn function works the same way as but it appends a newline character.

```
main = do
  putStr "Hello "
  putStrLn "Haskell!"
```

26.2.4. The print function

```
print :: Show a => a -> IO ()
```

The IO print function outputs a value of any [Show type](#) to the standard output device. We have been using the print function in various examples throughout this book.

26.3. Input Functions

26.3.1. The getChar function

```
getChar :: IO Char
```

The getChar function reads a character from the standard input device. It returns the value as IO In the following example, we create a simple function which repeatedly reads a character from the terminal and prints it back unless it is When 'x' is inputted, we simply return with

```
echoChar :: IO ()
echoChar = do
  c <- getChar ①
  case c of
    'x' -> return ()
    _   -> do putStrLn c; echoChar ②
```

①

Note that the [monadic](#) in the context of the do expression, effectively does a safe conversion of IO Char to Char in this example. That is, the type of c is

②

We recursively call echoChar in this example.

26.3.2. The getLine function

```
getLine :: IO String
```

The `getLine` function reads a line of text from the standard input device and it returns the value as an IO String Monad. Here's an essentially the same function, which "echoes" one line at a time, instead of one character at a time.

```
echoLine :: IO ()
echoLine = do
  line <- getLine
  case line of
    "exit" -> return ()
    _      -> do
      putStrLn line
      echoLine
```

①

Using the similar monadic assignment, we effectively convert IO String to String in this example.

26.3.3. The getContents function

```
getContents :: IO String
```

The getContents function returns all user input as a single string.

```
main = do
  content <- getContents
  putStr content
```

①

The getContents function continues to read the input until it encounters EOF (e.g., Ctrl+D). Note that this particular [do expression](#) is equivalent to the following using the [monadic binding](#)

```
main = getContents >>= putStr
```


26.3.4. The readIO function

```
readIO :: Read a => String -> IO a
```

The readIO function reads and parses a string, and it returns an IO monad value of a Read type. It raises an exception when the parse fails. The repeatNTimes function in the next example reads two strings as an Int and a list replicates the list by n times, and returns the result as IO

```
repeatNTimes :: String -> String -> IO [Int]
repeatNTimes rep list = do
  n <- readIO rep
  xs <- readIO list
  return $ concat $ replicate n xs
```

```
main = do
  list <- repeatNTimes "3" "[1, 2, 3]"
  print list
```

①

This will print

26.3.5. The readLn function

```
readLn :: Read a => IO a
```

The readLn function combines getLine and For example,

```
main = (readLn :: IO Int) >>= print ①
```

①

This read an input as an Int and prints out the value if parse is successful. Otherwise, it throws an error.

26.3.6. The interact function

```
interact :: (String -> String) -> IO ()
```

The `interact` function takes a function of type `String -> String` as its argument. The entire input from the standard input device is passed to this function as its argument, and the resulting string is outputted on the standard output device. For example, here's another version of the `echo` line function, which converts all input characters to uppercase letters.

```
import Data.Char (toUpper)

main = interact $ map toUpper
```

26.4. File Functions

`FilePath` is declared to be a type synonym for `String` in the Prelude.

26.4.1. The readFile function

```
readFile :: FilePath -> IO String
```

The `readFile` function reads a file and returns the content of the file as a string. For example, using the following function in the current directory,

```
$ cat hello.txt  
Hello, world  
ditto
```

```
main = do  
  content <- readFile "hello.txt" ①  
  print $ lines content           ②
```

①

If the named file is not found, it will throw an error.

②

If successful, it will print ["Hello,

26.4.2. The writeFile function

```
writeFile :: FilePath -> String -> IO ()
```

The `writeFile` function takes a file path and content string, and it writes the content to the given file. If the file does not exist, it creates a new file. If a file with the given name exists, it overwrites. For example,

```
main = do
  let quote = "The future belongs to those who believe in the beauty of their
  dreams."
  writeFile "world.txt" (quote ++ "\n") ①
  readFile "world.txt" >=> print ②
```

①

This IO action creates a file named `world.txt` in the current directory, if it does not exist, and it writes the string `quote` to the file.

②

This will print `The future belongs to those who believe in the beauty of their dreams.` to the terminal.

26.4.3. The appendFile function

```
appendFile :: FilePath -> String -> IO ()
```

The `appendFile` function takes a file path and a content string as two arguments, and it writes the content at the end of the given file. If the file does not exist, it creates a new file. For example,

```
main = do
  let quote2 = "The best way to predict the future is to invent it."
  appendFile "world.txt" quote2           ①
  future2 <- readFile "world.txt"
  print $ words future2                   ②
```

①

We use the same file used in the previous example. This IO action will append the given content, `quote2` after the current content.

②

Output:

Epilog

Haskell is a beautiful language. That is, once you get to know it. It is a shame that only a tiny fraction of the whole developer community end up using, and enjoying, programming languages like Haskell.

If you are reading this, congratulations! You passed the most difficult part of learning Haskell. Once you become familiar with this relatively foreign syntax of Haskell, the world is your oyster. You will quickly find out that you can do so much more with so much less with Haskell. And, more importantly, you will enjoy programming more, with Haskell.

Programming languages are not just for utility, just like natural languages are not just for utility. We enjoy Shakespeare, for instance, although it has no practical value. In this age of super AI and machine learning, when programming, as a human labor, is becoming possibly obsolete (although not any time soon), programming can still be useful, and enjoyable, like an art.

Haskell is a "higher-level" programming language. Functional programming is about rather than In imperative programming, you, as a programmer, have to tell exactly how things are done to the computer. That is why we, not the computer, learn algorithms and what not.

In the higher level programming, in the near future, we will not have to concern ourselves with exactly how. We will just need to tell computers (or, AIs) what to do. They will then figure out how best to do it. (Hopefully.) In our view, functional programming is a stepping stone to

that future. Languages like Haskell, which are more abstract and more high-level, can be the best tool for our next progress. We will see.

But, for now, go out and do some functional programming!

About the Author

Harry Yoon has been programming for over three decades. He has used over 20 different programming languages in his academic and professional career. His experience spans broad areas from scientific programming and machine learning to enterprise software and Web and mobile app development.

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